

# CONTEXT REASONING FOR ROLE-BASED MODELS

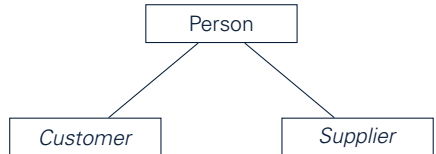
Stephan Böhme

Dresden, 27.10.2017

# Motivation

## What is a Role?

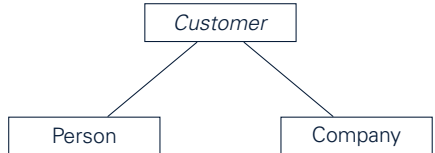
- Modelling concept from OOP introduced by Bachman in 1973
- Classification of roles with 26 *Features* including identity, behaviour, relationships, players, ... and about Contexts and Constraints (Kühn, Leuthäuser, et al. 2014; Steimann 2000)



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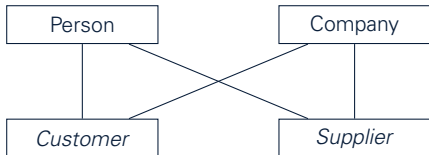
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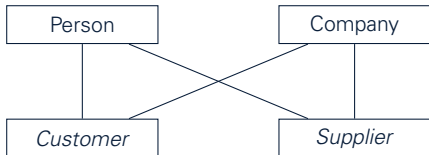
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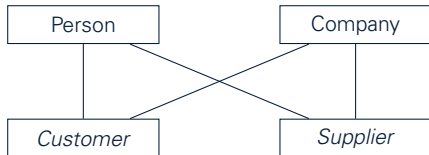
## Requirements for modern Software Systems:

- Adaptability
- High expressiveness
- Longevity

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## Requirements for modern Software Systems:

- Adaptability → Roles allow for dynamic changes of the system.
- High expressiveness → Roles increase separation of concerns.
- Longevity → Roles enable updating running applications.

# Role-Based Systems

- Software systems that use the notion of roles
- Focus on: Compartment Role Object Model (CROM), (Kühn, Leuthäuser, et al. 2014)
  - Well-defined semantical foundation (Kühn, Böhme, et al. 2015)

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  - Modelling errors stay undetected
- ↳ Logic-based formalisms

## Requirements on logical formalism

- Decidable reasoning tasks
- Express contexts, 'players' and roles as formal objects
- Model contexts and ternary relation of role-playing
- Ability to handle *rigid*, i.e. context-independent, knowledge

# Workflow of Automated Analysis of Role-Based Models



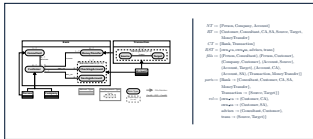
Banking  
application

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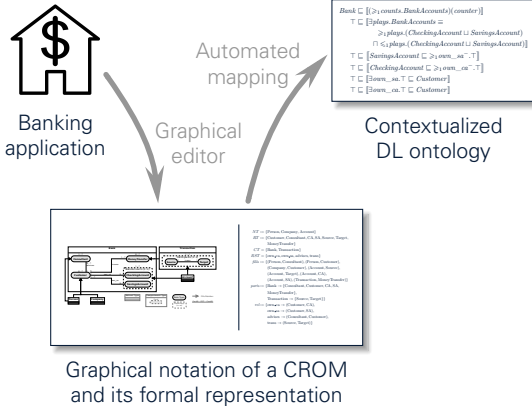
Banking  
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Graphical  
editor

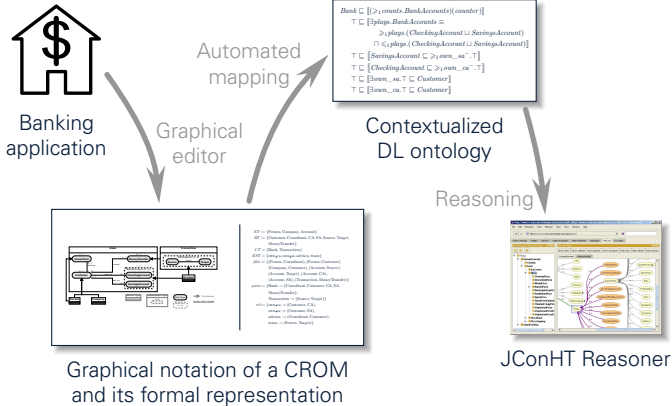


Graphical notation of a CROM  
and its formal representation

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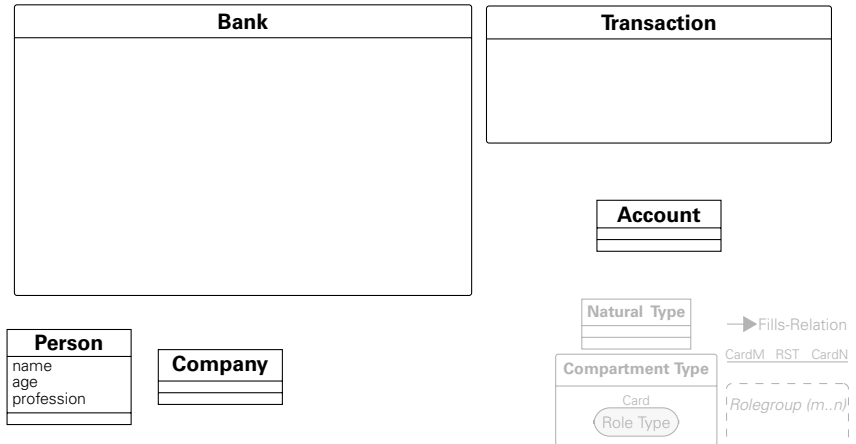
## 3



