

Domain Relational Calculus

Find the names of pizzas that come in a 10 inch size

$$\{ \langle N \rangle \mid \exists C \exists S (\text{pizza}(C, N, S) \wedge S = 10) \}$$

Find the names of pizzas that come in a 10 inch or a 12 inch size

$$\{ \langle N \rangle \mid \exists C \exists S (\text{pizza}(C, N, S) \wedge (S = 10 \vee S = 12)) \}$$

Find the names of pizzas that come in both a 10 inch and a 12 inch size

$$\{ \langle N1 \rangle \mid \exists C1 \exists S1 \exists C2 \exists N2 \exists S2 \\ (\text{pizza}(C1, N1, S1) \wedge \text{pizza}(C2, N2, S2) \wedge N1 = N2 \wedge S1 = 10 \wedge S2 = 12) \}$$

Find the pairs of different codes of pizzas with the same name and the same size (is there any?)

$$\{ \langle C1, C2 \rangle \mid \exists N1 \exists S1 \exists N2 \exists S2 \\ (\text{pizza}(C1, N1, S1) \wedge \text{pizza}(N2, C2, S2) \wedge C1 \neq C2 \wedge N1 = N2 \wedge S1 = S2) \}$$

Find the names and phone numbers of the stores in "College Park" or "Greenbelt" that sell a 10 inch pizza named "pepperoni" for less than \$8

$$\{ \langle SN, P \rangle \mid \exists C \exists N \exists S \exists A \exists Pr \\ (\text{pizza}(C, N, S) \wedge \text{store}(SN, A, P) \wedge \text{sells}(SN, C, Pr) \wedge (A = \text{« College Park »} \vee A = \text{« Greenbelt »}) \\ \wedge N = \text{“pepperoni”} \wedge S = 10 \wedge Pr < 8) \}$$

Find the codes of the most expensive pizzas – assume the scheme of the database is reduced to a relation pizza(code, price) to simplify –

$$\{ \langle C1 \rangle \mid \exists N1 \exists S1 \forall C2 \forall N2 \forall S2 \\ (\text{pizza}(C1, N1, S1) \wedge (\text{pizza}(C2, N2, S2) \Rightarrow P1 \geq P2)) \}$$

Find the names of the stores that sell all the pizzas

$$\{ \langle SN \rangle \mid \exists A \exists P \forall C \forall N \forall S \exists Pr \\ (\text{store}(SN, A, P) \wedge (\text{pizza}(C, N, S) \Rightarrow \text{sells}(SN, C, Pr))) \}$$