

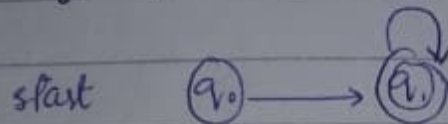
Tuesday
21/02/19

①

→ Deterministic: For any particular input, it gives particular output

→ Recognizable: Reached to final state.

Model for infinite possible numbers



→ Valid Machine: Accepts valid while rejects invalid.

→ Lexical Analyser: left to right scan and recognize a valid word / alphabet.

Tokenization is a technique.

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→ Alphabets :-

-- Finite set of symbols or letters.

eg:

$\Sigma = \{a, b\}$

$\Sigma = \{0, 1\}$

Ram → Cache

32-bit instruction

4 bits → opcode

28 bits → address

CU → reads opcode and recognize instruction

eg: Alphabets of OOL

$\{0 - 7, 10 - 17, 20, 27 - 30 \dots\}$

eg: $\Sigma = \{ab, cd\} \rightarrow 2 \text{ alphabets}$

ALGOL → 113 letters.

Includes letters, digits and variety of operators such as GOTO and IF.

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→ Strings:

- - Concatenation of finite symbols from alphabet.

→ Empty String: String with 0 character.
Zero occurrence of alphabets.

Transition without 0 input is expressed as Empty string.

eg: Screen saver → Time is input but it happens when you do nothing.

Denoted by " Λ " or " ϵ ".

→ Words:

- - They are strings. (set of alphabets).
- - It belongs to some language.

eg:

* String with max length 2
 $\Sigma = \{a, b, ab, ba\}$.

When we impose some conditions.

"{All Words are strings but not all strings are Words}."

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eg:

$$L = \{x^n, n = 1, 2, 3\}$$

$$V = \underbrace{\{x, xx, xxx\}}_{\text{words \& strings}} \underbrace{\{xxxx, xxxxx\}}_{\text{strings}}$$

$$L = \{x^{\text{odd}}\}$$

$$V = \underbrace{\{x, xxx, xxxxx\}}_{\text{words \& strings}}$$

→ Valid / Invalid Alphabets

Invalid → multiple symbols alphabet
 $\Sigma = \{B, ab, Bab\} \rightarrow 3 \text{ words}$

Eg: $\Sigma = \{B, Ba, bab, d\}$
string → BababB.

.. If ambiguity is there while tokenizing a string then it is invalid.

.. If an alphabet is a prefix of another alphabet in a same set it means that alphabet is invalid.

source program + input \rightarrow interpreter \rightarrow output .
(5)

source program \rightarrow compiler \rightarrow target program

$\Sigma_1 = \{B, aB, bab, d\} \rightarrow \text{valid}$

$\Sigma_2 = \{B, Ba, bab, d\} \rightarrow \text{invalid b/c of ambiguity.}$

\rightarrow length of strings =

• - Denoted by $|S|$.

• - Number of letters in strings.

eg :

$\Sigma = \{B, aB, bab, d\}$

$S = BaBbabd$

Tokenizing = $(B), (aB), (bab), (d)$.

$|S| = 4$.

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⑥

→ Reverse of a string =

Rewriting of tokens of a string in
reverse order

$$\begin{aligned}\text{eg: } L &= \{10, 01\} \\ S &= 100110 \\ S^r &= 100110\end{aligned}$$

$$\begin{aligned}L &= \{1, 0\} \\ S &= 100110 \\ S^r &= 011001\end{aligned}$$

$$\begin{aligned}L &= \{a, b, c\} \\ S &= \{a b c\} \\ S^r &= c b a\end{aligned}$$

$$\begin{aligned}L &= \{B, aB, bab, d\} \\ S &= B a B b a b B d \\ \text{Rev}(S) &= d B b a b a B B\end{aligned}$$

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→ Operation on Words.

* Repetition of words upto n times

$$W^n = \underbrace{WW \dots W}_n$$

eg: $(abba)^2 = abbaabba$.

$$W^0 = \Lambda$$

$$(abba)^0 = \Lambda$$

* The set of all possible string from alphabet Σ including empty string.
* operation.

$$\Sigma = \{a, b\}$$

$$\Sigma^* = \{\Lambda, a, b, aa, ab, ba, bb, aaa, aab, \dots\}$$

$$(ab)^* = \{\Lambda, ab, abab, ababab, \dots\}$$

$$(a+b)^* = \{\Lambda, a, b, ab, aba, \dots\}$$

$$a+b = b+a$$

$$a \cdot b \neq b \cdot a$$

$$\bigcirc \xrightarrow{a} \bigcirc \xrightarrow{b} \bigcirc \quad \text{a followed by b}$$

$$\bigcirc \xrightarrow{b} \bigcirc \xrightarrow{a} \bigcirc \quad \text{b followed by a.}$$

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* + Operation.

The set of all possible strings from alphabet Σ except Λ .

$$\Sigma = \{a, b\}$$

$$\Sigma^+ = \Sigma^* - \{\Lambda\}$$

$$\Sigma^+ = \{a, b, ab, aa, \dots\}$$

→ Operation on languages.

A language is any subset of Σ^*

Language of all possible words

$$\Sigma = \{a, b\}$$

$$\Sigma^* = \{\Lambda, a, b, aa, ab, \dots\}$$

(Identifier → user defined names)

Identifiers → infinite language.

Keywords → finite language.

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NOTE :

→ $\phi = \{ \} \neq \{ \Lambda \}$ ^{language which contains empty string}

The language contains no words.

→ Set size $|\{ \}| = |\phi| = 0$

→ Set size $|\{ \Lambda \}| = 1$

→ String length $|\Lambda| = 0$.

$L = \{ a^n b^n : n \geq 0 \}$.
 Λ ^(order)
ab
aabb
aaa bbb } words
infinite language.

$abb \notin L$ (condition satisfy nhi hori).

→ The Usual Set Operations

* $\{ a, ab, aaaa \} \cup \{ bb, ab \} = \{ a, ab, bb, aaaa \}$.

* $\{ a, ab, aaaa \} \cap \{ bb, ab \} = \{ ab \}$.

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$$* \{a, ab, aaaa\} - \{bb, ab\} = \{a, aaaa\}$$

$$\bar{L} = \Sigma^* - L$$

* Complement universal language

$$\{a, ba\} = \{a, b, aa, ab, bb, aaa, \dots\}$$

$a, ba, aba, baa, aaba, baaa, baba$

The complement operation is a subtraction operation of given language from a universal language.

→ Reverse of a Language :-

$$L^R = \{w^R : w \in L\}$$

$$\{ab, aab, baba\}^R = \{ba, baa, abab\}$$

eg: $L = \{a^n b^n : n \geq 0\}$

$$L^R = \{b^n a^n : n \geq 0\}$$

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→ Concatenation

(Cartesian Product)

$$\{ \text{Concat}(\{L_1\}, \{L_2\}) \}$$

$$L_1 L_2 = \{xy : x \in L_1, y \in L_2\}$$

$$\{a, ab, ba\} \{b, aa\}$$

$$= \{ab, aab, abb, abaa, bab, baaa\}$$

If language is infinite then resultant will also be infinite.