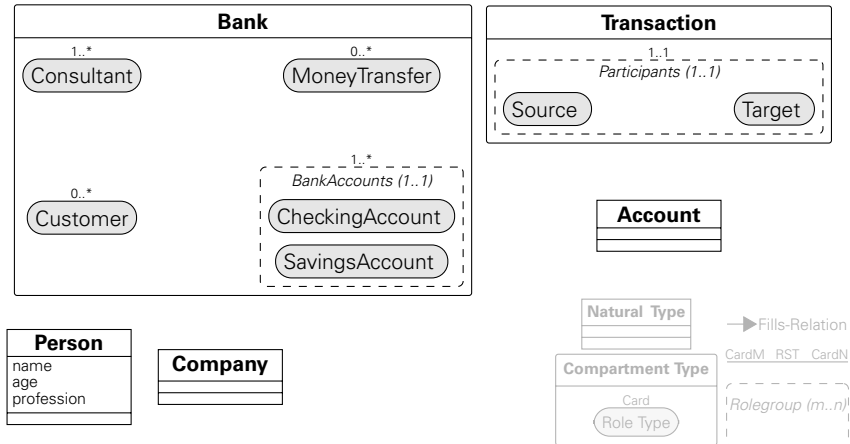
# Running Example – Banking Application



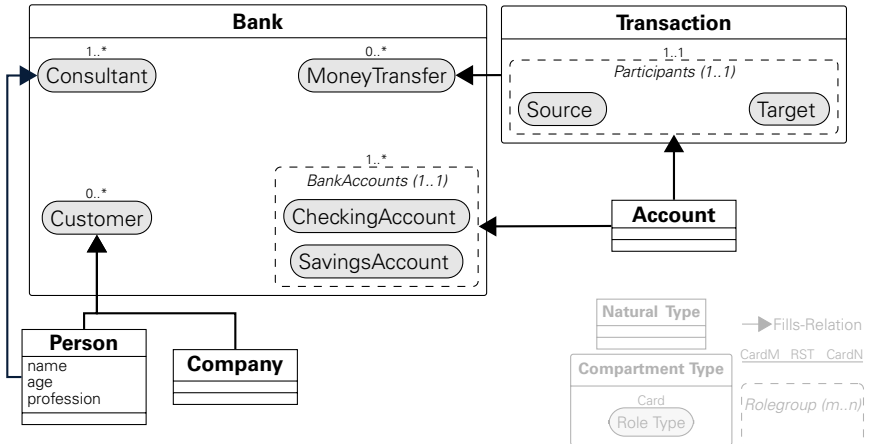
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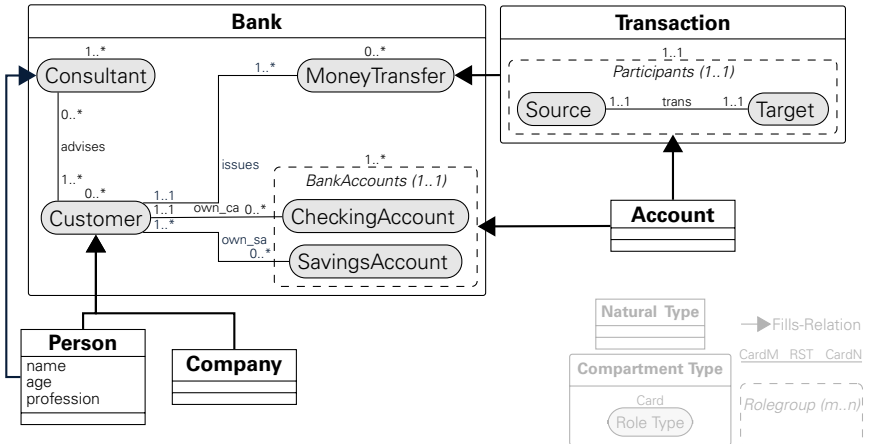
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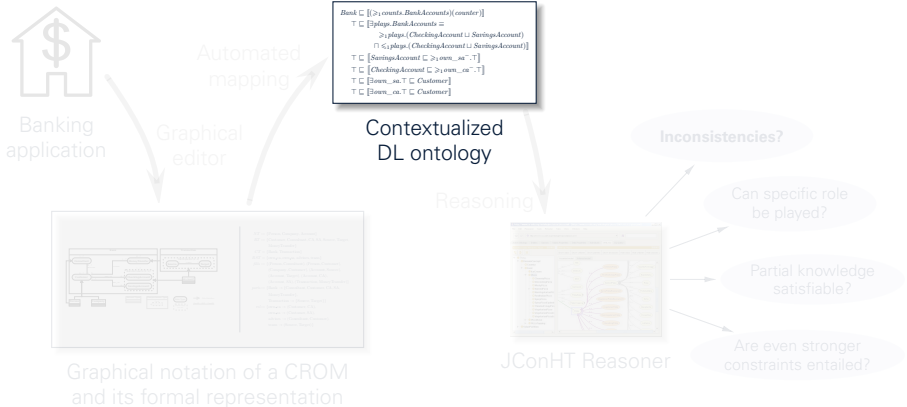
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# Workflow of Automated Analysis of Role-Based Models



## Syntax and Semantics of the DL $\mathcal{ALC}$

Every consultant advises customers who own an checking account.

