







Functional Dependencies

For a relation scheme R, a functional dependency from a set S of attribute of R to a set T of attribute of R exists if and only if:

For every instance of |R| of R, if two t-uples in |R| agree on the values of the attributes in S, then they agree on the values of the attributes in T.

We write: S → T

Functional Dependencies

company(eNumber, firstName, lastName, address, department, position, salary)

{position} → {salary}

If two t-uples in the relation company have the same value for the attribute position then they must have the same value for the salary attribute.

Functional Dependencies

employee(eNumber, firstName, lastName, address, department, position)

{firstName, lastName} → {eNumber, address, department, position}

If two t-uples in the relation employee relation have the same first name and last name then they must the same t-uple (no duplicate)

One to one function. Strong relationship bt or pri leap & functional depending

Functional Dependencies

company(enumber, firstname, lastname, address, department, position, salary)

 $\{position\} \rightarrow \{salary\}$

 \forall X1 \forall X2 \forall X3 \forall X4 \forall X5 \forall X6 \forall X7 \forall X8 \forall X9 \forall X10 \forall P \forall S1 \forall S2 ((company(X1, X2, X3, X4, X5, P, S1)

Lyinterno of DRC

Functional Dependencies

company(enumber, firstname, lastname, address, department, position, salary)

 $\{position\} \rightarrow \{salary\}$

CHECK (NOT EXISTS (

SELECT *

FROM company c1, company c2

WHERE c1.position=c2.position AND c1.salary <> c2.salary))

Functional Dependencies

salary(position, salary)

 $\{position\} \rightarrow \{salary\}$

CHECK (NOT EXISTS (

SELECT *

FROM salary s1, salary s2

WHERE s1.position=s2.position AND s1.salary <> s2.salary))

PRIMARY KEY (position)

I can just simply do this

Trivial FDs 1/

 $X \rightarrow Y$

YCX -> PROPER subject

{firstName, address} → {firstName}

Non-Trivial FDs

 $X \rightarrow Y$

Y ⊄ X → Not or proper subset

{eNumber} → {address}

 $\{firstName, lastName\} \rightarrow \{firstName, \}$ address)

Completely Non-Trivial FDs $X \to Y$ $Y \cap X = \emptyset \quad \text{\downarrow} \quad \text{\downarrow}$ $\{ \text{firstName, lastName} \} \to \{ \text{address} \}$

Superkeys

A set of attributes whose knowledge

determines the value of the entire t-uple is a superkey

employee(eNumber, firstName, lastName, address, department, position, salary)

{firstName, lastName} > contidute (ce)
{eNumber} > contidute (ce)
{firsName, lastName, address} > Not. (a) contin first > ce is is continued and continued

Candidate Keys

A minimal (for inclusion) set of attributes whose knowledge determines the value of the entire t-uple is a **candidate key**employee(eNumber, firstName, lastName, address, department, position, salary)

{firstName, lastName}
{eNumber}

The designer chooses one candidate key to be the primary key

It is sometimes possible to infer new functional dependencies from a set of given functional dependencies

Reasoning about Functional Dependencies

(independently from any particular instance of the relation scheme or of any additional knowledge)

Introduction to Database Systems

Reasoning about Functional Dependencies

For example:
From
{eNumber} → {firstName}
and
{eNumber} →{lastName}

We can infer
{eNumber} → {firstName, lastName}

3

Armstrong's Axioms

- Be X, Y, Z be subsets of the relation scheme of a relation R
- Reflexivity: -> Every trivial fun dependeny: the If $Y \subset X$, then $X \rightarrow Y$
- Augmentation:

If $X \rightarrow Y$, then $X \cup Z \rightarrow Y \cup Z$

Transitivity:

If $X \rightarrow Y$ and $Y \rightarrow Z$, then $X \rightarrow Z$

by acting or annon they

both sides

Armstrong's Axioms

employee(eNumber, firstName, lastName, address, department, position, salary)

Reflexivity:

If {firstName} ⊂ {firstName, lastName}, Then {firstName, lastName} → {firstName}

Armstrong's Axioms

employee(eNumber, firstName, lastName, address, department, position, salary)

Augmentation:

If $\{position\} \rightarrow \{salary\},\$ then {position, eNumber} \rightarrow {salary, eNumber}

Armstrong's Axioms

employee(eNumber, firstName, lastName, address, department, position, salary)

Transitivity:

If {eNumber} → {position} and $\{position\} \rightarrow \{salary\},\$ Then $\{eNumber\} \rightarrow \{salary\}$

Armstrong's Axioms

Armstrong's axioms are sound

For example: Transitivity Let X, Y, Z be subsets of the relation R If $X \rightarrow Y$ and $Y \rightarrow Z$, then $X \rightarrow Z$

Proof:

- 1. Let R be a relation scheme.
- 2. Let $X \rightarrow Y$ and $Y \rightarrow Z$ be two functional dependencies on R.
- 3. Let T1 and T2 be two tuples of |R| are such that, for all attributes Ax in X, T1. Ax = T2.Ax.
- 4. We know that for all Ay in Y, T1. Ay = T2.Ay since $X \rightarrow Y$
- We know that for all Ay in Y, T1. Ay = T2.Ay since $Y \rightarrow Z$ Therefore for all Az in Z, T1. Az = T2.Az
- 7. Therefore $X \rightarrow Z$

Armstrong's Axioms

Armstrong's axioms are sound

For example: Consider the scheme {name, room, tel} with the set of functional dependencies:

 $\{\{\text{room}\} \rightarrow \{\text{tel}\}, \{\text{tel}\} \rightarrow \{\text{name}\}\}$

We can deduce that the following functional dependency holds:

 $\{\mathsf{room}\} \to \{\mathsf{name}\}$

Proof:

- 1. Let R= {name, room, tel}
- 2. Let $\{room\} \rightarrow \{tel\}$ be a functional dependency on R
- 3. Let $\{tel\} \rightarrow \{name\}$ be a functional dependency on R
- 4. Therefore {room} → {name} holds on R by Transitivity of (2) and (3)

Armstrong's Axioms

Armstrong's axioms are sound

For example: Weak-Augmentation Let X, Y, Z be subsets of the relation R

If
$$X \rightarrow Y$$
, then $X \cup Z \rightarrow Y$

Proof

- 1. Let R be a relation scheme
- 2. Let $X \rightarrow Y$ be a functional dependency on R
- Therefore $X \cup Z \rightarrow Y \cup Z$ by Augmentation of (2) with Z
- 4. We know that $Y \cup Z \to Y$ by Reflexivity because $Y \subset Y \cup Z$ 5. Therefore $X \cup Z \to Y$ by Transitivity of (3) and (4)

Closure of a Set of Functional Dependencies

For a set F of functional dependencies, we call the closure of F, noted F+, the set of all the functional dependencies that F entails

Armstrong's Axioms

Armstrong's axioms are complete

F+ can be computed by applying the Armstrong Axioms in all possible ways

WAll possible Armstony Axioms

Closure of a Set of Functional Dependencies

Consider the relation scheme R(A,B,C,D)

- $F = \{\{A\} \rightarrow \{B\}, \{B,C\} \rightarrow \{D\}\}$
- $\begin{tabular}{ll} \blacksquare & F+ = \{\{A\} \to \{A\}, \ \{B\} \to \{B\}, \ \{C\} \to \{C\}, \ \{D\} \to \{D\}, \end{tabular}$ $[...], \{A\} \rightarrow \{B\}, \{A,B\} \rightarrow \{B\}, \{A,D\} \rightarrow \{B,D\},$ ${A,C} \rightarrow {B,C}, {A,C,D} \rightarrow {B,C,D}, {\{A\} \rightarrow {A,B}},$ ${A,B} \rightarrow {A,B}, {A,D} \rightarrow {A,B,D}, {A,C} \rightarrow {A,B,C},$ $\{A,C,D\}\rightarrow \{A,B,C,D\}, \{B,C\}\rightarrow \{D\}, [...], \{A,C\}$ $\rightarrow \{D\}, [...]\}$