→ Power operation on Languages:

$$L^n = \underbrace{L L \dots L}_n$$

$$\{a, b\}^3 = \{a, b\} \{a, b\} \{a, b\} =$$

$$\{aaa, aab, aba, abb, baa, bab, bba, bbb\}$$

$$L^0 = \{\epsilon\}$$

→

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$$* L^2 = \{a^n b^n a^m b^m : n, m \geq 0\}$$

$$aabb a a bbb \in L^2$$

$$* L^3 = \{a^n b^n a^m b^m a^p b^p : n, m, p \geq 0\}$$

→ Star Closure on languages (Kleene*) :-

$$L^* = L^0 \cup L^1 \cup L^2 \cup \dots$$

$$\{a, bb\}^* = \Lambda$$

a, bb
aa, abb, bba, bbbb
aaa,

$$L^1 = \{a, ab\}$$

$$L^0 = \Lambda$$

$$L^2 = \{a a b, a b a, a a \mid a b a b\}$$

$$L^3 = \{a b a b a b, a a a, a a b a\}$$

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→ Defining Language:

1. Descriptive definition of a language:
-- A theoretical expression of language.

2. Regular expressions:
-- Defining language through mathematical notation.

3. Finite Automata:
-- Models, abstract machines.

1 Descriptive definition:

-- The language L of strings of odd length defined over $\Sigma = \{a\}$ can be written as:
$$L = \{a, aaa, aaaaa, \dots\}$$

-- The language L of strings that does not start with 'a' defined over $\Sigma = \{a, b, c\}$ can be written as
$$L = \{b, c, ba, \dots\}$$

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- - The language L of strings of length 2 defined over $\Sigma = \{0, 1, 2\}$ can be written as:
 $L = \{01, 02, 10, \dots\} \quad (0+1+2) \{2\}$
- - The language L of strings ending in '0' defined over $\Sigma = \{0, 1\}$ can be written as:
 $L = \{0, 00, 10, \dots\}$
- - Language EQUAL of strings with no. of a's equals to no. of b's defined over $\Sigma = \{a, b\}$
 $L = \{\lambda, ab, abab, abba, \dots\}$
- - Language EVEN-EVEN of strings with even no. of a's and even no. of b's defined over $\Sigma = \{a, b\}$
 $L = \{\lambda, aabb, abab, \dots\}$
- - The language PRIME of strings defined over $\Sigma = \{a\}$, as $\{a^p : p \text{ is prime}\}$ can be written as
 $L = \{a, aa, aaa, \dots\}$

1. Palindrome

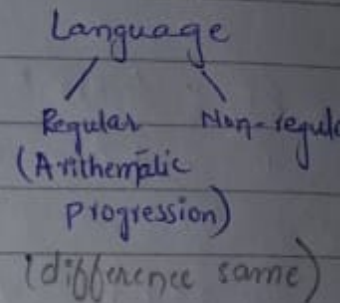
The language consisting of Λ and the strings S defined over Σ such that $\text{Rev}(S) = S$.

$$\Sigma = \{a, b\},$$

$$L = \{\Lambda, a, b, aa, bb, aqa, aba, \dots\}.$$

2. Regular Expressions:

It's a mathematical notation that can express Regular languages.



Regular Expression is a pattern to express the language.

$*$ \rightarrow zero or more occurrence of alphabets

$+$ \rightarrow one or more occurrence

\cdot \rightarrow concatenation.

$?$ \rightarrow 0, 1

$$[abc] \rightarrow [a \text{ or } b \text{ or } c]$$

$$(a+b+c) \rightarrow aubuc$$

$$a\{2\} \rightarrow \{aa\}$$

$$a?\{\Lambda, a\}$$

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eg: $(a+b.c)^*$

describes the language

$\{a, b, c\}^* = \{\lambda, a, bc, aa, abc, bca, \dots\}$

RE = $(a+b)^*$

$L = \{\lambda, b, a, aa, bb, aba, \dots\}$

RE = $(ab)^*$

$L = \{\lambda, ab, abab, ababab, \dots\}$

$a^* + b^* \neq (a+b)^*$

NOTE:

- - 'All finite languages are regular'.
- - 'There are some finite languages where there is no A.P.'

Q Can we use Regular expression for finite languages with no A.P.

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$$(a^*b^*)^* = (a+b)^*$$

→ Primitive Regular Expression :-

Language	Regular Expression.
ϕ	ϕ
$\{ \Lambda \}$	Λ
$\{ a \}$	a
$\{ a, b \}^*$	$(a+b)^*$

- Concatenation of two or more regular expression is a regular expression.

$$R_1 \cdot R_2 = R$$

eg:

$$R_1 = a^*, R_2 = (a+b)$$

$$R_1 \cdot R_2 = a^* \cdot (a+b)$$

- Union of two or more regular expression

$$R_1 + R_2 = R$$

eg:

$$R_1 = a^*, R_2 = b^*$$

$$R_1 + R_2 = R$$

$$a^* + b^*$$

- Closure of regular expression is a regular expression

$$R = (R)^*$$

eg:

$$R = (a+b)^*$$

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$$\Lambda^* = (a+b)^*$$

$$\rightarrow (a+b)^* = \{\Lambda, a, b, ab, ba, aab, \dots\}$$

$$\rightarrow a^* + b^* = \{\Lambda, a, b, aa, bb, aqa, bbb, \dots\}$$

$$\rightarrow (a+b)^* = (b+a)^*$$

$$\rightarrow (ab)^* \neq (ba)^*$$

$$\rightarrow (ab)^* = \{\Lambda, ab, abab, ababab, \dots\}$$

$$\rightarrow (ba)^* = \{\Lambda, ba, baba, \dots\}$$

- - The language L contains all strings with atleast two consecutive zeroes defined over $\Sigma = \{0, 1\}$.

$$L = \{00, 000, 001, 100, \dots\}$$

$$R.E = (0+1)^* 00 (0+1)^*$$

- - The language L contains all strings without two consecutive zeroes defined over $\Sigma = \{0, 1\}$.

$$R.E = (1+01)^* (0+1)$$

(19) .

$$R.E = (1^*011^*)^*(0+1) + 1^*(0+1)$$

* For one language there may exist more than one regular expressions but for each regular expression there exist a one language.

$$\bullet - R.E : L(1) = \{a^{2n}b^{2m}b : n, m \geq 0\}$$

$$L = \{b, aab, bbb, \dots\}$$

The language L of strings ending in b defined over $\Sigma = \{a, b\}$.

$$R.E = (aa)^*(bb)^*b$$

$$\bullet - a^{2n}b^{3m}c, n, m \geq 0$$

$$R.E = (aa)^*(bbb)^*c$$

rest

Q Is there any case when S^+ contains Λ ?

$$\text{Ans. If } S = \{\Lambda, a\}$$

$$S^+ = \{\Lambda, a, aa, aaa, \dots\}$$

Yes, if set contains alphabet ' Λ '

$$\bullet - (S^+)^* = (S^*)^*$$

$$\bullet - (S^+)^+ = S^+$$

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$$\circ - (S^*)^+ = (S^+)^*$$

Ex 3.1 :

$$\textcircled{1} L((a+b)^*b(a+ab)^*) < 4 \\ = \{b, ab a, abab, bba, bbab\}$$

$$\textcircled{2} ((0+1)(0+1)^*)^* 00(0+1)^*$$

Yes

$$\textcircled{4} \{a^n b^m : (n+m) \text{ is even}\}$$

R.E : $(aa)^*(bb)^* + (aa)^*a(bb)^*b$

$$\textcircled{5} (a) L_1 = \{a^n b^m : n \geq 4, m \leq 3\}$$

R.E : $aaaaa^* \cdot (1 + b + bb + bbb)$

$$(b) L_2 = \{a^n b^m : n < 4, m \leq 3\}$$

R.E : $(1 + a + aa + aaa) \cdot (1 + b + bb + bbb)$

→ (c) The complement of L_1

$$\text{R.E : } (1 + a + aa + aaa + aaaa) \cdot bbbb^* + (a+b)^*$$

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(9) $L = \{a^n b^m : n \geq 1, m \geq 1, nm \geq 3\}$

R.E: $a \cdot a^* \cdot bbb + aaa \cdot b \cdot b^*$

(12) $L = \{vwv : v, w \in \{a, b\}^*, |v| = 2\}$

$aa(a+b)^*aa + ab(a+b)^*ab + ba(a+b)^*ba +$
 $bb(a+b)^*bb$

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→ The language of string defined over $\Sigma = \{a, b\}$ having exactly 'aa'

$$b^* a a b^*$$

→ The language L of strings with 2 a's over $\Sigma = \{a, b\}$.

