

$$9. \mathcal{L}\{t^2 e^{3t} \sin(2t)\}$$

$$= (-1)^2 \frac{d^2}{ds^2} (\mathcal{L}\{e^{3t} \sin(2t)\})$$

$$\mathcal{L}\{3^t \sin(2t)\} = \mathcal{L}\{\sin(2t)\} \Big|_{s \rightarrow s-3} = \frac{2}{s^2+4} \Big|_{s \rightarrow s-3} = \frac{2}{(s-3)^2+4}$$

$$= (-1)^2 \frac{d^2}{ds^2} \left(\frac{2}{s^2-6s+13} \right) \rightarrow \frac{d}{ds} \left(\frac{2}{s^2-6s+13} \right) = \frac{-2(2s-6)}{(s^2-6s+13)^2} = \frac{-4s+12}{(s^2-6s+13)^2}$$

$$= (-1)^2 \left(\frac{(s^2-6s+13)^2(-4) - (-4s+12)(4s^3-36s^2+124s-156)}{(s^2-6s+13)^4} \right)$$

$$= (-1) \left(\frac{12s^2 - 72s + 92}{(s^2-6s+13)^3} \right)$$

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$$10: \mathcal{L}\{ (t+1)^2 u(t-1) \} \quad a=1$$

$$e^s \mathcal{L}\{ t^2 \} = \frac{2e^{-s}}{s^3}$$

$$11: \mathcal{L}\{ e^{t-5} + u(t-5) \} \quad h=1$$

$$- \frac{d}{ds} \mathcal{L}\{ e^{t-5} u(t-5) \} \quad a=5$$

$$- \frac{d}{ds} e^{-5s} \mathcal{L}\{ e^t \} = - \frac{d}{ds}$$

$$= \frac{5s-4}{(s+1)^2} \cdot e^{-5s}$$

$$\frac{e^{-5s}}{s-1} = \frac{(s-1)(-s e^{-5s}) - e^{-5s}}{(s+1)}$$