

- Let us say, the magnitude of the voltage across the red phase i.e. magnitude of the voltage between neutral point (N) and red phase terminal (R) is  $V_R$ .
- The magnitude of the voltage across yellow phase is  $V_Y$  and the magnitude of the voltage across blue phase is  $V_B$ .
- In the balanced star system, magnitude of phase voltage in each phase is  $V_{ph}$ .  
 $\therefore V_R = V_Y = V_B = V_{ph}$
- We know in the star connection, line current is same as phase current. The magnitude of this current is same in all three phases and say it is  $I_L$ .  
 $\therefore I_R = I_Y = I_B = I_L$ , Where,  $I_R$  is line current of R phase,  $I_Y$  is line current of Y phase and  $I_B$  is line current of B phase. Again, phase current,  $I_{ph}$  of each phase is same as line current  $I_L$  in star connected system.  
 $\therefore I_R = I_Y = I_B = I_L = I_{ph}$ .

Now, let us say, the voltage across R and Y terminal of the star connected circuit is  $V_{RY}$ .

The voltage across Y and B terminal of the star connected circuit is  $V_{YB}$ .

From the diagram, it is found that

$$V_{RY} = V_R + (-V_Y)$$

$$\text{Similarly, } V_{YB} = V_Y + (-V_B)$$

$$\text{And, } V_{BR} = V_B + (-V_R)$$

Now, as angle between  $V_R$  and  $V_Y$  is  $120^\circ$  (electrical), the angle between  $V_R$  and  $-V_Y$  is  $180^\circ - 120^\circ = 60^\circ$  (electrical).

$$\begin{aligned} V_L = |V_{RY}| &= \sqrt{V_R^2 + V_Y^2 + 2V_R V_Y \cos 60^\circ} \\ &= \sqrt{V_{ph}^2 + V_{ph}^2 + 2V_{ph} V_{ph} \times \frac{1}{2}} \\ &= \sqrt{3} V_{ph} \\ \therefore V_L &= \sqrt{3} V_{ph} \end{aligned}$$

Thus, for the star-connected system line voltage =  $\sqrt{3} \times$  phase voltage.

Line current = Phase current

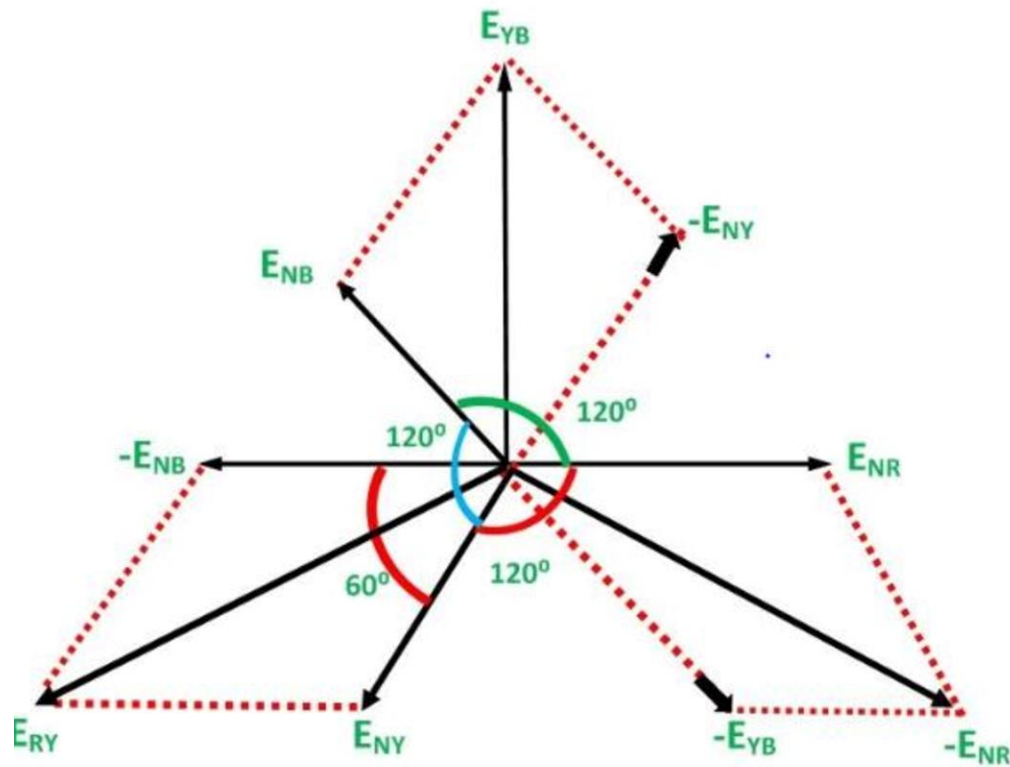
As, the angle between voltage and current per phase is  $\phi$ , the electric power per phase is

