

In the Lecture Series Introduction to Database Systems

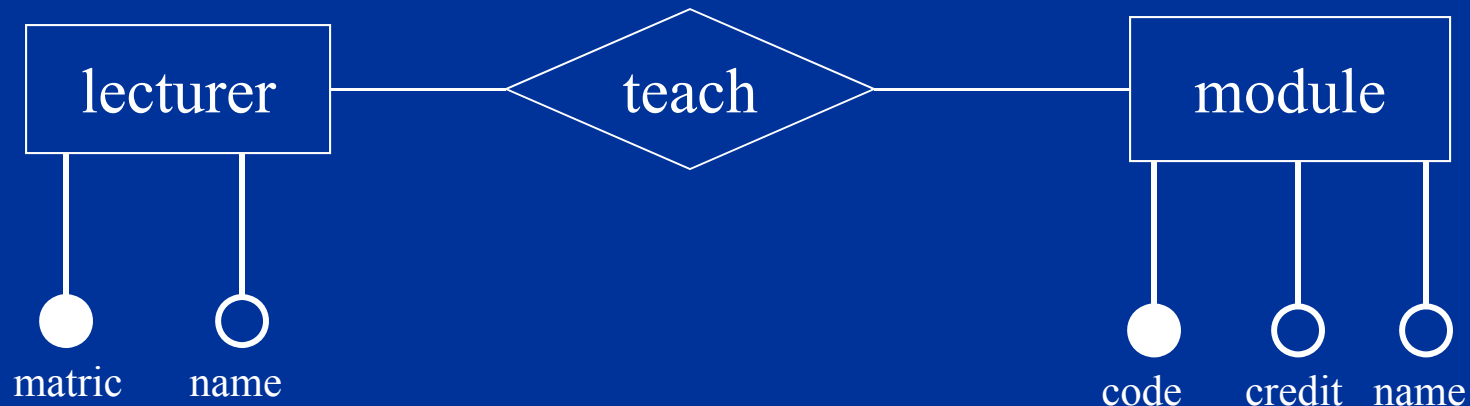
# Tuple Relational Calculus

*Presented by Stéphane Bressan*

*Introduction to Database Systems*

# Example

- lecturer(matric, name)
- module(code, name, credit),
- teach(matric, code)



## Example

- $\{T \mid T \in \text{lecturer}\}$
- $\{T \mid \exists T1 (T1 \in \text{lecturer} \wedge T = T1)\}$
- $\{T \mid \exists T1 (T1 \in \text{lecturer} \wedge T.\text{matric} = T1.\text{matric} \wedge T.\text{name} = T1.\text{name})\}$

by CONVENTION!

# Syntax of Tuple Relational Calculus

- $\{T \mid \text{formula}\}$
- Variables are tuples
- $T \in \text{rel}$ :  $T$  is a tuple in relation  $\text{rel}$
- $T.a$ : The value of attribute  $a$  in  $T$ .
- $T1 = T2$ :  $T1$  and  $T2$  must have the same attributes with same values.
- Parenthesis can be omitted if non ambiguous (not advised)
  - $\{T \mid \exists T1 (T1 \in \text{lecturer} \wedge T.\text{name} = T1.\text{name})\}$
  - $\{T \mid \exists T1 T1 \in \text{lecturer} \wedge T.\text{name} = T1.\text{name}\}$

## Example

- $\{T \mid \exists T1 \ T1 \in \text{lecturer}$   
     $\wedge T1.\text{name} = \text{"Smith"}$   
     $\wedge T.\text{matric} = T1.\text{matric}\}$

## Example

- $\{T \mid \exists T1 \exists T2 \exists T3$   
     $T1 \in \text{lecturer}$   
     $\wedge T2 \in \text{module}$   
     $\wedge T3 \in \text{teach}$   
     $\wedge T1.\text{matric} = T3.\text{matric}$   
     $\wedge T2.\text{code} = T3.\text{code}$   
     $\wedge T2.\text{credit} < 2$   
     $\wedge T.\text{lec\_name} = T1.\text{name}$   
     $\wedge T.\text{mod\_name} = T2.\text{name}\}$

## Example

SELECT

T1.name as lec\_name,

T2.name as mod\_name

FROM lecturer T1, module T2, teach t3

WHERE T1.matric = T3.matric

AND T2.code = T3.code

AND T2.credit < 2

## Example

Find the names of the lecturers teaching all modules:

$$\{T \mid \exists T1 \forall T2 \exists T3$$
$$T1 \in \text{lecturer}$$
$$\wedge (T2 \in \text{module} \Rightarrow ($$
$$T3 \in \text{teach}$$
$$\wedge T1.\text{matric} = T3.\text{matric}$$
$$\wedge T2.\text{code} = T3.\text{code}))$$
$$\wedge T.\text{name} = T1.\text{name}\}$$