Equivalence of Sets of Functional Dependencies

Two sets of functional dependencies F and G are equivalent if and only if

F+=G+

Finding Keys: Example Example: Consider the relation scheme R(A,B,C,D)WTS: {A,B} -> {4,B,C,O} with functional dependencies: $\{A\} \rightarrow \{C\} \text{ and } \{B\} \rightarrow \{D\}.$ Is {A,B} a candidate key? Augmentation: {A,B3 > {B,C} >> ALL B on both side

{A,R3 > {A,B,C} -> Add A on both sides ? A, B, C} > { A, B, C, D} > Add A, B, C on both side,

Transitivity: {A,B} -> {A,B,C,O} houseon a Dather System

(> cas: {A,B} > {A,B,C} -> {A,B,C,O} : Superkey

Finding Keys: Example Proper proceeds too

Example: {A,B} is a superkey.

Proof

- 1. We know that $\{A\} \rightarrow \{C\}$
- 2. Therefore $\{A,B\} \rightarrow \{A,B,C\}$, by augmentation of (1) with{A,B}
- 3. We know that $\{B\} \rightarrow \{D\}$
- 4. Therefore $\{A,B,C\} \rightarrow \{A,B,C,D\}$, by augmentation of (3) with {A, B, C}
- 5. Therefore $\{A,B\} \rightarrow \{A,B,C,D\}$ by transitivity of (2) and (4)

Q.E.D

Finding Keys: Example

Example: {A,B} is a candidate key (minimal)

We must show that neither {A} nor {B} alone are candidate keys

This can be done by producing counter example relation instance verifying the functional dependencies given but neither {A}→{A,B,C,D} nor $\{B\}\rightarrow \{A,B,C,D\}$

We will however learn an algorithm to do otherwise

Closure of a Set of Attributes

For a set A of attributes, we call the **closure** of A (with respect to a set of functional dependencies F), noted A+, the maximum set of attributes such that A→A+ (as a consequence of F)

Closure of a Set of Attributes: Example

Consider the relation scheme R(A,B,C,D) with functional dependencies

$$\{A\} \rightarrow \{C\} \text{ and } \{B\} \rightarrow \{D\}.$$

•
$$\{A\}+=\{A,C\}$$

$$\{c\}^{+} = \{c\}$$

$$\{c\}^{+} = \{c\}$$

■
$$\{B\}$$
+ = $\{B,D\}$

■ {B}+ = {B,D}
■ {A,B}+ = {A,B,C,D}

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$$A$$

Closure of a Set of Attributes: Algorithm 1

- Input:
 - R a relation scheme
 - F a set of functional dependencies
 - X ⊂ R
- Output:
 - X+ the closure of X w.r.t. F

Closure of a Set of Attributes: Algorithm 1

- X⁽⁰⁾ := X
- Repeat
 - \blacksquare $X^{(i+1)} := X^{(i)} \cup A$, where A is the union of the sets Z of attributes such that there exist $Y \rightarrow$ Z in F, and Y \subset X⁽ⁱ⁾
- Until X⁽ⁱ⁺¹⁾ := X⁽ⁱ⁾
- Return X(i+1)

Closure of a Set of Attributes: Example

$$R = \{A,B,C,D,E,G\}$$

$$F = \{ \{A,B\} \rightarrow \{C\}, \{C\} \rightarrow \{A\}, \{B,C\} \rightarrow \{D\}, \{A,C,D\} \rightarrow \{B\}, \{D\} \rightarrow \{E,G\}, \{B,E\} \rightarrow \{C\}, \{C,G\} \rightarrow \{B,D\}, \{C,E\} \rightarrow \{A,G\} \}$$