$\text{CONSULTANT} \sqsubseteq \exists \text{advises.}(\text{CUSTOMER} \sqcap \exists \text{own\_ca.CHECKINGACCOUNT})$

Peter is a consultant.       $\text{CONSULTANT}(\text{Peter})$

## Syntax and Semantics of the DL $\mathcal{ALC}$

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$N_C$  ... concept names

$N_R$  ... DL role names

$N_I$  ... individual names

CONSULTANT, CUSTOMER, CHECKINGACCOUNT

advises, own\_ca

*Peter*



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$N_I$  ... individual names

Peter

concept constructors:

$C_1 \sqcap C_2, C_1 \sqcup C_2, \neg C_1, \exists r.C, \forall r.C$

set of  $\mathcal{ALC}$  concepts:

smallest set that is closed under  $N_C$  and the concept constructors of  $\mathcal{ALC}$

General concept inclusion (GCI):

$C \sqsubseteq D$

assertion:

$C(a), r(a, b)$

$\mathcal{ALC}$ -axiom:

a GCI or an assertion

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A DL interpretation  $\mathcal{I}$  has a domain  $\Delta^{\mathcal{I}}$  and maps

- concept names  $A$  to sets  $A^{\mathcal{I}} \subseteq \Delta^{\mathcal{I}}$ ,
- DL role names  $r$  to binary relations  $r^{\mathcal{I}} \subseteq \Delta^{\mathcal{I}} \times \Delta^{\mathcal{I}}$ , and
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The semantics of the constructors is defined as

- $(C \sqcap D)^{\mathcal{I}} := C^{\mathcal{I}} \cap D^{\mathcal{I}}$ ,
- $(\neg C)^{\mathcal{I}} := \Delta^{\mathcal{I}} \setminus C^{\mathcal{I}}$ , and
- $(\exists r.C)^{\mathcal{I}} := \{d \in \Delta^{\mathcal{I}} \mid \exists e.(d, e) \in r^{\mathcal{I}} \wedge e \in C^{\mathcal{I}}\}$

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Interpretation  $\mathcal{I}$  is a model of

- the GCI  $C \sqsubseteq D$  iff  $C^{\mathcal{I}} \subseteq D^{\mathcal{I}}$ , and
- the assertion  $C(a) \text{ } (r(a, b))$  iff  $a^{\mathcal{I}} \in C^{\mathcal{I}}$  ( $(a^{\mathcal{I}}, b^{\mathcal{I}}) \in r^{\mathcal{I}}$ ).

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# Intuition of Contextualized DL $\mathcal{L}_M \llbracket \mathcal{L}_O \rrbracket$

- Two-dimensional, two-sorted description logic
- $\mathcal{L}_M$  to describe knowledge *about* contexts (meta level)
- $\mathcal{L}_O$  to describe knowledge *within* contexts (object level)
- Contexts  $\hat{=}$  possible worlds
- Concepts, axioms of object logic are usual  $\mathcal{L}_O$  concepts, axioms
- Object axioms used as meta concepts
  - $\underbrace{\llbracket C \sqsubseteq D \rrbracket}_{\text{meta concept}}$  describes set of worlds where  $\underbrace{C \sqsubseteq D}_{\text{object axiom}}$  holds

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# Syntax and Semantics of $\mathcal{L}_M$ $[[\mathcal{L}_O]]$



# Syntax and Semantics of $\mathcal{L}_M \llbracket \mathcal{L}_O \rrbracket$

$$O = (O_C, O_R, O_I)$$

$$O_{\text{Crig}} \subseteq O_C$$

$$O_{\text{Rrig}} \subseteq O_R$$

$$M = (M_C, M_R, M_I)$$

object concept name  $A \in O_C$

object concept  $C$  (using constructors of  $\mathcal{L}_O$ )

object axioms  $C \sqsubseteq D$   
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$\mathcal{L}_M \llbracket \mathcal{L}_O \rrbracket$  ontology  $\mathcal{B} \dots$  conjunction of m-axioms

# Syntax and Semantics of $\mathcal{L}_M \llbracket \mathcal{L}_O \rrbracket$

Nested interpretation  $\mathcal{J} = (\mathbb{C}, \cdot^{\mathcal{J}}, \Delta^{\mathcal{J}}, (\cdot^{\mathcal{I}_c})_{c \in \mathbb{C}})$