## Example

Find the names of the lecturers T1 such that, for any module T2, the lecturer teaches the module (as recorded in T3).

$$\{T \mid \exists T1 \forall T2 \exists T3$$
$$T1 \in \text{lecturer}$$
$$\wedge (T2 \in \text{module} \Rightarrow ($$
$$T3 \in \text{teach}$$
$$\wedge T1.\text{matric} = T3.\text{matric}$$
$$\wedge T2.\text{code} = T3.\text{code}))$$
$$\wedge T.\text{name} = T1.\text{name}\}$$

## Example

- $\{T \mid \exists T1($   
     $T1 \in \text{lecturer}$   
     $\wedge \quad \forall T2$   
         $(T2 \in \text{module} \Rightarrow$   
             $(\exists T3 (T3 \in \text{teach}$   
             $\wedge T1.\text{matric} = T3.\text{matric}$   
             $\wedge T2.\text{code} = T3.\text{code})))$   
     $\wedge T.\text{name} = T1.\text{name})\}$

## Example

$$\exists T1 \forall T2 \exists T3$$

We are looking for tuples T such that the formula below is true for SOME tuple T1, ALL tuples T2, and SOME tuple T3 and :

$$\begin{aligned} & T1 \in \text{lecturer} \\ & \wedge (T2 \in \text{module} \Rightarrow ( \\ & \quad T3 \in \text{teach} \wedge T1.\text{matric} = T3.\text{matric} \\ & \quad \wedge T2.\text{code} = T3.\text{code})) \\ & \wedge T.\text{name} = T1.\text{name} \end{aligned}$$

## Example

If  $T1 \in \text{lecturer}$  and  $T2 \notin \text{module}$ ,  
the formula is true!!!!

$T1 \in \text{lecturer}$

$\wedge (T2 \in \text{module} \Rightarrow ($

$T3 \in \text{teach} \wedge T1.\text{matric} = T3.\text{matric}$   
 $\wedge T2.\text{code} = T3.\text{code}))$

$\wedge T.\text{name} = T1.\text{name}$

## Example

If  $T1 \in \text{lecturer}$  and  $T2 \in \text{module}$ , then the formula is true if there is a  $T3 \in \text{teach}$  which shares the same matric number with  $T1$  and module code with  $T2$ .

Namely, if the lecturer teaches the module.

$$\begin{aligned} & T1 \in \text{lecturer} \\ & \wedge (T2 \in \text{module} \Rightarrow ( \\ & \quad T3 \in \text{teach} \wedge T1.\text{matric} = T3.\text{matric} \\ & \quad \wedge T2.\text{code} = T3.\text{code})) \\ & \wedge T.\text{name} = T1.\text{name} \end{aligned}$$

## Example

The formula is false only if

$T1 \notin \text{lecturer}$  or if  $T2$  is a module, but there is no  $T3$  which shares the same matric number with  $T1$  and module code with  $T2$

$$\begin{aligned} & T1 \in \text{lecturer} \\ & \wedge (T2 \in \text{module} \Rightarrow ( \\ & \quad T3 \in \text{teach} \wedge T1.\text{matric} = T3.\text{matric} \\ & \quad \wedge T2.\text{code} = T3.\text{code})) \\ & \wedge T.\text{name} = T1.\text{name} \end{aligned}$$

## Example to SQL

$$\{T \mid \exists T1 \forall T2 \exists T3$$
$$\quad (T1 \in \text{lecturer}$$
$$\quad \wedge (T2 \in \text{module} \Rightarrow ($$
$$\quad \quad T3 \in \text{teach}$$
$$\quad \quad \wedge T1.\text{matric} = T3.\text{matric}$$
$$\quad \quad \wedge T2.\text{code} = T3.\text{code}))$$
$$\quad \wedge T.\text{name} = T1.\text{name})\}$$

## Example to SQL

$$\{T \mid \exists T1 \forall T2$$
$$\quad (T1 \in \text{lecturer}$$
$$\quad \wedge (T2 \in \text{module} \Rightarrow (\exists T3$$
$$\quad \quad (T3 \in \text{teach}$$
$$\quad \quad \wedge T1.\text{matric} = T3.\text{matric}$$
$$\quad \quad \wedge T2.\text{code} = T3.\text{code})))$$
$$\quad \wedge T.\text{name} = T1.\text{name})\}$$