$$X = \{B,D\} \qquad X^{o} = \{B,O\}$$

$$X = \{B,D\} \qquad X^{co} = \{B,O,E,G\} \quad (\{0\} \Rightarrow \{E,G\})$$

$$X = \{B,C,D,E,G\} \quad (\{B,E\} \Rightarrow \{C\})$$

$$X = \{B,D\} \qquad X^{co} = \{B,C,D,E,G\} \quad (\{B,E\} \Rightarrow \{C\})$$

$$X = \{B,D\} \qquad X^{co} = \{B,C,D,E,G\} \quad (\{C\} \Rightarrow \{F\})$$

Closure of a Set of Attributes: Example

 $R = \{A,B,C,D,E,G\}$

$$\begin{split} F &= \{ \ \{A,B\} \rightarrow \{C\}, \ \{C\} \rightarrow \{A\}, \ \{B,C\} \rightarrow \{D\}, \ \{A,C,D\} \rightarrow \{B\}, \ \{D\} \rightarrow \{E,G\}, \\ &\{B,E\} \rightarrow \{C\}, \ \{C,G\} \rightarrow \{B,D\}, \ \{C,E\} \rightarrow \{A,G\}\} \end{split}$$

 $X = \{B, D\}$

- $X^{(0)} = \{B, D\}$
- {D}→{E,G}
- $X^{(1)} = \{B, D, E, G\}$
- $\{B,E\}\rightarrow\{C\}$,
- $X^{(2)} = \{B,C,D,E,G\}$
- $\{C,E\}\rightarrow\{A,G\}$
- $X^{(3)} = X^{(4)} = X + = \{A,B,C,D,E,G\}$

I had it to the Deblace Park .

Equivalence of Sets of Functional Dependencies

Every set F of functional dependencies is equivalent to a set of functional dependencies Y→Z such that Z is a singleton, i.e. every right-hand side has a single attribute

Introduction to Database System

Minimal Set of Dependencies

A set of dependencies F is minimal if and only if:

- 1. Every right-hand side is a single attribute
- For no functional dependency X→A in F and proper subset Z of X is F {X→A} ∪ {Z→A} equivalent to F
- 3. For no functional dependency $X \rightarrow A$ in F is the set $F \{X \rightarrow A\}$ equivalent to F

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Minimal Cover

A set of functional dependencies F is a minimal cover of a set of functional dependencies G if and only if

- F is minimal
- F is equivalent to G



 (an <u>extended minimal cover</u> is obtained by undoing step 1)

Introduction to Database System

Minimal Cover

- Every set of functional dependencies has a minimal cover
- There might be several different minimal cover of the same set

Introduction to Database Systems

```
Eg: (0) + (E, 41 Las for + 123, 903 + 147
\begin{cases} 0.3 \Rightarrow \{E.3 \Rightarrow \{D, G.3 \Rightarrow \{E,G.3\}\} \\ 0.5 \Rightarrow \{G.3 \Rightarrow \{G.3 \Rightarrow \{D,G.3\}\} \} \Rightarrow \{G.3 \Rightarrow \{E,G.3\} \end{cases}
  (63 → 3E,43 : (E,43 - 1/2) : Reflectivity
                                   15,93 = {43 : Reflexivity
                               => {0} > {8} {03} > {6}? } Transierly
```

```
Minimal Cover: Example
                                                                                                                                                                 F = \{ \{A,B\} \rightarrow \{C\}, \{C\} \rightarrow \{A\}, \{B,C\} \rightarrow \{D\}, \{C\} \rightarrow \{C\}
                                                                                                                                                                                                                       \{A,C,D\}\rightarrow\{B\},\{D\}\rightarrow\{E,G\},\{B,E\}\rightarrow\{C\},
                                                                                                                                                                                                                  \{C,G\}\rightarrow\{B,D\}, \{C,E\}\rightarrow\{A,G\}\}
                                                                                                                                    Simplify all RHS !! : {0} > {E, G3 :
0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             1 CIE3 + (A,G) : ? CIE3 > (A)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             {4E3 = 163
```

