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Capital Asset Pricing Model

In addition to the Capital Market Line, we will further introduce another important Asset Pricing Model which is also called CAPM and pronounced "cap M".

The CAPM is a model that describes the relationship between systematic risk and assets. The CAPM assumes that the excess return of a stock is determined by the stock's relationship with the market's movement. It is the foundation of the factor models used by portfolio managers for portfolio construction.

Ok, let's quickly recap: the systematic risk, or market risk, is undiversifiable risk of the entire market. In contrast, the idiosyncratic risk is the asset-specific risk.

Ok, let's take a look at CAPM. For a stock, the return of stock i equals the return plus β times the difference between the market return and the risk free return. The covariance of stock i and the market divided by the variance of the market.

$$r_i - r_f = \beta \times (r_m - r_f)$$

r_i = stock return

r_f = risk free rate

r_m = market return

$$\beta_i = \frac{\text{cov}(r_i, r_m)}{\sigma_m^2}$$

β describes which direction and by how much a stock or portfolio moves relative to the market. For example, if a stock has a β of 1, this indicates that if the market's excess return is 5%, the stock's excess return would also be 5%. If a stock has a β of 1.1, this indicates that if the market's excess return is 5%, the stock's excess return would be $1.1 \times 5\%$, or 5.5%.

Compensating Investors for Risk

Generally speaking, investors need to be compensated in two ways: time value of money and risk. The time value of money is represented by the risk free return. This is the compensation for putting down investments over a period of time. β times $r_m - r_f$ represents the compensation for taking on market risk. It is the additional excess return the investor would require for taking on market exposure, β . $r_m - r_f$ is the risk premium, and β reflects the exposure of an asset to market risk.

When the β_i for stock i equals 1, stock i moves up and down with the same magnitude as the market. When β_i is greater than 1, stock i moves up and down more than the market. If β_i is less than 1, stock i moves up and down less than the market.

Let's look at a simple example. If the risk free return is 2%, β_i of stock i equals 1.2, and the market return is 10%, the return of stock i equals $2\% + 1.2 \times (10\% - 2\%) = 11.6\%$.

$$r_f = 2\%$$

$$\beta_i = 1.2$$

$$r_m = 10\%$$

$$r_i = 2\% + 1.2 \times (10\% - 2\%) = 11.6\%$$

Security Market Line

The Security Market Line is the graphical representation of CAPM and it represents the relationship between the risk and return of stocks. Please note that it is different from the Capital Market Line. The y-axis is expected returns but the x-axis is beta. (You may recall that for the Capital Market Line, the x-axis was standard deviation of a portfolio.) As beta increases, the return increases. Hence, the investors demand higher returns to compensate risk.