$$b^* a b^* a b^*$$

→ The language L of string atleast 2 a's over $\Sigma = \{a, b\}$

$$(a+b)^* aa (a+b)^* \\ (a+b)^* a (a+b)^* a (a+b)^*$$

→ The language L of strings with atleast one 'a' and one 'b'.

$$(a+b)^* a (a+b)^* b (a+b)^* + \\ (a+b)^* b (a+b)^* a (a+b)^*$$

→ The language L of strings with even length.

$$(a+b)^{2n} \\ ((a+b)(a+b))^n$$

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→ The language L of strings with odd length.

$$(a+b)((a+b)(a+b))^*$$

→ The language L of strings starting with 'a' and ending with 'b' or starting with 'b' and ending with 'a'.

$$a(a+b)^*b + b(a+b)^*a$$

→ The language of strings with words not ending with 'a'.

$$(a+b)^*b + \lambda$$

(or) $((a+b).b)^*$

→

- [abcd] means (a|b|c|d)
- [b-g] means [bcdefg]
- [b-gM-Qkr] means [bcdefg]

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→ RE for Tokenization.

Identifiers

letter $\rightarrow (a|b|c|\dots|z|A|B|C|\dots|Z)$

digit $\rightarrow (0|1|2|\dots|8|9)$

id $\rightarrow \text{letter} (\text{letter} | \text{digit})^*$

numbers

integer $\rightarrow (+|-|E)(0|1|2|\dots|9)\text{digit}^*$

decimal $\rightarrow \text{integer} . (\text{digit})^*$

real $\rightarrow (\text{integer} | \text{decimal}) E (+|-) \text{digit}^*$

complex $\rightarrow '(' \text{real} ', ' \text{real} ')'$

if

• $- [a-z][a-z0-9]^*$

• $- [0-9]^+$

• $- ([0-9]^+ " [0-9]^*) ([0-9]^* " [0-9]^+)$

• $- (" [a-z]^* "\n") (" [a-z]^* "\n" | " \t ")$

no token just
white spaces.

Chapter # 2

→ Deterministic Finite Automata
And Regular Languages.

Automation: An abstract machine which performs something automatically.

Deterministic: specific output

Automation: Rejects or accepts string.

DFA → combination of 5 tuples

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$$\text{DFA} = (Q, \Sigma, \delta, q_0, F)$$

Q = finite set of states (at least one state)

q_0 = initial state ($q_0 \in Q$)

F = set of final states ($F \subseteq Q$)

Σ = finite set of input alphabet

δ = transition function.

$$Q = \{q_0, q_1, \dots, q_n\}$$

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• To reject a string:
(OR) $q_{\text{last}} \in (Q - F)$
(OR) $q_{\text{last}} \in F$

• Transition Function:
 $\delta: Q \times \Sigma \rightarrow Q$ $(q \rightarrow q_0)$
 $\delta(q, x) = q'$

• Extended Transition Function:
 $\delta^*: Q \times \Sigma^* \rightarrow Q$
 $\delta^*(q, w) = q'$

• Inductive Definition:
Basis: $\delta^*(q, \epsilon) = q$
Induction: $\delta^*(q, w\delta) = \delta(\delta^*(q, w), \delta)$

eg: $\delta^*(q_0, bbb)$
 $= \delta(\delta^*(q_0, bb), b)$
 $= \delta(\delta(\delta^*(q_0, b), b), b)$
 $= \delta(\delta(\delta(\delta^*(q_0, \epsilon), b), b), b)$
 $= \delta(\delta(\delta(q_0, b), b), b)$
 $= \delta(\delta(q_1, b), b)$
 $= \delta(q_2, b)$
 $= b$

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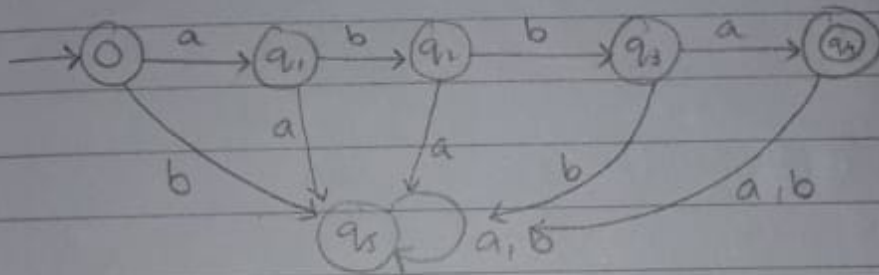
→ language of DFA:

All the strings that derive M to a final state is the language of DFA.

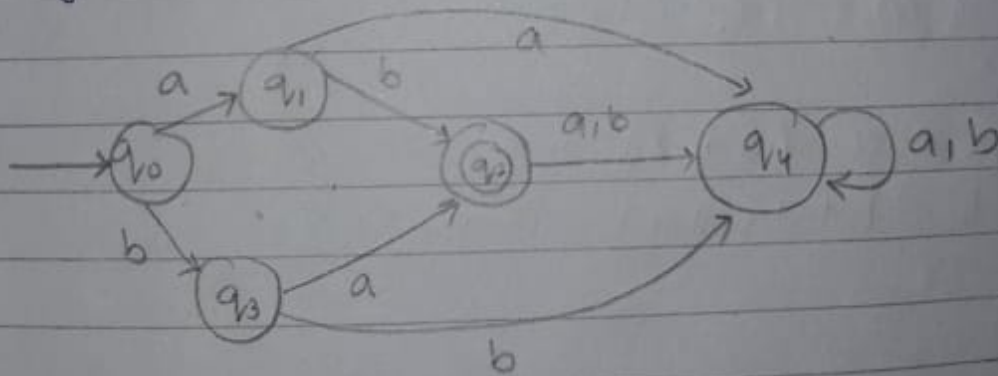
(OR)

All the strings accepted by the model is the language of the DFA.

eg: $L(M) = \{ \Lambda, abba \}$

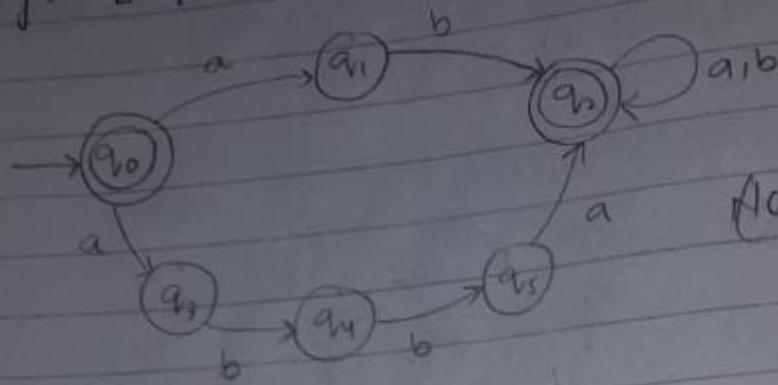


eg: $L(M) = \{ ab, ba \}$



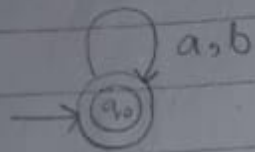
(30)