$$V_{ph} I_{ph} \cos \phi = \frac{V_L}{\sqrt{3}} I_L \cos \phi$$

So the total power of three phase system is

$$3 \times \frac{V_L}{\sqrt{3}} I_L \cos \phi = \sqrt{3} V_L I_L \cos \phi$$

or **Diagram** of Star Connection is shown below.



$$E_{RY} = \sqrt{E_{NY}^2 + E_{NR}^2 + 2E_{NY}E_{NR} \cos 60^\circ} \quad \text{or}$$

$$E_L = \sqrt{E_{ph}^2 + E_{ph}^2 + 2E_{ph}E_{ph} \times 0.5} \quad \text{or}$$

$$E_L = \sqrt{3E_{ph}^2} = \sqrt{3} E_{ph} \quad (\text{in magnitude})$$

Similarly,

$$E_{YB} = E_{NB} - E_{NY} \quad \text{or} \quad E_L = \sqrt{3} E_{ph} \quad \text{and}$$

$$E_{BR} = E_{NR} - E_{NB} \quad \text{or} \quad E_L = \sqrt{3} E_{ph}$$

Hence, in Star Connections Line voltage is root 3 times c

$$\text{Line voltage} = \sqrt{3} \times \text{Phase voltage}$$

$$E_{NR} = E_{NY} = E_{NB} = E_{ph}$$

$$E_{RY} = \sqrt{E_{NY}^2 + E_{NR}^2 + 2E_{NY}E_{NR} \cos 60^\circ} \quad \text{or}$$

$$E_L = \sqrt{E_{ph}^2 + E_{ph}^2 + 2E_{ph}E_{ph} \times 0.5} \quad \text{or}$$

$$E_L = \sqrt{3E_{ph}^2} = \sqrt{3} E_{ph} \quad (\text{in magnitude})$$

Similarly,

$$E_{YB} = E_{NB} - E_{NY} \quad \text{or} \quad E_L = \sqrt{3} E_{ph} \quad \text{and}$$

$$E_{BR} = E_{NR} - E_{NB} \quad \text{or} \quad E_L = \sqrt{3} E_{ph}$$

Hence, in Star Connections Line voltage is root 3 times of phase voltage.