- $(\mathbb{C}, \cdot^{\mathcal{J}})$  DL interpretation on meta level
- $(\Delta, \cdot^{\mathcal{I}_c})$  DL interpretation on object level for each possible world
- $x^{\mathcal{I}_c} = x^{\mathcal{I}_d}$  for all  $c, d \in \mathbb{C}$ ,  $x \in O_{\text{Crig}} \cup O_{\text{Rrig}} \cup O_I$

object concept name  $A^{\mathcal{I}_c} \subseteq \Delta$

object concept  $C$

meta concepts  $\llbracket C \sqsubseteq D \rrbracket$

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meta concept name  $B^{\mathcal{J}} \subseteq \mathbb{C}$

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$\mathcal{L}_M \llbracket \mathcal{L}_O \rrbracket$  ontology  $\mathcal{B}$

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object concept name  $A^{\mathcal{I}_c} \subseteq \Delta$

object concept  $C^{\mathcal{I}_c} \subseteq \Delta$  (acc. to semantics of  $\mathcal{L}_O$ )

meta concepts  $\llbracket C \sqsubseteq D \rrbracket^{\mathcal{J}} := \{c \in \mathbb{C} \mid \mathcal{I}_c \models C \sqsubseteq D\}$   
 $\llbracket C(a) \rrbracket^{\mathcal{J}} := \{c \in \mathbb{C} \mid \mathcal{I}_c \models C(a)\}$

meta concept name  $B^{\mathcal{J}} \subseteq \mathbb{C}$

meta concept  $E^{\mathcal{J}} \subseteq \mathbb{C}$  (acc. to semantics of  $\mathcal{L}_M$ )

meta axioms  $\left. \begin{array}{l} \mathcal{J} \models E \sqsubseteq F \\ \mathcal{J} \models E(c) \end{array} \right\} \text{standard entailment relation}$

$\mathcal{L}_M \llbracket \mathcal{L}_O \rrbracket$  ontology  $\mathcal{J} \models \mathcal{B}$

## Example of Contextualized DL $\mathcal{L}_M \llbracket \mathcal{L}_O \rrbracket$

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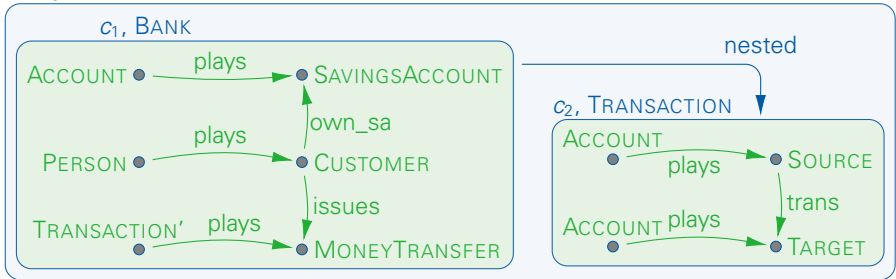
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$\mathbb{C}$





# Complexity of Consistency Problem

$\mathcal{L}_M \backslash \mathcal{L}_O$		$\mathcal{EL}$	$\mathcal{ALC} - \mathcal{SHOQ}$	$\mathcal{SHOIQ}$
no rigid names	$\mathcal{EL}$	constant	EXP-complete	NEXP-complete
	$\mathcal{ALC} - \mathcal{SHOQ}$			
	$\mathcal{SHOIQ}$			
only rigid concepts	$\mathcal{EL}$	constant		NEXP-hard and in 2NEXP
	$\mathcal{ALC} - \mathcal{SHOQ}$		NEXP-complete	
	$\mathcal{SHOIQ}$			
with rigid roles	$\mathcal{EL}$	constant		2EXP-hard and in 2NEXP
	$\mathcal{ALC} - \mathcal{SHOQ}$	NEXP-complete	2EXP-complete	
	$\mathcal{SHOIQ}$			

## Upper Bounds for $\mathcal{L}_M$ $[\mathcal{L}_O]$

Idea: Split consistency problem into two separate decision problems

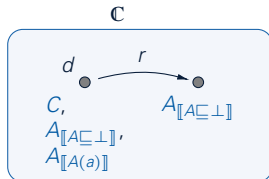
- *Outer consistency* with  $\mathcal{X}$
- *Admissibility* of  $\mathcal{X}$

Check whether meta level is consistent.

Check whether the induced o-axioms are consistent.

$$\begin{aligned}\mathcal{B}_{ex} = & C \sqsubseteq [A(a)] \\ & \wedge (C \sqcap [A \sqsubseteq \perp])(d) \\ & \wedge (\exists r. [A \sqsubseteq \perp])(d)\end{aligned}$$

$$\mathcal{X} = \underbrace{\{\emptyset, \{[A(a)]\}, \{[A \sqsubseteq \perp]\}\}}_{\{[A(a)], [A \sqsubseteq \perp]\} \notin \mathcal{X}}$$



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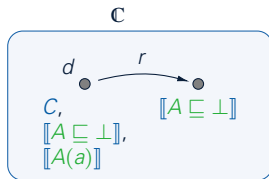
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$$\wedge (C \sqcap [[A \sqsubseteq \perp]])(d)$$