eg: $L = \{ \epsilon, ab, abba \}$

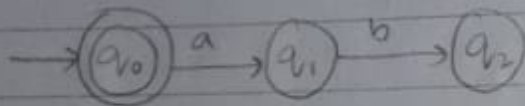


Not a DFA

eg: R.E: $(a+b)^*$

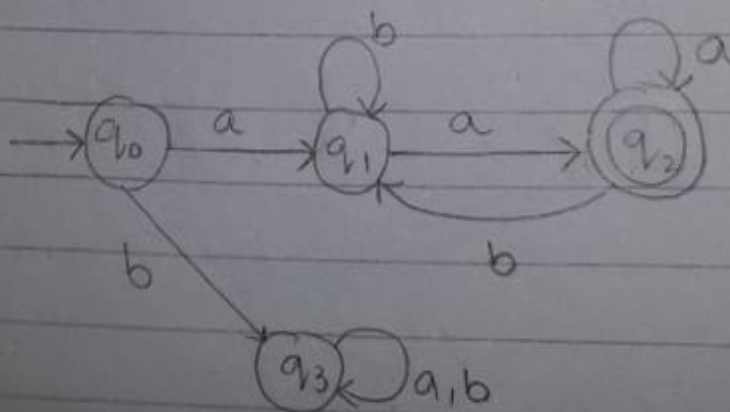


eg: Empty language



eg: $a \cdot (a+b)^* \cdot a$

$L = \{ aa, aaa, aba, aaba, \dots \}$

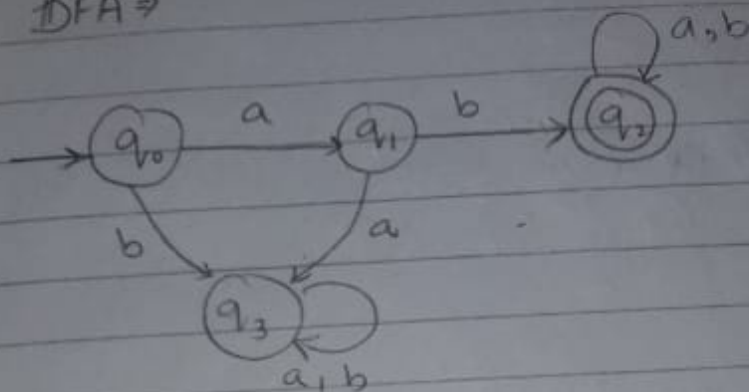


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* $L =$ all strings with prefix ab
 $L = \{ ab, aba, abb, abab, \dots \}$
R.E = $ab(a+b)^*$

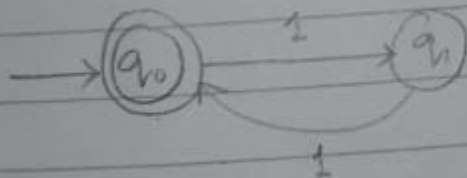
DFA \Rightarrow



NOTE: For every regular expression, there exist one or more DFA's. If there exist a DFA for a language then the language is Regular.

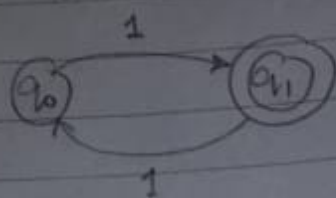
* $L = \{ x \in \text{even length of strings } x \in \Sigma^* \}$
 $\Sigma = \{ 1 \}$

$L = \{ \Lambda, 11, 1111, 111111, \dots \}$

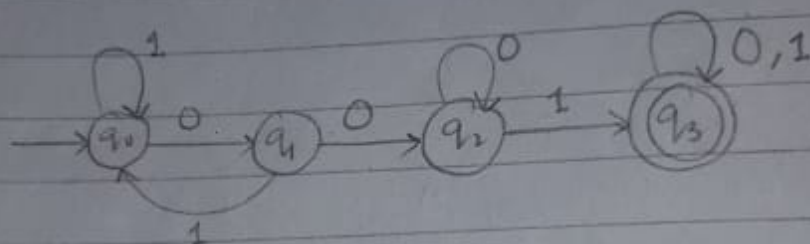


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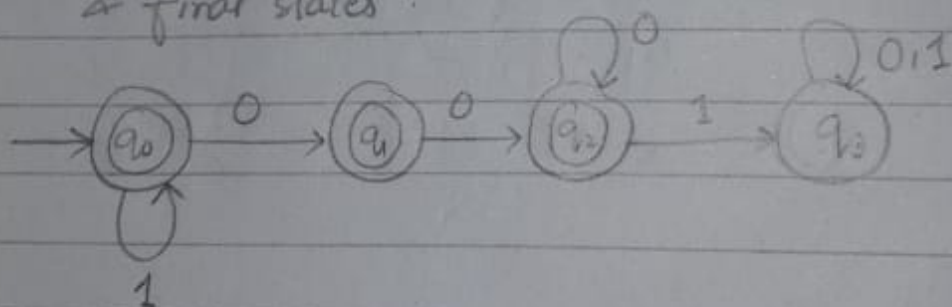
* $L = \{x \in \text{odd length strings}\}$
 $L = \{1, 111, 11111, \dots\}$



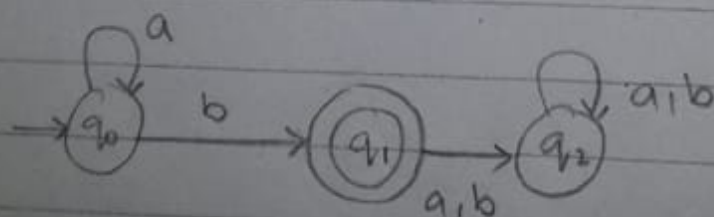
* $L = \{\text{all binary strings containing substring } 001\}$
 R.E: $(0+1)^* 001 (0+1)^*$



* $L = \{\text{all binary strings without substring } 001\}$
 Hint: Take complement and change initial & final states.

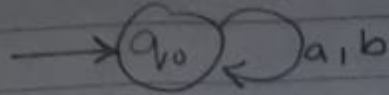


* $L = \{a^n b : n \geq 0\}$ R.E: $a^* b$

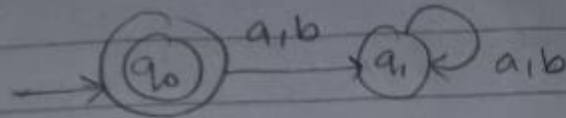


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* $L = \{ \} \Rightarrow$ Empty language

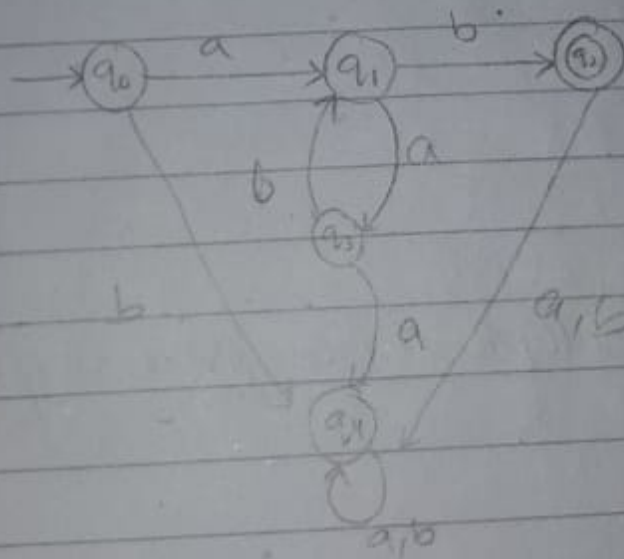


* $L(M) = \{ a \}$



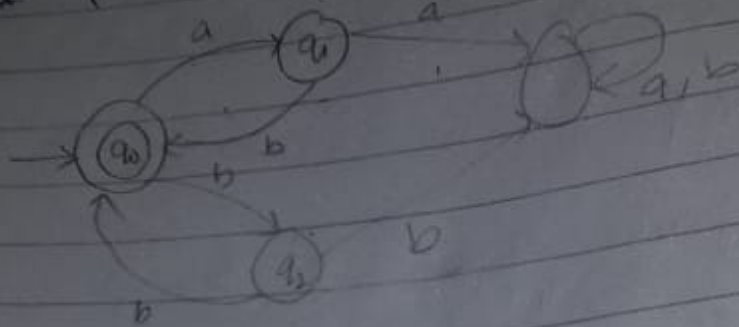
* $L = \{ a^n b^n : n \geq 0 \}$

* $a \cdot (ab)^* \cdot b$



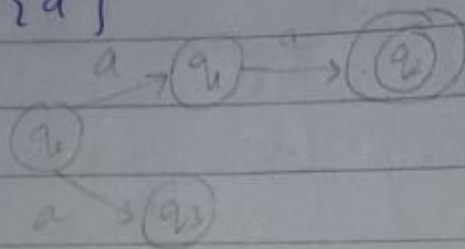
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* $(ab + bb)^*$



→ Non-Deterministic Finite Acceptor
Simpler to design (NFA).
difficult to program.

