

**CS2102 Database Systems**  
**2013/2014 Semester I**

**Tutorial #5 Functional Dependencies**

1. Is the following rule correct?

$$\forall X \in R \ \forall Y \in R \text{ (if } X \rightarrow Y \text{ then } Y \subseteq X)$$

2. The following rule is called pseudo-transitivity. Use Armstrong axioms to prove it.

$$\forall X \in R \ \forall Y \in R \ \forall Z \in R \ \forall W \in R \text{ (if } X \rightarrow Y \text{ and } Z \rightarrow W \text{ and } Z \subseteq Y, \text{ then } X \rightarrow W)$$

3. Consider the set of functional dependencies:

$F = \{ \{A\} \rightarrow \{B\}, \{C\} \rightarrow \{D\}, \{B, D\} \rightarrow \{E\}, \{D\} \rightarrow \{A, D\}, \{A, C\} \rightarrow \{E, B\} \}$  on the relation scheme  $R = \{A, B, C, D, E\}$ .

- a. Give an example instance of  $R$  that complies with the functional dependencies.
- b. Give an example instance of  $R$  that violates the functional dependencies.
- c. Compute  $F^+$ , the closure of  $F$ .
- d. Give an example of a trivial functional dependency in  $F^+$ .
- e. Give an example of a non-trivial functional dependency in  $F^+$ .
- f. Compute  $\{C\}^+$ , the closure of the set of attributes  $\{C\}$ .
- g. Compute a minimal cover of  $F$ .