### University of Bergen Department of Informatics

### Hidden parallelepiped in Hawk

Author: Eirik Djupvik Skjerve

Supervisors: Igor Aleksandrovich Semaev & Martin Feussner



# UNIVERSITETET I BERGEN Det matematisk-naturvitenskapelige fakultet

November, 2024

#### Abstract

Quantum computers threaten todays encryption schemes. NIST asked for new standards, among them is HAWK. This thesis will investigate if HAWK is secure against a variation of an attack that broke NTRU-Sign.



Thank you to some people

Eirik D. Skjerve

Saturday 2<sup>nd</sup> November, 2024

## Contents

1	Introduction				
	1.1	Conte	xt and motivation	1	
	1.2	Object	tives	2	
	1.3	Thesis	soutline	2	
<b>2</b>	Background				
	2.1	Asymı	metric cryptography	3	
		2.1.1	Digital signatures	3	
		2.1.2	Hash-Then-Sign	3	
		2.1.3	GGH	3	
	2.2	Linear	algebra & lattices	3	
		2.2.1	Lattices	3	
	2.3	Proba	bility theory	3	
		2.3.1	Distributions	3	
3	Hav	vk and	Learning a parallelepiped	4	
	3.1	Hawk		4	
		3.1.1	Simple Hawk	4	
		3.1.2	Key generation	5	
		3.1.3	Signature generation	5	
		3.1.4	Signature verification	5	
	3.2	Learni	ing a parallelepiped	5	
		3.2.1	Assumptions	5	
		3.2.2	Covariance matrix	5	
		3.2.3	Hidden parallelepiped to hidden hypercube	5	
		3.2.4	Gradient descent	5	
		3.2.5	Hawk resistance against HPP	5	
	3.3	Imple	mentation	5	

4 Adap	Adapting HPP to Hawk		
4.1	Covariance matrix secret key in Hawk	6	
Bibliography			
A Gene	erated code	8	

### Introduction

#### 1.1 Context and motivation

Digital signatures are an important part of secure communication today. The most used cryptographic scheme used for digital signatures today is DSA (Digital Signature Algorithm) or RSA (Rivest, Shamir, and Adleman) signatures (source). However, in 1994, Peter Shor developed Shor's algorithm, which, given a large enough quantum computer, is able to solve the hard problems DSA and RSA is based upon, namely the Discrete Logarithm Problem and Prime Factorization(source). Whether big enough quantum computers will emerge any time soon is debatable. However, measures against this potential looming threat has already begun. In 2016, NIST (National Institute of Standards and Technology) announced a standardization process for new standard schemes for KEMs (Key Encapsulation Methods) and digital signatures that have strong security against quantum computers (source). Many of the submissions to this process, including KRYSTALS-Dilithium which is to be standardized, are based on lattice problems that are believed to be hard to solve for both classical and quantum computers (source).

Cryptographic schemes based on lattice problems are not an enirely new phenomenon, however. NTRU-Sign, published in 2003(source), is a digital signature scheme based on the hardness of the Closest Vector Problem (source). The original scheme was broken due to Phong. Q. Nguyen & Oded Regev in 2006 [3], who showed that by observing enough signatures generated with one secret key, one can retrieve the secret key. A newer

digital signature scheme, Hawk (source), submitted to NIST's standardization process, is a scheme similar that of NTRU and GGH. The goal of this thesis is to try and adapt the Hidden Parallelepiped Problem attack to Hawk [2]. Hawk spec here [1]

#### 1.2 Objectives

The objective for this thesis consists of two main parts:

- Implementation of Hawk in Rust. As the first part of the thesis I implement the Hawk digital signature scheme in the Rust programming language. Implementing a scheme on ones own is a good way to actually learn how it works. I chose to implement it in Rust for the sake of learning the programming language. Moreover, having ones own version makes it easier to experiment, adjust and modify to ones need. It would also be a challenge to understand and work with complicated source code someone else has written.
- Cryptanalysis and experimentation. As part two of the thesis I want to do cryptanalysis of Hawk. The goal is to use the "Learning a parallelepiped" attack [3] and adjusting it to try and break Hawk. This requires both theoretical and practical work, and experiments will be implemented in Rust.

#### 1.3 Thesis outline

Chapter 2 will introduce important notions and mathematical background used in this thesis. Chapter 3 will introduce Hawk and the *Learning a Parallelepiped* attack and implementations of these. In Chapter 4, a version HPP attack aimed at Hawk will be presented. Chapter 5 will show results, and Chapter 6 will discuss future work.

## Background

- 2.1 Asymmetric cryptography
- 2.1.1 Digital signatures
- 2.1.2 Hash-Then-Sign
- 2.1.3 GGH
- 2.2 Linear algebra & lattices
- 2.2.1 Lattices
- 2.3 Probability theory
- 2.3.1 Distributions

## Hawk and Learning a parallelepiped

#### 3.1 Hawk

In the following Hawk, the digital signature scheme, will be presented, as in [1]

#### 3.1.1 Simple Hawk

Present simple sketch of keygen, sign and ver, as well as an example in dimension 2

- 3.1.2 Key generation
- 3.1.3 Signature generation
- 3.1.4 Signature verification
- 3.2 Learning a parallelepiped
- 3.2.1 Assumptions
- 3.2.2 Covariance matrix
- 3.2.3 Hidden parallelepiped to hidden hypercube
- 3.2.4 Gradient descent
- 3.2.5 Hawk resistance against HPP

#### 3.3 Implementation

Something something about the implementation of Hawk in Rust. Mentions of sampling, integer/float types, speed and comparison to Hawk team's C code?

Something something about the implementation of HPP in Rust. Something about speedup/parallelization of gradient descent?

# Adapting HPP to Hawk

In this chapter we investigate the steps needed to possibly apply the Hidden Parallelepiped Problem to the Hawk digital signature scheme.

#### 4.1 Covariance matrix secret key in Hawk

Nothing yet I'm afraid

## **Bibliography**

[1] Joppe W. Bos, Olivier Bronchain, Léo Ducas, Serge Fehr, Yu-Hsuan Huang, Thomas Pornin, Eamonn W. Postlethwaite, Thomas Prest, Ludo N. Pulles, and Wessel van Woerden. Hawk. Technical report, NXP Semiconductors, Centrum Wiskunde & Informatica, Mathematical Institute at Leiden University, NCC Group, PQShield, Institut de Mathématiques de Bordeaux, September 2024.

URL: https://hawk-sign.info/.

[2] Léo Ducas, Eamonn W. Postlethwaite, Ludo N. Pulles, and Wessel van Woerden. Hawk: Module LIP makes lattice signatures fast, compact and simple. Cryptology ePrint Archive, Paper 2022/1155, 2022.

URL: https://eprint.iacr.org/2022/1155.

[3] Phong Q. Nguyen and Oded Regev. Learning a parallelepiped: Cryptanalysis of ggh and ntru signatures, 2009.

### Appendix A

#### Generated code

Listing A.1: Source code of something

1 println!("Goodbye World");