$$\text{Line voltage} = \sqrt{3} \times \text{Phase voltage}$$

# THREE PHASE SYSTEM

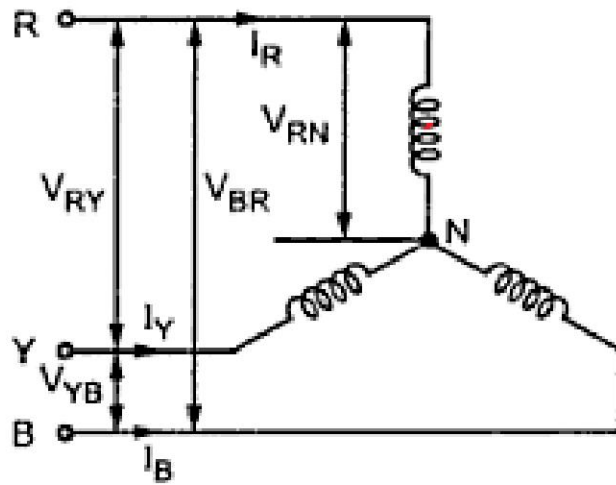
## BASICS

Line voltage  $V_L$  = voltage between lines

Phase voltage  $V_{ph}$  = voltage between a line and neutral

# THREE PHASE SYSTEM

## BALANCED STAR



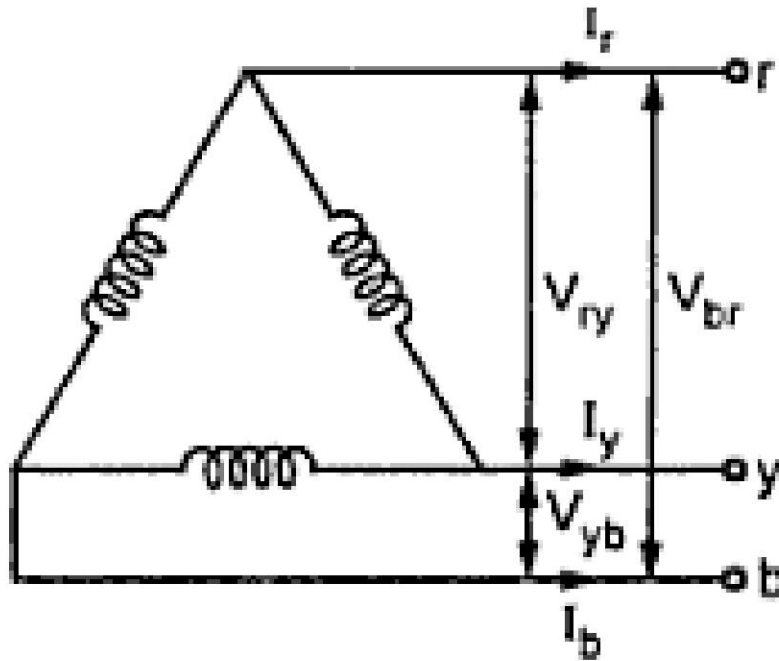
Line Voltage  $V_L = \sqrt{3} V_{ph}$

Line current  $I_L = I_{ph}$



# THREE PHASE SYSTEM

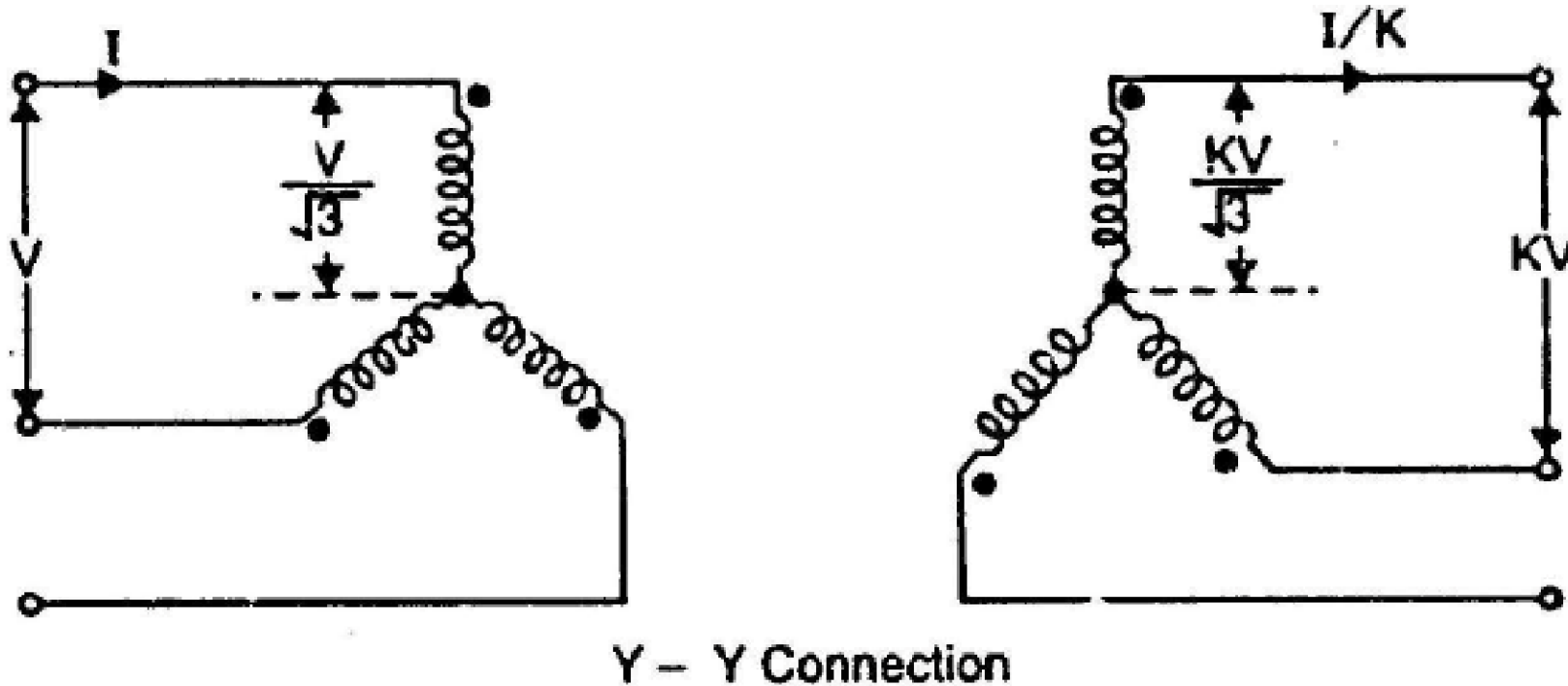
## BALANCED DELTA



Line Voltage  $V_L = V_{ph}$

Line current  $I_L = \sqrt{3} I_{ph}$

# Star- Star connection



- This connection satisfactory only in balanced load otherwise neutral point will be shifted.