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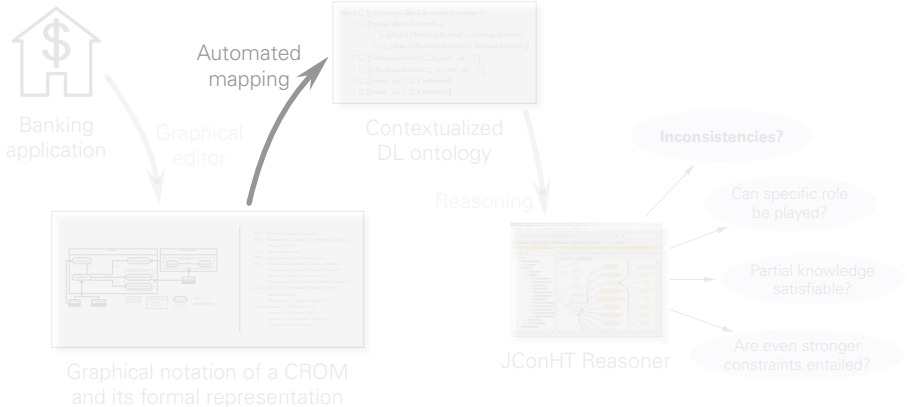
- *Outer consistency with  $\mathcal{X}$*
- *Admissibility of  $\mathcal{X}$*

### Lemma

*The  $\mathcal{L}_M \llbracket \mathcal{L}_O \rrbracket$  ontology  $\mathcal{B}$  is consistent iff there is a set  $\mathcal{X}$  such that*

1.  *$\mathcal{X}$  is admissible, and*
2. *the outer abstraction of  $\mathcal{B}$  is outer consistent w.r.t.  $\mathcal{X}$ .*

# Workflow of Automated Analysis of Role-Based Models



# Automated Mapping

Objective:      Given a CROM  $\mathcal{M}$ , construct an ontology  $\mathcal{O}_{\mathcal{M}}$  s.t.  
                          $\mathcal{O}_{\mathcal{M}}$  consistent iff  $\mathcal{M}$  satisfiable

# Automated Mapping

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General idea:

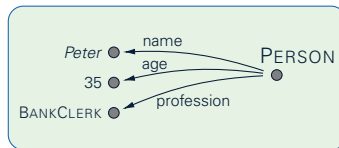
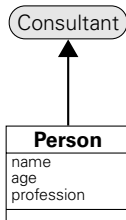
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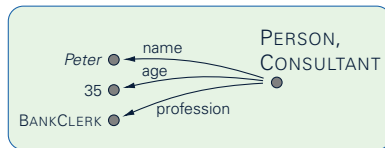
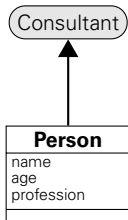


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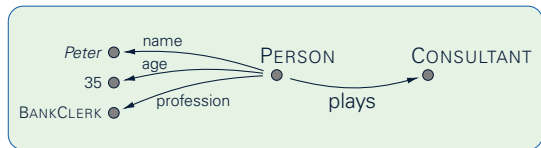
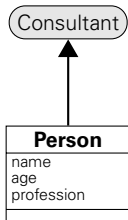


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• Compartment types	$\rightsquigarrow$ meta concepts
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• Fields of natural types	$\rightsquigarrow$ (rigid) object DL roles
• Role Types	$\rightsquigarrow$ (non-rigid) object concepts
• plays-relation	$\rightsquigarrow$ (non-rigid) object DL role
• Relationship types	$\rightsquigarrow$ (non-rigid) object DL roles
• Occurrence constraints	$\rightsquigarrow$ object individual $\delta$ , DL role 'counting'

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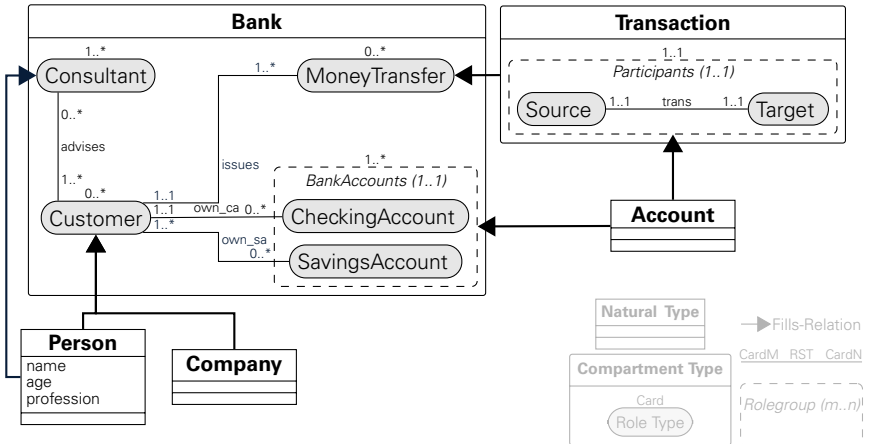
Constraints:

- without constraints  $\rightsquigarrow$   $ALLC \llbracket ALLCTQ \rrbracket$
- with occurrence constraints  $\rightsquigarrow$   $ALLC \llbracket ALLCOTQ \rrbracket$
- full  $\rightsquigarrow$   $ALLC \llbracket SHOTQ \rrbracket$
- current version of CROM  $\rightsquigarrow$  no rigid DL roles needed
- additional constraints based on fields of natural type  $\rightsquigarrow$  rigid roles needed!

