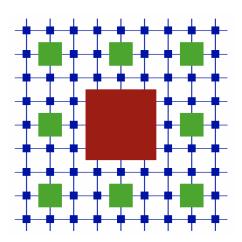
# CarpetX

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#### Abstract

TODO: Maybe change this description. CarpetX is a Cactus driver based on AMReX, a software framework for block-structured AMR (adaptive mesh refinement). CarpetX is intended for the Einstein Toolkit.

### 1 Introduction

TODO: This document should cover the topics listed here.
TODO: We should have some words explaining what CarpetX is.

- 1. loop.hxx/where\_t/ghosts\_inclusive
- 2. What loop functions should be used? loop\_device or the other ones?
- 3. Picture of grid regions

# 2 Building and using standard images

# 3 Writing CCL files

### 3.1 configuration.ccl

TODO: talk about requirements for bringing carpetx things in for accessing the APIs

#### 3.2 interface.ccl

TODO: talk about new tags

#### 3.3 schedule.ccl

TODO: Talk about important new schedule bins and the read/write safeguards on schedules.

#### 3.4 Preprocessor macros

TODO: Talk about new macros and new macro features. The test below is mostly ok, but needs to be adapted

The macros DECLARE\_CCTK\_ARGUMENTSX\_WaveToyX\_RHS, CCTK\_ARGUMENTS and DECLARE\_CCTK\_PARAMETERS allow the thorn writer to access parameters and grid functions declared in the thorn's .ccl files. Note that Cactus now supports the DECLARE\_CCTK\_ARGUMENTSX\_FUNC\_NAME macro, where FUNC\_NAME is the name of a grid function declared in the schedule.ccl file. These macros restrict the access of a function to it's schedule-declared grid functions. More importantly, it provides a variable called grid which can be used to access the functionalities of the Loop API.

## 4 Loops over grid elements

In CarpetX loops over grid elements are not written explicitly. Operations that are to be executed for every grid element (cells, edges or points) are specified via C++ lambda functions, also known as closures or anonymous functions.

These objects behave like regular C++ functions, but can be defined *inline*, that is, on the body of a function or as an argument to another function.

An important concept to grasp with lambda function is *captures*. If a lambda (let us call this the child function) is defined in the body of an outer function (let us call this the parent function), the child can access variables defined in the parent function, provided that these variables are *captured*. The two most relevant modes of capture while using CarpetX are *capture by reference* (denoted with the & sign in the square brackets denoting the start of the lambda) and *capture by value* (denoted by an = sign inside the square brackets of the lambda declaration).

When running on GPUs, captures by value are *required* and captures by reference are *forbidden*. This is because data must be copied from host (CPU side) memory to device (GPU side) memory in order to be executed.

The API for writing loops in CarpetX is provided by the Loop thorn. To use it, one must add

```
1 REQUIRES Loop
```

to the thorn's configuration.ccl file and

```
INHERITS: CarpetX
USES INCLUDE HEADER: loop.hxx  # For using CarpetX on CPUs
USES INCLUDE HEADER: loop_device.hxx # For using CarpetX on GPUs
```

to the thorn's interface.ccl file. Furthermore, one must include the Loop API header file in all source files where the API is needed by adding

```
1 #include <loop.hxx>
2 #include <loop_device.hxx>
```

to the beginning of the source file.

TODO: Figure out whether we need both of these header files

### 4.1 Loop regions

Before actually writing any code that iterates over grid elements, one must choose *which* elements are to be iterated over. We shall refer to the set of points in the grid hierarchy that will be iterated over when a loop is executed as a *Loop region*. The following regions are defined in the Loop API:

- 1. All: This region refers to all points contained in the grid. Denoted in code by the all suffix.
- 2. Interior: This region refers to the interior of the grid. Denoted in code by the int prefix.

3. Outermost interior: This region refers to the outermost "boundary" points in the interior. They correspond to points that are shifted inwards by = cctk\_nghostzones[3] from those that CarpetX identifies as boundary points. From the perspective of CarpetX (or AMReX), these do not belong in the outer boundary, but rather the interior. This excludes ghost faces, but includes ghost edges/corners on non-ghost faces. Loop over faces first, then edges, then corners. Denoted in code by the outermost\_int suffix.