$\Sigma = \{a\}$



* May have multiple choice for a single input.

NFA accepts a string:

if whole string is consumed and automaton is at final state.

NFA rejects a string:

NFA definition:

$$M = (Q, \Sigma, \delta, q_0, F)$$

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→ Extended Transition Function = δ^*

1) Base clause : $\delta^*(q_0, \Lambda) = \{q\}$

2) Inductive clause : $\delta^*(q, ya)$
 $= \bigcup_{p \in \delta^*(q, y)} \delta(p, a)$

Example:

$$\delta^*(0, ab) = ?$$

Sol

$$\Rightarrow \bigcup_{p \in \delta^*(0, a)} \delta(p, b)$$

$$\Rightarrow \delta^*(0, a) = \bigcup_{p \in \delta^*(0, \Lambda)} \delta(p, a)$$

$$\Rightarrow \delta^*(0, \Lambda) = \{0\}$$

$$\Rightarrow \delta(\{0\}, a) = \{0, 1, 3\}$$

$$\Rightarrow \delta(\{0, 1, 3\}, b) = \delta(0, b) \cup \delta(1, b) \cup \delta(3, b)$$

$$= \{2\} \cup \{3\} \cup \{1\}$$

$$= \{1, 2, 3\}$$

$$\Rightarrow \delta^*(0, ab) = \{1, 2, 3\}$$

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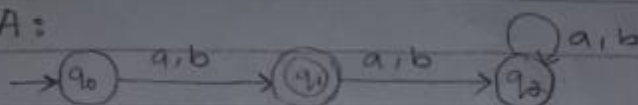
Every DFA is also NFA

(37) Every NFA is also a NFA- Λ

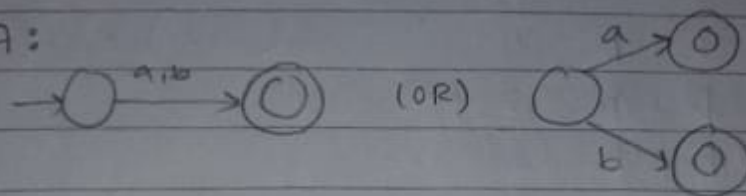
→ NFA with Null Transition:-

$L = \{a, b\}$, $\Sigma = \{a, b\}$, R.E = $a + b$

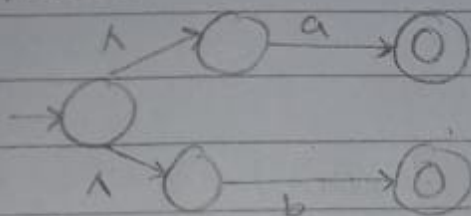
DFA:



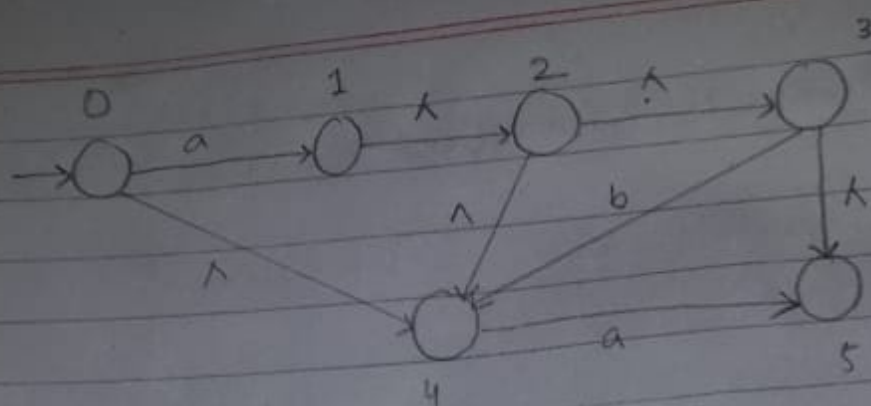
NFA:



NFA NULL:



If a language can be accepted by DFA, then it ^{is} ~~can~~ also be accepted by NFA & NFA- Λ .



states	a	b	λ
0	1	∅	4
1	∅	∅	2
2	∅	∅	3, 4
3	∅	4	5
4	5	∅	∅
5	∅	∅	∅

$$\delta(0, \lambda) = \{4\}$$

→ Definition of λ -closure:

" λ closure of set S of states of Φ by $\lambda(S)$ "
 (OR) $\lambda(S)$ is defined as - the number of states that can be reached by reading λ arc, including S itself.

$$\lambda(0) = \{0, 4\}$$

$$\lambda\{1\} = \{1, 2, 3, 4, 5\}$$

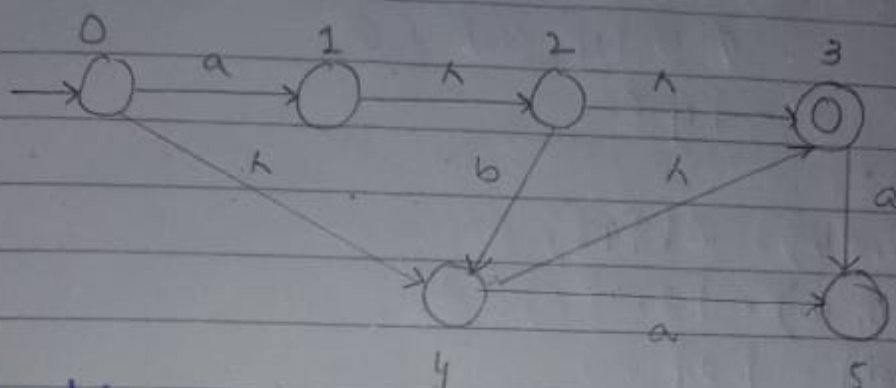
$$\lambda\{2\} = \{2, 3, 4, 5\}$$

$$\lambda\{3\} = \{3, 5\}$$

(39)

→ Extended transition function:
definition of δ^* :

- Base clause: $\delta^*(q, \epsilon) = \{q\}$.
- Inductive clause: $\delta^*(q, ya) = \bigcup_{p \in \delta^*(q, y)} \delta(p, a)$



Example:

Sol. $\delta^*(0, ab) = ?$

$$\delta^*(0, ab) = \bigcup_{p \in \delta^*(0, a)} \delta(p, b) \rightarrow (1)$$

$$\delta^*(0, a) = \bigcup_{p \in \delta^*(0, \epsilon)} \delta(p, a) \rightarrow (2)$$

$$\delta^*(0, \epsilon) = \{0\} = \{0, 3, 4\}$$

Putting this in eq(1)

$$\begin{aligned} \delta(\{0, 3, 4\}, a) &= \delta(0, a) \cup \delta(3, a) \cup \delta(4, a) \\ &= \{1\} \cup \{5\} \cup \{5\} \\ &= \{1, 5\} \end{aligned}$$

Putting this in eq(2)

$$\delta^*(0, a) = \{1, 5\}$$

(40)

$$\begin{aligned} &= \Lambda \{1\} \cup \Lambda \{5\} \\ &= \{1, 2, 3\} \cup \{5\} \\ \delta^*(0, a) &= \{1, 2, 3, 5\} \end{aligned}$$