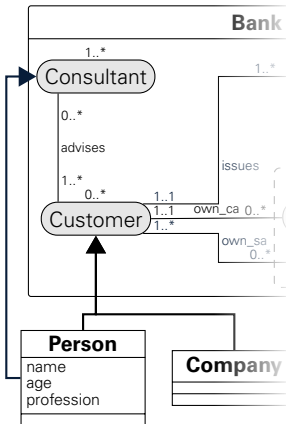
# Complexity of Consistency Problem

$\mathcal{L}_M \backslash \mathcal{L}_O$		$\mathcal{EL}$	$\mathcal{ALC} - \mathcal{SHOQ}$	$\mathcal{SHOIQ}$
no rigid names	$\mathcal{EL}$	constant	EXP-complete	CROM ★ NEXP-complete
	$\mathcal{ALC} - \mathcal{SHOQ}$			
	$\mathcal{SHOIQ}$			
only rigid concepts	$\mathcal{EL}$	constant		NEXP-hard and in 2NEXP
	$\mathcal{ALC} - \mathcal{SHOQ}$		NEXP-complete	
	$\mathcal{SHOIQ}$			
with rigid roles	$\mathcal{EL}$	constant		2EXP-hard and in 2NEXP
	$\mathcal{ALC} - \mathcal{SHOQ}$	NEXP-complete	2EXP-complete	
	$\mathcal{SHOIQ}$			

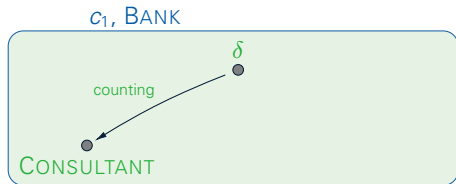
## Example of Mapping



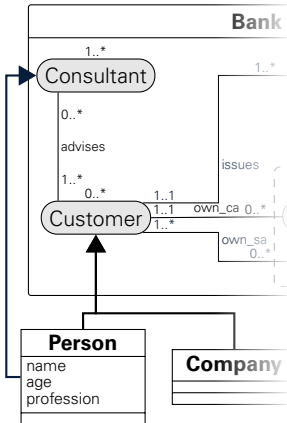
## Example of Mapping



$$\begin{aligned} T &\sqsubseteq [\text{CONSULTANT LI CUSTOMER} \sqsubseteq =_1 \text{counting}^- . \{\delta\}] \\ \text{BANK} &\sqsubseteq [(\geq_1 \text{counting} . \text{CONSULTANT})(\delta)] \end{aligned}$$



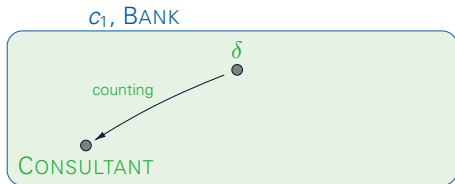
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$$T \sqsubseteq [\text{CONSULTANT} \sqcup \text{CUSTOMER} \sqsubseteq =_1 \text{counting}^- . \{\delta\}]$$

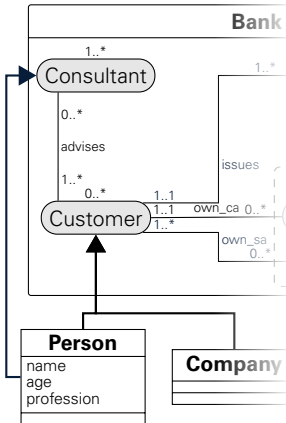
$$\text{BANK} \sqsubseteq [(\geq_1 \text{counting} . \text{CONSULTANT})(\delta)]$$

$$\text{BANK} \sqsubseteq [T \sqsubseteq \forall . \text{advises} . \text{CUSTOMER}]$$

$$\text{BANK} \sqsubseteq [\text{CONSULTANT} \sqsubseteq \geq_1 \text{advises} . T]$$