TODO: Picture of grid regions

### 4.2 Loop methods

Loop API functions are methods of the GridDescBase or GridDescBaseDevice classes which contain functions for looping over grid elements on the CPU or GPU, respectively. TODO: Is this correct? Do we need these two classes? Can we make it with on. The macro DECLARE\_CCTK\_ARGUMENTSX\_FUNCTION\_NAME provides a variable called grid, which is an instance of either of these classes. The name of each looping method is formed according to

```
loop_ + <loop region>+ [_device]
```

For example, to loop over boundaries using the CPU one would call

```
1 grid.loop_bnd <...>(...);
```

To obtain a GPU equivalent version, one would simply append \_device to the function name. Thus, for example, to loop over the interior using a GPU, one would call

```
1 grid.loop_int_device <...>(...);
```

Let us now look at the required parameter of loop methods. The typical signature is as follows

```
template <int CI, int CJ, int CK, ..., typename F>
void loop_REG_PU(const vect<int, dim> &group_nghostzones, const F &f);
```

The template parameters meanings are as follows:

- 1. CI: Centering index for the first grid direction. Must be set explicitly and be either 0 or 1. 0 means that this direction will be looped over grid vertices, while 1 means that it will be looped over cell centers.
- 2. CJ: Centering index for the second grid direction. Must be set explicitly and be either 0 or 1. 0 means that this direction will be looped over grid vertices, while 1 means that it will be looped over cell centers.
- 3. CK: Centering index for the third grid direction. Must be set explicitly and be either 0 or 1. 0 means that this direction will be looped over grid vertices, while 1 means that it will be looped over cell centers.
- 4. F: The type signature of the lambda function passed to the loop. It is not required to be set explicitly and is automatically deduced by the compiler.

Note that centering indexes can be mixed: setting the indices to (1,0,0), for instance, creates loops over faces on the x direction. Function parameter meanings are as follows:

- 1. group\_nghostzones: The number of ghost zones in each direction of the grid. This can be obtained by calling grid.nghostzones.
- 2. f: The C++ lambda to be executed on each step of the loop.

#### 4.3 Loop Lambdas

We shall now discuss the syntax and the available elements of the lambda functions that are to be fed to the Loop methods described in Section 4.2.

To start, let us be reminded of the general syntax of a lambda function in C++:

```
// append ; if assigning to a variable
[capture_parameter] (argument_list) -> return_type { function_body }
```

When running on GPUs, the capture\_parameter field used should always be =, indicating pass by value (copy) rather than &, indicating pass by reference. The argument\_list of the lambda should receive only one element of type PointDesc (which will be described on Sec. 4.4) and the lambda must return no value, which means that return\_type can be omitted altogether.

This means that a typical lambda passed to a loop method will have the form

```
1 [=] (const Loop::PointDesc &p) {
2  // loop body
3 }
```

#### 4.4 The PointDesc type and loop lambda body

The PointDesc type provides a complete description of the current grid element in the loop. The following members are the ones that are expected to be used more often:

- 1. I: A 3-element array containing the grid point indices.
- 2. DI: A 3-element array containing the direction unit vectors from the current grind point.
- 3. X: A 3-element array containing the point's coordinates.
- 4. DX: A 3-element array containing the point's grid spacing.
- 5. iter: The current loop iteration.

In the body of a loop lambda, grid functions declared in the thorn's interface.ccl file are available as GF3D2 objects, which are C++ wrappers around native Cactus grid functions. These objects are accessible by directly calling them as functions taking arrays of grid indices as input. Such indices, in turn can be obtained by directly accessing PointDesc members.