Putting this in eq(1)

$$\begin{aligned} \delta(\{1, 2, 3, 5\}, b) &= \delta(1, b) \cup \delta(2, b) \cup \delta(3, b) \cup \delta(5, b) \\ &= \emptyset \cup \{4\} \cup \emptyset \cup \emptyset \\ &= \{4\} \end{aligned}$$

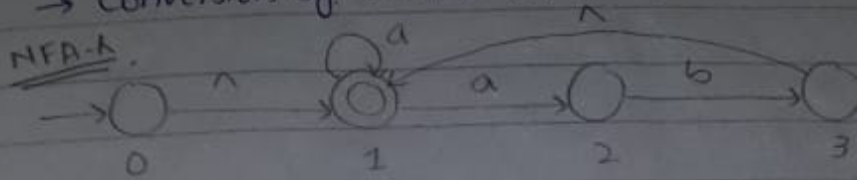
$$\begin{aligned} \delta^*(0, ab) &= \Lambda(\{4\}) \\ \delta^*(0, ab) &= \{3, 4\} \cap \{3\} \\ \delta^*(0, ab) &= \{3\} \end{aligned}$$

$$L = \{\Lambda, a, ab\}$$

$$R.E = \Lambda + a + ab$$

(41)

→ Conversion of NFA- Λ to NFA:



① State (q)	② Input (x)	③ $\Lambda(\{q\})$	④ null-closure of q $\bigcup_{p \in \Lambda(\{q\})} \delta(p, x)$
0	a	$\{0, 1\}$	$\delta(0, a) \cup \delta(1, a)$ $= \emptyset \cup \{1, 2\} = \{1, 2\}$
0	b	$\{0, 1\}$	\emptyset
1	a	$\{1\}$	$\{1, 2\}$
1	b	$\{1\}$	\emptyset
2	a	$\{2\}$	\emptyset
2	b	$\{2\}$	$\{3\}$
3	a	$\{1, 3\}$	$\{1, 2\}$
3	b	$\{1, 3\}$	\emptyset

$$\textcircled{3} \delta_2(q, a) = \Lambda\left(\bigcup_{p \in \Lambda(\{q\})} \delta(p, a)\right)$$

$$\{1, 2\}$$

$$\emptyset$$

$$\{1, 2\}$$

$$\emptyset$$

$$\emptyset$$

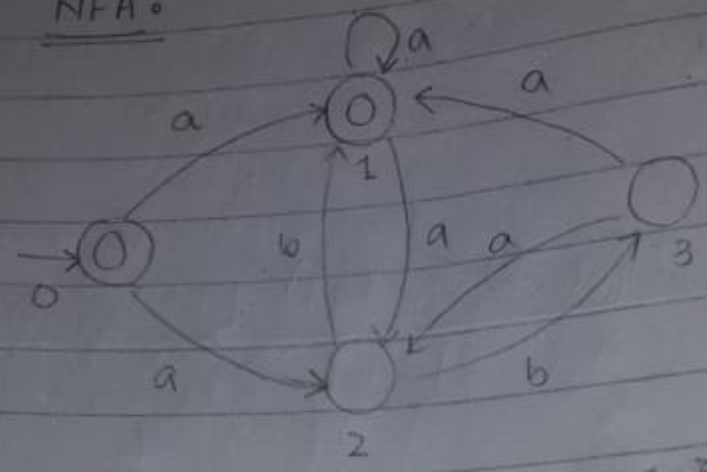
$$\{1, 3\}$$

$$\{1, 2\}$$

$$\emptyset$$

(42)

NFA :



$$A_1 = \{1\} \quad \{0,1\} \cap \{1\} = \{1\}$$

if $(\{0\} \cap A_1 \neq \emptyset)$ then

$$A_2 = A_1 \cup \{0\} \rightarrow A_2 = \{0,1\}$$

else

$$A_2 = A_1$$

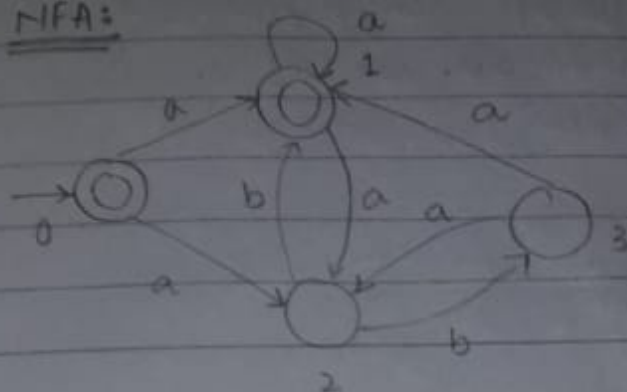
$$L = \{\epsilon, a, ab, aab, aaba, \dots\}$$

$$R.E = a^* (ab)^* a^*$$

(43)

→ Conversion from NFA to DFA :-

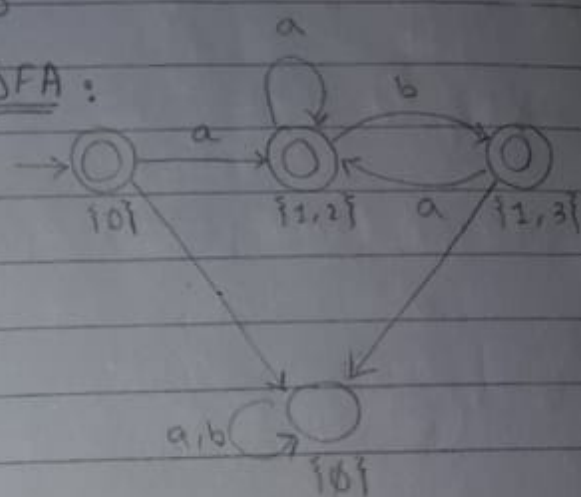
NFA:



$L = \{ \Lambda, a, ab, aab, \dots \}$
 $R.E = a^*(ab)^*a^*$

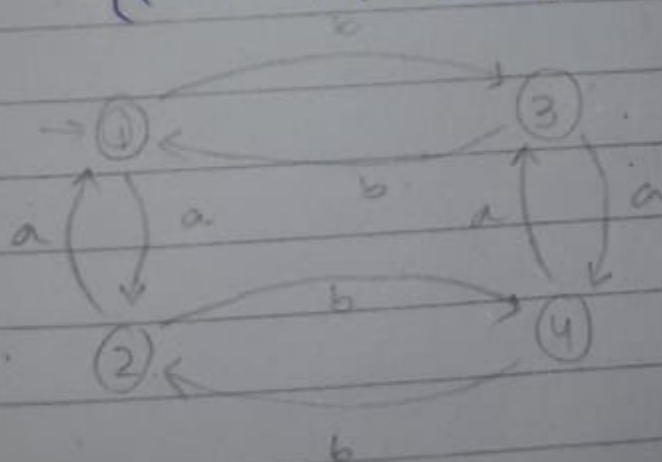
DFA:

State	a	b
$\{0\}$	$\{1,2\}$	\emptyset
$\{1,2\}$	$\{1,2\}$	$\{1,3\}$
$\{1,3\}$	$\{1,2\}$	\emptyset
$\{\emptyset\}$	\emptyset	\emptyset