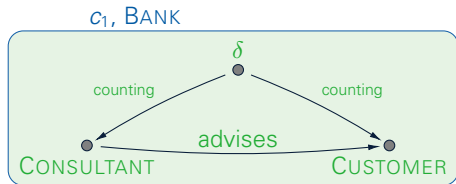
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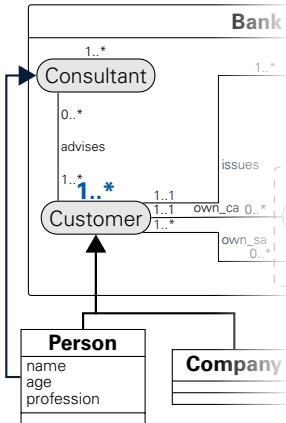
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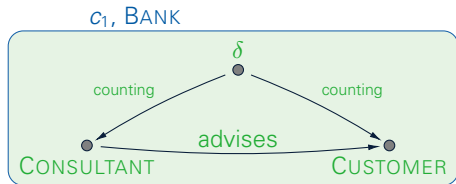
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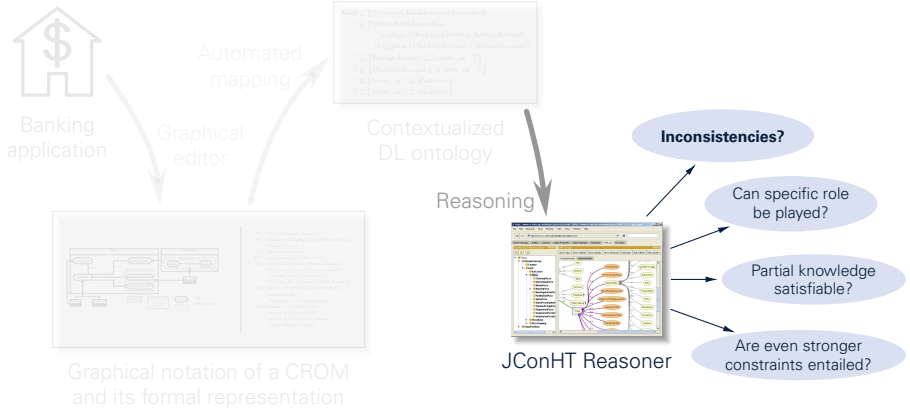
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# Workflow of Automated Analysis of Role-Based Models



## JConHT – A *SHOIQ* [*SHOIQ*] Reasoner

- Java implemented **Contextualized** description logic reasoner based on **HermiT/HyperTableau**
  - First reasoner capable of processing contextualized DL ontologies
  - Utilize Lemma about separation of reasoning tasks
    1. Check consistency of meta level
    2. Check whether induced object axioms consistent
  - Reuse existing, highly optimized reasoners
    - Model-construction based reasoner necessary
    - Implemented in Java
    - Good performance on DL Consistency
- ↳ HermiT as core reasoner

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# Algorithm for Checking Consistency

**Input** :  $\mathcal{SHOIQ}$  [ $\mathcal{SHOIQ}$ ]-ontology  $\mathcal{O}$

**Output**: true if  $\mathcal{O}$  is consistent, false otherwise

Preprocessing (results in  $(\mathcal{C}, \mathcal{A})$ ):

1. Elimination of transitivity axioms, normalization, clausification
2. Repletion of DL-clauses

Let  $(T, \lambda)$  be any derivation for  $(\mathcal{C}, \mathcal{A})$ .

$\mathfrak{A} := \{\mathcal{A}' \mid \text{there exists a leaf node in } (T, \lambda) \text{ that is labelled with } \mathcal{A}'\}$

**for**  $\mathcal{A}' \in \mathfrak{A}$  **do**

**if**  $\mathcal{A}'$  is clash-free **then**

**if**  $\mathcal{O}$  contains rigid names **then**

**if**  $\mathcal{K}_{\text{rig}} := (\mathcal{O}_{\mathcal{A}'}, \mathcal{R}_{\mathcal{O}'})$  is consistent **then**

└ **return** true

**else**

Let  $\{c_1, \dots, c_k\}$  be the individuals occurring in  $\mathcal{A}'$

**if**  $\mathcal{K}_i := (\mathcal{O}_{c_i}, \mathcal{R}_{\mathcal{O}})$  is consistent for all  $1 \leq i \leq k$  **then**

└ **return** true

**return** false



## Repletion of DL-Clauses

$$\begin{aligned}\mathcal{B}_{\text{ex}} &:= \neg C(s) \\ &\wedge [\neg B(a)] \sqsubseteq C \\ &\wedge \neg C \sqsubseteq [B \sqsubseteq \perp]\end{aligned}$$

## Repletion of DL-Clauses

$$\mathcal{B}_{\text{ex}} := \neg C(s)$$

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$$\mathcal{A}_{\text{ex}} := \{\neg C(s)\}$$

$$\mathcal{C}_{\text{ex}} := \{[\neg B(a)](x) \rightarrow C(x),$$

$$\top \rightarrow C(x) \vee [B \sqsubseteq \perp](x)\}$$

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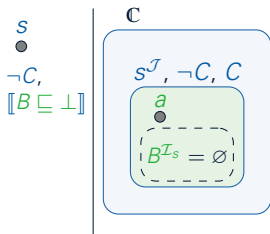
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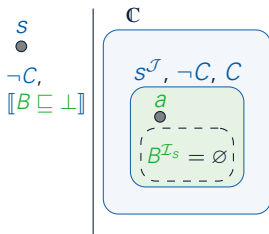
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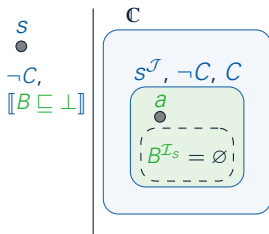
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Let  $\mathcal{C}$  be a set of DL-clauses. The **repletion** of  $\mathcal{C}$  is obtained from  $\mathcal{C}$  by adding the DL-clause  $\top \rightarrow [\alpha](x) \vee [\neg \alpha](x)$  for each o-axiom  $[\alpha]$  occurring in  $\mathcal{C}$ .