### 4.5 Example: Computing a RHS with finite differences

Let us now combine the elements describe thus far into a single example. Let us suppose that the following system of PDEs is implemented in Cactus:

$$\partial_t u = \rho \tag{1}$$

$$\partial_t \rho = \partial_x^2 u + \partial_y^2 u + \partial_z^2 u \tag{2}$$

Let us suppose that the grid functions u and rho where made available, while grid functions u\_rhs and rho\_rhs are their corresponding RHS storage variables. The function that computes the RHS of Eqs. (1)-(2) can be written as

```
1
   extern "C" void LoopExample_RHS(CCTK_ARGUMENTS) {
 2
     DECLARE_CCTK_ARGUMENTS_LoopExample_RHS;
 3
     DECLARE_CCTK_PARAMETERS;
 4
     // The grid variable is implicitly defined via the CCTK macros
 5
 6
     // A 0/1 in template parameters indicate that a grid is vertex/cell
         centered
 7
     grid.loop_int < 0, 0, 0 > (
       grid.nghostzones,
 8
 9
10
        // The loop lambda
        [=] (const Loop::PointDesc &p) {
11
          using std::pow;
12
13
          const CCTK_REAL hx = p.DX[0] * p.dX[0];
14
          const CCTK_REAL hy = p.DX[1] * p.dX[1];
15
          const CCTK_REAL hz = p.DX[2] * p.dX[2];
16
17
          const CCTK_REAL dudx = u(p.I - p.DI[0]) - 2 * u(p.I)
18
            + u(p.I + p.DI[0])/hx;
19
20
21
          const CCTK_REAL dudy = u(p.I - p.DI[1]) - 2 * u(p.I)
22
            + u(p.I + p.DI[1])/hy;
23
24
          const CCTK_REAL dudz = u(p.I - p.DI[2]) - 2 * u(p.I)
25
            + u(p.I + p.DI[2])/hz;
26
27
          u_rhs(p.I) = rho(p.I);
28
          rho_rhs(p.I) = ddu;
29
       } // Ending of the loop lambda
30
     ); // Ending of the loop_int call
31
32
```

Name	Description			
constant	The state vector is kept constant in time			
Euler	Forward Euler method			
RK2	Explicit midpoint rule			
RK3	Runge-Kutta's third-order method			
RK4	Classic RK4 method			
SSPRK3	Third-order Strong Stability Preserving Runge-Kutta			
RKF78	Runge-Kutta-Fehlberg 7(8)			
DP87	Dormand & Prince 8(7)			
Implicit Euler	Implicit Euler method			

Table 1: Available methods in ODESolvers

#### 4.6 SIMD Vectorization of loops

TODO: See SIMDWaveToyX/src/simdwavetoyx.cxx TODO: Do the fused SIMD operations declared in Arith can be used?

## 5 Using flux

## 6 Time integration using ODESolvers

In CarpetX, time integration of PDEs via the Method of Lines is provided by the ODESolvers thorn. This makes time integration tightly coupled with the grid driver, allowing for more optimization opportunities and better integration.

From the user's perspective, ODESolvers is very similar (and sometimes even more straightforward) the MoL thorn, but a few key differences need to be observed. Firstly, not all integrators available to MoL are available to ODESolvers. The list of all supported methods is displayed in Tab. 1. Method selection occurs via configuration file, by setting

```
1 ODESolvers::method = "Method name"
```

and the default method used if none other is set is "RK2".

Additionally, users can set verbose output from the time integrator by setting

```
1 ODESolvers::verbose = "yes"
```

By default, this option is set to "no". Finally, to control the step size of the time integrator, it is possible to set the configuration parameter CarpetX::dtfac, which defaults to 0.5, is defined as

$$dtfac = dt / min(delta\_space)$$
 (3)

where min(delta\_space) refers to the smallest step size defined in the CarpetX grid and dt is the time integrator step.

To actually perform time evolution, the PDE system of interest needs to be declared to Cactus as a set of Left-Hand Side (or LHS, or more commonly *state vector*) grid functions plus a set of Right-Hand

Side (RHS) grid functions. The RHS grid functions correspond exactly to the right-hand side of the evolution equations while the state vectors stores the variables being derived in time in the current time step. More time steps can be stored internally, depending on the time integrator of choice, but this is an implementation detail that is supervised automatically by ODESolvers. To make this clear, consider the PDE system comprised of Eqs. (1)-(2). In this example, the state vector would be the set  $(u, \rho)$  while the right-hand side would be all elements to the right of the equal signs. Note that derivative appearing on the RHS are only derivatives in space. By discretizing space with a grid and replacing continuous derivatives with finite approximations (by using finite differences, for instance) the time-space dependent PDE system now becomes a ODE system in time, with the state vector being the sought variables. By providing the RHS of the PDE system, ODESolvers can apply the configured time stepping method and compute the next time steps of the state vector.