→ Even-Even example

$$((aa+bb)(ab+ba))^*$$

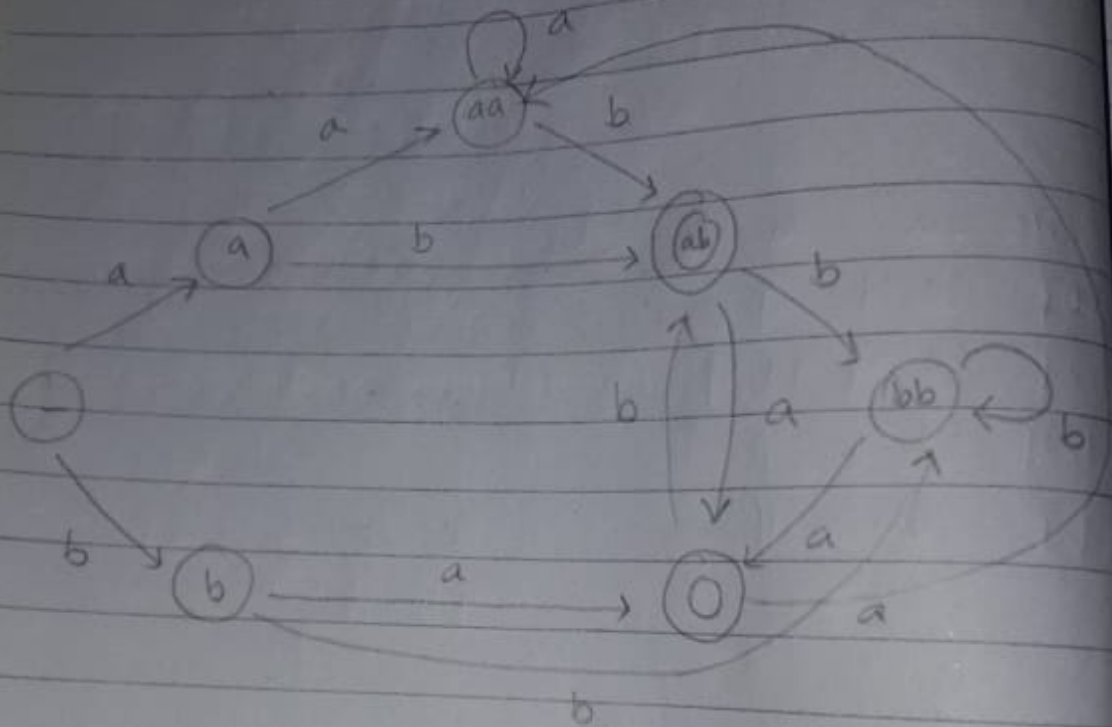


19/Febl/19

(44)

→ John Mallin

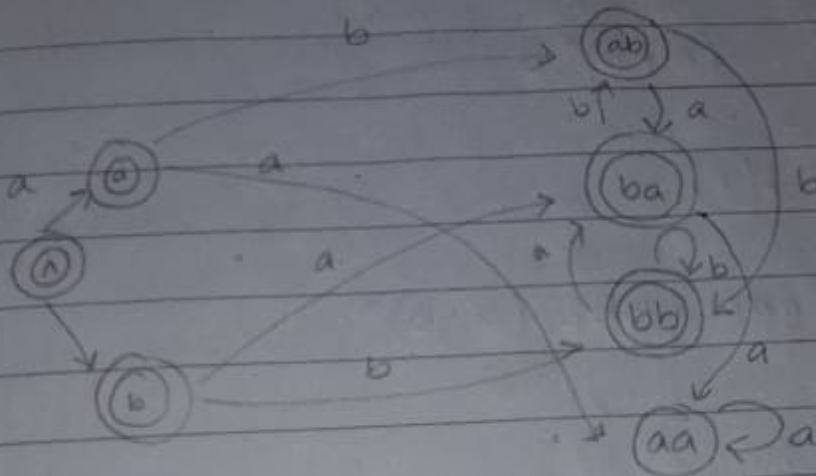
→ $L = \{w \text{ belongs to } \{a,b\}^* : \text{length}(w) \geq 2 \text{ \& } w \text{ neither ends in } aa \text{ nor } bb\}$
 $= (a+b)^+(ab+ba)$.



(45)

→ L = {w belongs to $\{a,b\}^*$, w does not end in aa}

R.E = $\Lambda + a + b + (a+b)^+ (ab+ba+bb)$

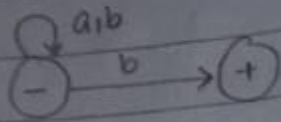


(46)

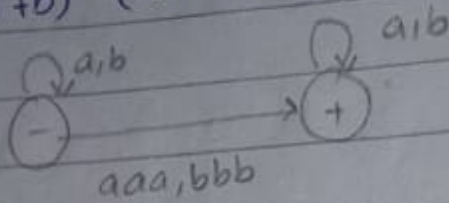
→ Transition Graph:
→ To read substrings.

Every FA is also TG but not every TG is FA.

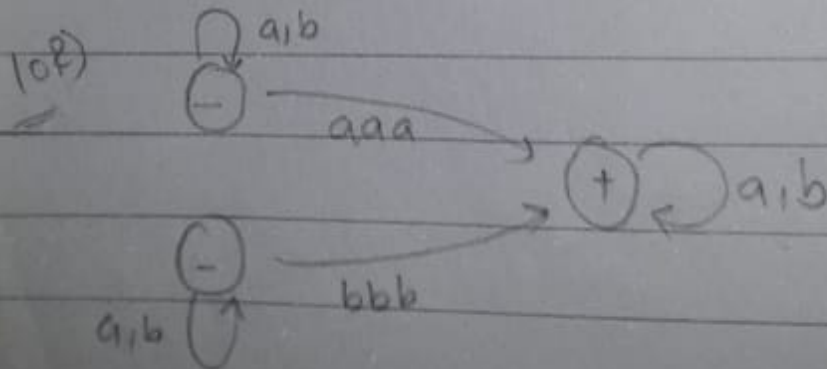
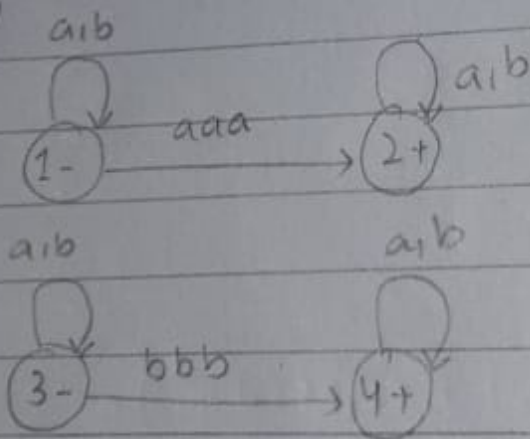
eg: RE: $(a+b)^*b$



eg $(a+b)^*(aaa+bbb)(a+b)^*$



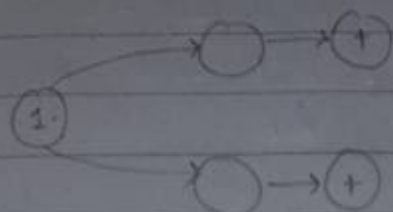
(OR)



(47)

eg $a(a+b)^*b + b(a+b)^*a$

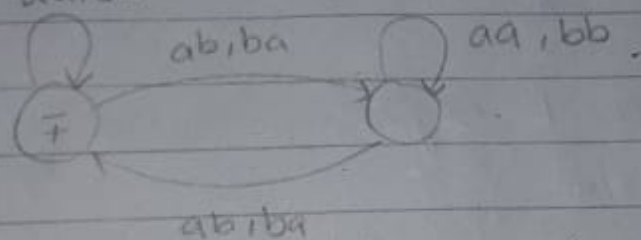
Language L beginning & ending over different alphabet



eg: Language L of Even-Even.

$(aa+bb + (ab+ba)(aa+bb)^*(ab+ba))^*$

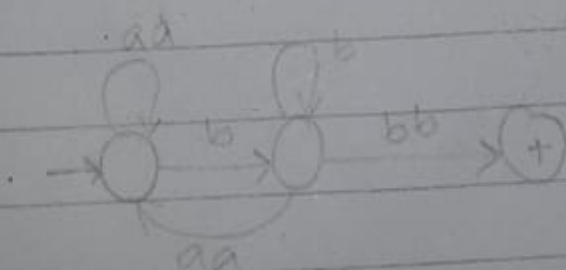
aa, bb



eg: Language L defined over $\{a, b\}$ in which 'a' occurs in even combination and ends with three or more b's.