Minimal Cover: Example (1) $F = \{ \{A,B\} \rightarrow \{C\}, \{C\} \rightarrow \{A\}, \{B,C\} \rightarrow \{D\}, \{C\} \rightarrow \{C\}$ ${A,C,D}\rightarrow {B}, {\underline{D}}\rightarrow {E,G}, {B,E}\rightarrow {C},$ $\{C,G\}\rightarrow \{B,D\}, \{C,E\}\rightarrow \{A,G\}$ $F' = \{ \{A,B\} \rightarrow \{C\}, \{C\} \rightarrow \{A\} \}, \{B,C\} \rightarrow \{D\}, \{C\} \rightarrow \{C\} \rightarrow$ $\{C,E\}\rightarrow\{A\}, \{C,E\}\rightarrow\{G\}\}$

{c,E3→{c3 -> {A3 I can be confresed.

Simplify

<>> {C,E} >1 H3

1A,C, D3 → 1R3

can derive

14,03 -> 183

from the other dependencies

103 -> 1A3

{63 → {63 ⇒ {603 → {6,63 ⇒ {83 > {6,03 → {83}} AND: FA, C, D3 -> (Rollemvitz) Minimal Cover: Example (2)

 $F' = \{\{C\} \rightarrow \{A\}, \underline{\{C,E\} \rightarrow \{A\}, \underline{\{A,C,D\} \rightarrow \{B\},}}$ $\{C,G\}\rightarrow \{B\}, \{A,B\}\rightarrow \{C\}, \{B,E\}\rightarrow \{C\},$ $\{B,C\}\rightarrow\{D\}, \{C,G\}\rightarrow\{D\}, \{D\}\rightarrow\{E\},$ $\{C,E\}\rightarrow\{G\}, \{D\}\rightarrow\{G\}\}$

 $F'' = \{\{C\} \rightarrow \{A\}, \{C,D\} \rightarrow \{B\}, \{C,G\} \rightarrow \{C,G\}, \{C,G\}, \{C,G\}, \{C,G\},$ $\{A,B\}\rightarrow\{C\}, \{B,E\}\rightarrow\{C\}, \{B,C\}\rightarrow\{D\},$ $\{C,G\}\rightarrow\{D\}, \{D\}\rightarrow\{E\}, \{C,E\}\rightarrow\{G\},$ $\{D\}\rightarrow\{G\}\}$

Minimal Cover: Example (3) can sofely remove Can be obtained $\{A,B\}\rightarrow \{C\}, \{B,E\}\rightarrow \{C\}, \{B,C\}\rightarrow \{D\},\$ $*\{C,G\}\rightarrow\{D\}, \{D\}\rightarrow\{E\}, \{C,E\}\rightarrow\{G\},$ from other functional $\{D\}\rightarrow\{G\}\}$ esignatures 16,43 > (0,0) $\{B,E\}\rightarrow\{C\}, \{B,C\}\rightarrow\{D\}, \{C,G\}\rightarrow\{D\},$ $\{D\}\rightarrow \{E\}, \{C,E\}\rightarrow \{G\}, \{D\}\rightarrow \{G\}\}$ =>{4,43 > {403

Extended Minimal Cover: Example (4)

 $F'''' = \{\{C\} \rightarrow \{A\}, \{C,D\} \rightarrow \{B\}, \{A,B\} \rightarrow \{C\},\$ $\{B,E\}\rightarrow\{C\}, \{B,C\}\rightarrow\{D\}, \{C,G\}\rightarrow\{D\},$ $\{D\} \rightarrow \{E,G\}, \{C,E\} \rightarrow \{G\}\}$ Combine 107 -> 1E3 503 > 243

Minimal Cover: Algorithm

We can apply steps (1), (2), (3) iteratively in various orders

However only (1) + (2) + (3) is guaranteed to lead to a minimal cover!:

- · Put functional dependencies in single attribute rhs
- · Minimize left side of each functional dependency
- · Delete redundant functional dependencies

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Credits

The content of this lecture is based on chapter 8 of the book "Introduction to database Systems"

By
S. Bressan and B. Catania, McGraw Hill publisher

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