To see how ODESolvers is used in practice, let us turn once again to the WaveToyX example, bundled with CarpetX. To begin, let us look at an excerpt from this example's interface.ccl file

```
CCTK_REAL state TYPE=gf TAGS='rhs="rhs" dependents="energy error"'
1
2
     {
3
        u
4
        rho
5
     } "Scalar wave state vector"
6
7
     CCTK_REAL rhs TYPE=gf TAGS='checkpoint="no"'
8
     {
9
        u_rhs
10
        rho_rhs
11
     } "RHS of scalar wave state vector"
12
13
      . . .
```

In lines1-5, the group of real grid functions called state, consisting of grid function u and rho, is declared. The TYPE=gf entry indicates that the variables in this group are grid functions (more details on Sec. 3). The TAGS entry is particularly important in this instance. It consists of a single quote string (marked by ') with space separated key-value pars of the form key="value". The rhs="rhs" pair indicates that these grid functions have an associated RHS group, that is, a group of variables with grid functions responsible for storing the PDE system's RHS and this group is called "rhs" which is defined later in lines 7-11. This information is used by ODESolvers while taking a time step and is tightly coupled to Cactus file parsers. In lines 7-11, the rhs group is declared with two real grid functions, u\_rhs and rho\_rhs. These variables will be responsible for holding the RHS data of the PDE, which will in turn be used by ODESolvers.

The next step is to schedule the execution of functions into their correct schedule groups. The most relevant schedule groups provided by <code>ODESolvers</code> are <code>ODESolvers\_RHS</code> and <code>ODESolvers\_PostStep</code>. The former is the group where one evaluates the RHS of the state vector everywhere on the grid and the latter is where boundary conditions are applied to the state vector, and projections are applied if necessary. For example, looking at <code>WaveToyX</code>'s <code>schedule.ccl</code> file, one sees

```
SCHEDULE WaveToyX_RHS IN ODESolvers_RHS

{
LANG: C
READS: state(everywhere)
WRITES: rhs(interior)
SYNC: rhs
} "Calculate scalar wave RHS"
```

Name	Type	Possible Values	Default Value	Description
shape_n	String	"sphere" or "cube"	"sphere"	Shape of refined region
active_n	Boolean	"yes" or "no"	"yes"	Is this box active?
num_levels_n	Single integer	[1, 30]	1	Number of refinement levels for this box
$position_x_n$	Single real number	Any real	0.0	x-position of this box
position_y_n	Single real number	Any real	0.0	y-position of this box
$position_z_n$	Single real number	Any real	0.0	z-position of this box
radius_n	30 element array of reals	-1.0 or positive real	-1.0 (radius ignored)	Radius of refined region for this level
radius_x_n	30 element array of reals	-1.0 or positive real	-1.0 (radius ignored)	x-radius of refined region for this level
radius_y_n	30 element array of reals	-1.0 or positive real	-1.0 (radius ignored)	y-radius of refined region for this level
radius_z_n	30 element array of reals	-1.0 or positive real	-1.0 (radius ignored)	z-radius of refined region for this level

Table 2: Configuration parameters for a single (1 out of 3) box that can be defined in parameter files using the BoxInBox thorn.

The schedule statement from lines 1-7 schedules the function that computes the RHS of the wave equation. Note that the function reads the state on the whole grid and writes to the RHS grid variables in the interior. With CarpetX, grid functions read and write statements are enforced: You cannot write to a variable which was declared as read only in the schedule.ccl file. Lines 9-15 exemplify the scheduling of a function in the ODESolvers\_PostStep group, which is executed after ODESolvers\_RHS during the time stepping loop. In this particular example, the scheduled function is computing the energy associated with the scalar wave equation system. These are all the required steps for using ODESolvers to solve a PDE system via the method of lines.

# 7 Implementing boundary conditions

# 8 Adding and controlling AMR

#### 8.1 Box-in-box AMR

CarpetX supports fixed mesh refinement via the so called box-in-box paradigm. This capability is provided by the BoxInBox thorn. Using it is very simple and similar to Carpet's CarpetRegrid2 usage.