$(aa)^*b(b^* + (aa(aa)^*b)^*)bb$

(OR) $(aa)^*b(b^* + ((aa)+b)^*)bb$



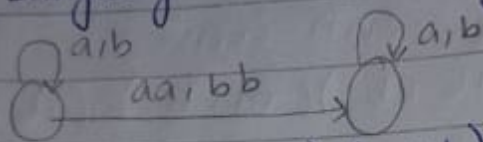
Thursday
21/Feb/19

(48)

→ Generalized Transition Graph:

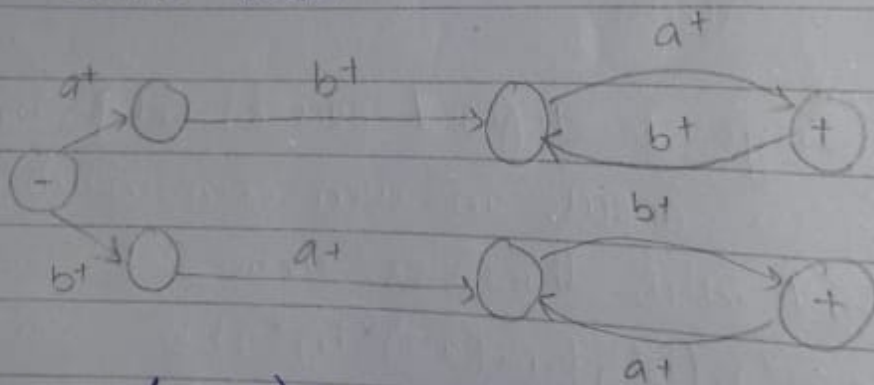
- ① Finite no. of sets.
- ② Finite set of input letters (Σ) from which input string formed.
- ③ Directed edges connected some pair of states labeled by R.E.

eg Language L containing aa or bb .



R.E: $(a+b)^* (aa+bb) (a+b)^*$

eg# Language L beginning and ending with same letter.



R.E: $a(a+b)^* a + b(a+b)^* b$

(49)

→ Kleene's Theorem: =.

If a language is expressed by FA, TG, RE then it can also be expressed by other two as well.

Part 1: If accepted by FA, then it can be accepted by TG.

Part 2: If accepted by TG, then it can be accepted by RE.

Part 3: If accepted by RE, then it can be accepted by FA.

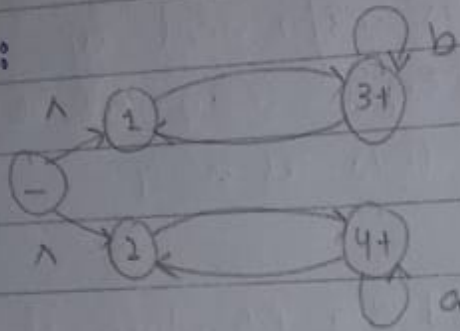
→ Part 1: Every FA is also a TG.
(conversion not required).

→ Part 2: Given TG, extract FA.

(50)

Obtaining RE from TG.

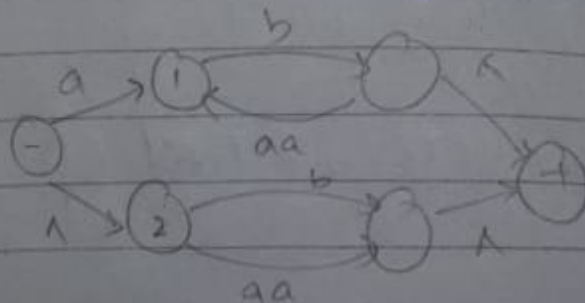
Step 1:



- Required if multiple initial states are there, then make new initial state connected new state by old by connecting through null.

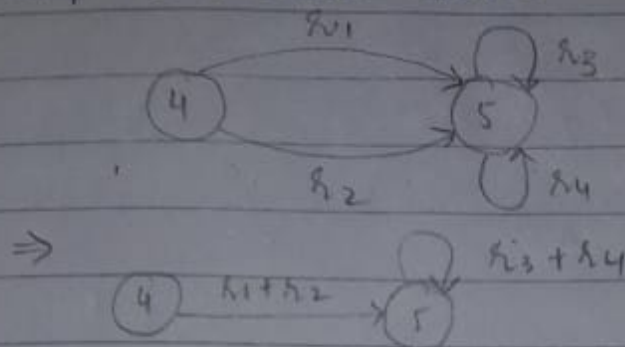
Step 2:

More than 1 final state, then introduce a new final state by joining new state with old by null transition.

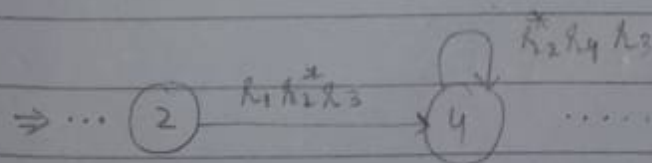
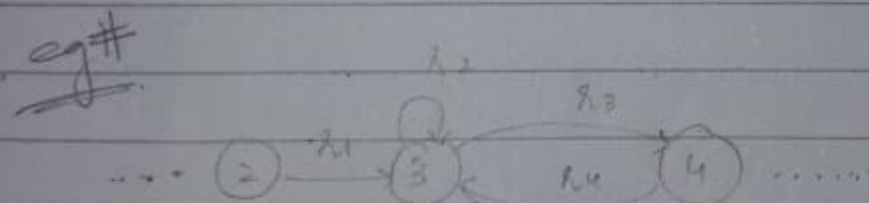
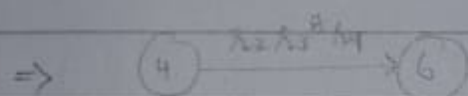
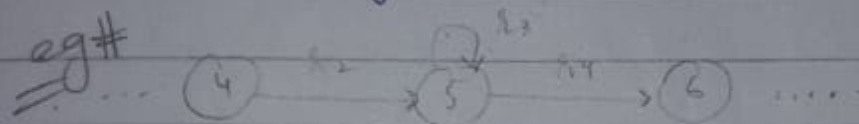


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Step 3: Reduce states

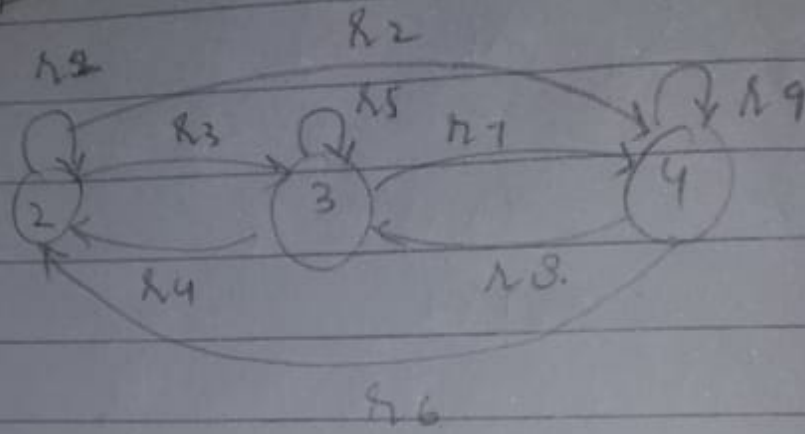


Step 4: By Pass and state elimination

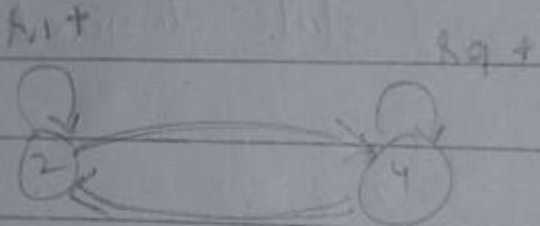


(52)

eg#



=>



$R_1 + (R_3$