## Repletion of DL-Clauses

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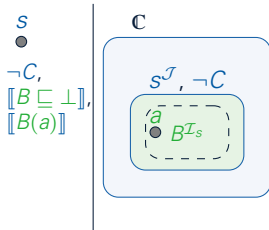
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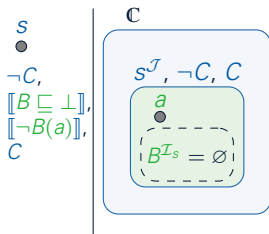
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Thank you for your attention!

Any questions?



# Performance Evaluation

- Pseudo-random domain models of increasing complexity:
  - based on parameter  $n$
  - $n$  natural types,  $n$  compartment types, for each compartment type  $n$  role types
- 3 different scenarios
  1. Number of (constrained) relationship types per compartment type
  2. Number of role groups per compartment type
  3. Whether or not compartments can play roles.
- Average execution time of JConHT
  - Translation from CROM models into ontologies neglected
  - For each configuration 100 executions
  - Average time needed to decide consistency

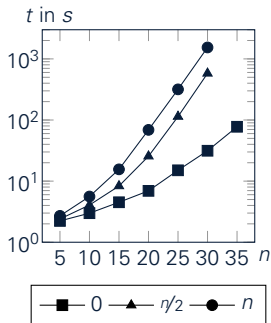
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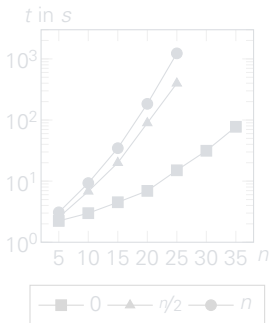
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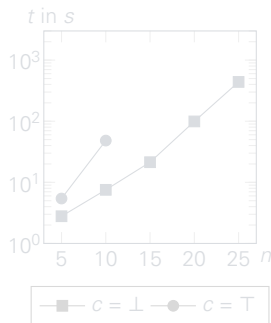
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(a) Variation of # RSTs.



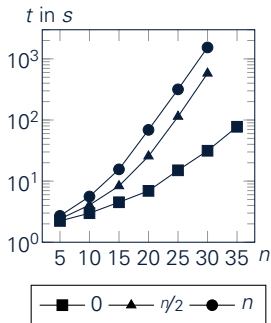
(b) Variation of # RGs.



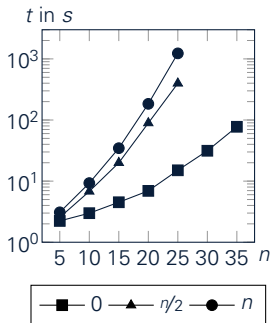
(c) Flat vs. nested CTs.

Average execution times of JConHT for benchmark ontologies.

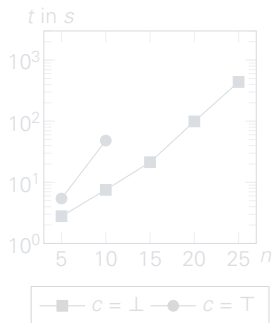
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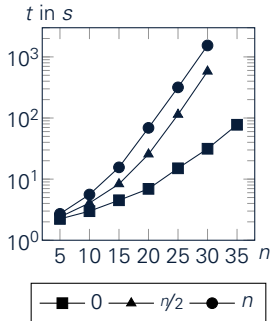
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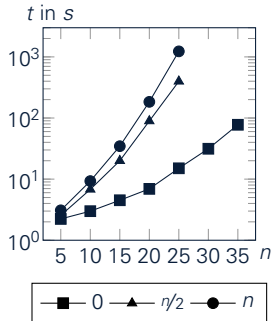
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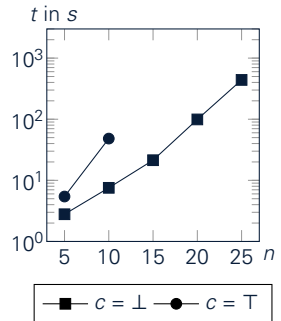
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Average execution times of JConHT for benchmark ontologies.

## References I

- Kühn, Thomas, Stephan Böhme, et al. (2015). "A combined formal model for relational context-dependent roles". In: *Proc. of the 8th ACM SIGPLAN Int. Conf. on Software Language Engineering (SLE 2015)*. (Pittsburgh, PA, USA). Ed. by Richard F. Paige, Davide Di Ruscio, and Markus Völter. ACM, pp. 113–124.
- Kühn, Thomas, Max Leuthäuser, et al. (2014). "A Metamodel Family for Role-Based Modeling and Programming Languages". In: *Proc. of the 7th Int. Conf. on Software Language Engineering (SLE 2014)*. (Västerås, Sweden). Ed. by Benoît Combemale et al. Vol. 8706. Lecture Notes in Computer Science. Springer-Verlag, pp. 141–160.
- Steimann, Friedrich (2000). "On the representation of roles in object-oriented and conceptual modelling". In: *Data & Knowledge Engineering* 35.1, pp. 83–106.