All configuration of boxes and levels are performed within configuration files. BoxInBox supports adding 3 "boxes" or "centers". Each box can be configured as summarized in Tab. 2. The n suffix should be replaced by 1, 2 or 3 for configuring the corresponding boxes. Each box can be shaped differently as either Cartesian-like cubes or spheres and support configuring up to 30 levels. Level's positions and radii can be set independently for each dimension. Note that for each box the active, num\_levels and position\_(xyz) field are stored as grid scalars. Each of the 30 refinement level radii and x, y, z individual radii for each box are also stored as grid arrays. This allows these parameters to be changed during a simulation run, allowing for moving boxes. This is useful, for example, when implementing a

puncture tracker.

These configurations are subjected to (and restricted by) two additional CarpetX configurations, namely CarpetX::regrid\_every, which controls how many iterations should pass before checking if the box grid variables have changed and CarpetX::max\_num\_levels which controls the maximum number of allowed refinement levels.

As an example, we present a configuration file excerpt for creating two refinement boxes with the  ${\tt BoxInBox}$  thorn

```
1
     BoxInBox::num_regions = 2
2
     BoxInBox::num_levels_1 = 2
3
     BoxInBox::position_x_1 = -0.5
4
5
     BoxInBox::radius_x_1[1] = 0.25
6
     BoxInBox::radius_y_1[1] = 0.5
7
     BoxInBox::radius_z_1[1] = 0.5
8
     BoxInBox::num_levels_2 = 2
9
     BoxInBox::position_x_2 = +0.5
10
     BoxInBox::radius_x_2[1] = 0.25
11
     BoxInBox::radius_y_2[1] = 0.5
12
13
     BoxInBox::radius_z_2[1] = 0.5
```

TODO: Add example for changing the boxes during runtime. Where to schedule the function that changes the boxes?

#### 8.2 Advanced AMR

CarpetX supports non-fixed (adaptive) mesh refinement. For cell level control of AMR, CarpetX provides user with a cell centered and non-checkpointed grid function called regrid\_error. Users are responsible for filling this grid function with real value however they see fit. Once it is filled, the configuration parameter CarpetX::regrid\_error\_threshold controls regridding: If the values stored in regrid\_error are larger than what is set in regrid\_error\_threshold, the region gets refined. Additionally, the configuration parameter CarpetX::regrid\_every controls how many iterations should pass before checking if the error threshold has been exceeded. The parameter CarpetX::max\_num\_levels controls the maximum number of allowed refinement levels.

Note that CarpetX does not provide a "standardized" regrid error routine. This is because refinement criteria are highly specific to the problem being solved via AMR, and thus there is no one size fits all error criteria. This might seem inconvenient, but ultimately it allows for users to have higher degrees of customization in their AMR codes. For demonstration purposes, we shall now provide a routine that estimates the regrinding error as TODO: what? Provide a good starter example. This implementation could be used as a starting point for codes that wish to use different error criteria in their AMR grids.

```
extern "C" void EstimateError(CCTK_ARGUMENTS) {
DECLARE_CCTK_ARGUMENTSX_EstimateError;
DECLARE_CCTK_PARAMETERS;

// The template indices indicate this a loop over cell centers
// Remember that regrid_error is a cell centered grid function
```

Once defined, EstimateError should be scheduled in both the postinitial and poststep bins. The poststep bin gets called right after a new state vector has been calculated, and is thus the proper place to analyze it. The postinitial scheduling is also necessary for computing the initial refinement after initial conditions have been set up. A thorn making use of the regrid\_error AMR mechanism should then add the following to its schedule.ccl file:

```
1
     SCHEDULE EstimateError AT postinitial
2
3
       LANG: C
4
       READS: state(everywhere)
       WRITES: CarpetX::regrid_error(interior)
5
6
     } "Estimate error for regridding"
7
8
     SCHEDULE EstimateError AT poststep
9
10
       LANG: C
11
       READS: state(everywhere)
       WRITES: CarpetX::regrid_error(interior)
12
13
     } "Estimate error for regridding"
```

- 9 Analyzing data
- 9.1 OpenPMD
- 9.2 SILO
- 10 Interpolation
- 11 Acknowledgements

References