# Star- Star connection

## Advantages

- 1.Requires less turns per winding ie cheaper**  
*Phase voltage is  $1/\sqrt{3}$  times of line voltage*
- 2.Cross section of winding is large ie stronger to bear stress during short circuit**  
*Line current is equal to phase current*
- 3. Less dielectric strength in insulating materials**  
*phase voltage is less*

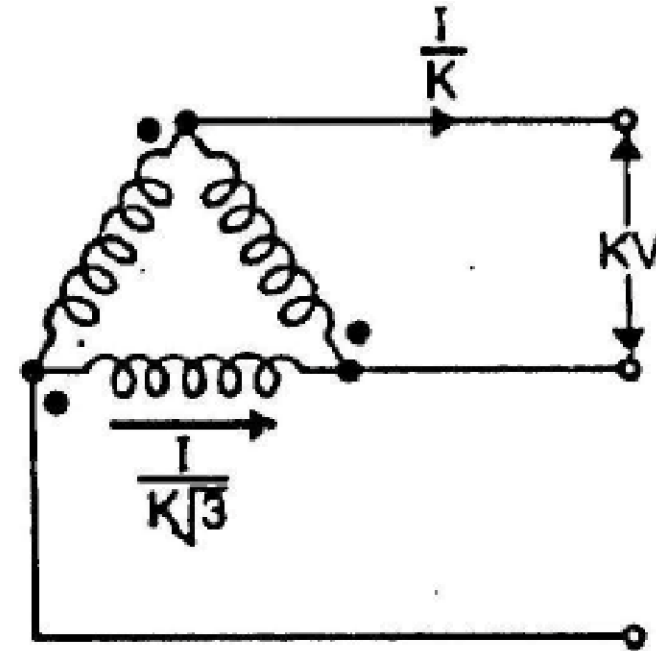
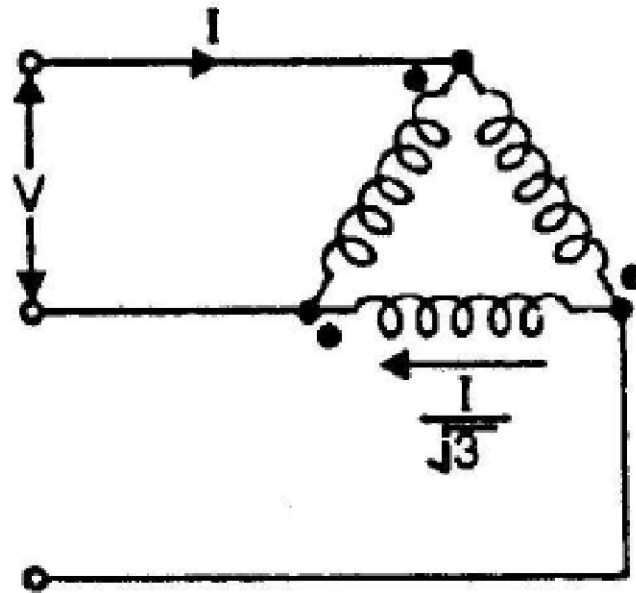
# Star- Star connection

## Disadvantages

- 1.If the load on the secondary side **unbalanced** then the **shifting of neutral point** is possible
- 2.The **third harmonic present** in the alternator voltage may appear on the secondary side. This causes distortion in the secondary phase voltages
3. Magnetizing current of transformer has **3<sup>rd</sup> harmonic** component

# Delta - Delta connection

(i)



$\Delta - \Delta$  Connection

➤ This connection is used for moderate voltages

# Delta - Delta connection

## Advantages

- 1. System voltages are more stable in relation to unbalanced load**
- 2. If one t/f is failed it may be used for low power level ie V-V connection**
- 3. No distortion of flux ie 3<sup>rd</sup> harmonic current not flowing to the line wire**

# Delta - Delta connection

## Disadvantages

1. Compare to Y-Y require more **insulation**
2. Absence of star point ie fault may severe