## Example to SQL

$$\{T \mid \exists T1 \forall T2$$
$$\quad (T1 \in \text{lecturer}$$
$$\quad \wedge ( \neg(T2 \in \text{module}) \vee (\exists T3$$
$$\quad \quad (T3 \in \text{teach}$$
$$\quad \quad \wedge T1.\text{matric} = T3.\text{matric}$$
$$\quad \quad \wedge T2.\text{code} = T3.\text{code})))$$
$$\quad \wedge T.\text{name} = T1.\text{name})\}$$

$A \Rightarrow B$  is the same as  $\neg A \vee B$

## Example to SQL

$$\{T \mid \exists T1 \forall T2$$
$$\quad (T1 \in \text{lecturer}$$
$$\quad \wedge \neg \neg (\neg (T2 \in \text{module}) \vee (\exists T3$$
$$\quad \quad (T3 \in \text{teach}$$
$$\quad \quad \wedge T1.\text{matric} = T3.\text{matric}$$
$$\quad \quad \wedge T2.\text{code} = T3.\text{code})))$$
$$\quad \wedge T.\text{name} = T1.\text{name})\}$$

Double Negation:

A is the same as  $\neg \neg A$

## Example to SQL

$$\{T \mid \exists T1 \forall T2$$
$$\quad (T1 \in \text{lecturer}$$
$$\quad \wedge \neg (T2 \in \text{module} \wedge \neg (\exists T3$$
$$\quad \quad (T3 \in \text{teach}$$
$$\quad \quad \wedge T1.\text{matric} = T3.\text{matric}$$
$$\quad \quad \wedge T2.\text{code} = T3.\text{code})))$$
$$\quad \wedge T.\text{name} = T1.\text{name})\}$$

De Morgan:

$\neg \neg (\neg A \vee B)$  is the same as  $\neg (A \wedge \neg B)$

## Example to SQL

$\{T \mid \exists T1$

$(T1 \in \text{lecturer}$

$\wedge \neg (\exists T3 (T2 \in \text{module} \wedge \neg (\exists T3$

$(T3 \in \text{teach}$

$\wedge T1.\text{matric} = T3.\text{matric}$

$\wedge T2.\text{code} = T3.\text{code}))))$

$\wedge T.\text{name} = T1.\text{name})\}$

De Morgan (for quantifiers):

$\forall X (\neg A)$  is the same as  $\neg (\exists X (A))$

## Example to SQL

$$\{T \mid \exists T1$$
$$\quad (T1 \in \text{lecturer}$$
$$\quad \wedge \neg (\exists T2 (T2 \in \text{module} \wedge \neg (\exists T3$$
$$\quad \quad (T3 \in \text{teach}$$
$$\quad \quad \wedge T1.\text{matric} = T3.\text{matric}$$
$$\quad \quad \wedge T2.\text{code} = T3.\text{code})))$$
$$\wedge T.\text{name} = T1.\text{name})\}$$

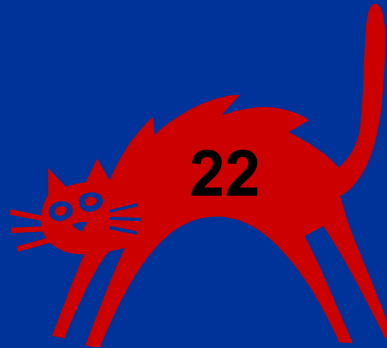
## Example to SQL

```
SELECT T1.name  
FROM lecturer T1  
WHERE NOT EXISTS (  
    SELECT *  
    FROM module T2  
    WHERE NOT EXISTS (  
        SELECT * FROM teach T3  
        WHERE T1.matric = T3.matric  
        AND T2.code = T3.code))
```

# Safety of Queries in T-uple Relational Calculus

$\{T \mid T \notin \text{lecturer}\}$

(“mycat”, 22, “red”) is not a lecturer, any tuple in the world maybe an answer if it is not already in the lecturer relation.



## Safety of Queries in T-uple Relational Calculus

A query is **safe** if the set of t-uples in the answer is a subset of the set of t-uples that can be constructed from the constants explicitly referenced directly (they appear in the query) or indirectly (they appear in a relation mentioned in the query) in the query.

We consider only safe queries



## Credits

The content of this lecture is based  
on chapter 3 of the book  
“Introduction to database  
Systems”

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