

Pt4

Thank you for your help in improving the revenue from our existing farms. Based on the increased revenue, we are now looking to expand our operations by working with additional farms to satisfy demand from industrial customers.

The six new farms have daily supply and milk fat content as given in the following table:

<i>Farm</i>	Cowbell	Creamy Acres	Milky Way	Happy Cows	Udder Delight	Fresh Pa
Supply (L)	8700	5400	8800	5400	8900	9300
Fat (%)	3.3	3.8	3.6	3.4	3.5	3.8

Note that none of these farms are organic and we do not have to take all the milk they supply.

The demand figures for whole milk and low fat milk on each day are given below:

<i>Demand (L)</i>	Mon	Tue	Wed	Thu	Fri	Sat	Sun
Whole Milk	13778	27488	68427	13740	27428	27519	82193
Low Fat Milk	3485	6896	17060	3543	6756	6794	20733

We do not have to meet all the demand. The wholesale selling prices for whole milk and low fat milk are \$0.90/L and \$0.92/L, respectively.

We effectively have no limit on production so we process as much milk as we need to every day, storing the finished product if necessary. We have no limit on storage, but there is a cost of \$0.05 (5 cents) per litre per day for refrigeration. Once again excess milk fat can be put to other uses.

How should we best plan our milk processing for the next seven days? Please provide us with the total income from this industrial production.

Sets

- $Farms$
- S : Supply
- F : Fat

Data

- W_w - wholesale price of whole milk (\$/L)
- W_l - wholesale price of low fat milk (\$/L)
- F_w - fat of whole milk (%)
- F_l - fat of low fat milk (%)
- S_f - supply from each farm (L)
- F_f - fat from each farm (%)
- C_s - cost of storage (\$/L/day)
- D_{wt} - demand of whole milk of a day (L)
- D_{lt} - demand of low fat milk of a day (L)

Variables

- P_{wft} - Production of whole milk from each farm (L) of a day
- P_{lft} - Production of low fat milk from each farm (L) of a day
- S_{wt} - Whole milk in storage (L) on a day
- S_{lt} - Low fat milk in storage (L) on a day

Objective function

$$\max(\sum_{t \in Days} (\sum_{f \in Farms} W_w * P_{wft} + W_l * P_{lft}) - (S_{wt} + S_{lt}) * C_s)$$

Constraints

$$\forall f \in Farms, \forall t \in Days, P_{wft} + P_{lft} \leq S_f$$

$$\forall t \in Days, \sum_{f \in Farms} F_w * P_{wft} + F_l * P_{lft} \leq \sum_{f \in Farms} S_f * F_f$$

$$S_{wt} = P_{wft} - Dwt + S_{wt-1}, \forall t \in Days \ t = 1$$

$$S_{lt} = P_{lft} - Dlt + S_{lt-1}, \forall t \in Days \ t = 1$$