

AI tutorial 5

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Question 1

Assume that $P = \neg(p1 \vee \neg p2)$. Write down the truth table for P. Give the list of interpretations I under which P is true. How many different interpretations are there that make P true?

p1	p2	$(p1 \vee \neg p2)$	$\neg(p1 \vee \neg p2)$	P
1	1	1	0	0
1	0	1	0	0
0	1	0	1	1
0	0	1	0	0

Question 2

Assume that $P = (((p1 \wedge \neg p2) \wedge p3) \Rightarrow p2)$. Write down the truth table for P. How many different interpretations make P true. Give the list of interpretations I under which P false.

p1	p2	p3	$(p1 \wedge \neg p2)$	$(p1 \wedge \neg p2) \wedge p3$	$(((p1 \wedge \neg p2) \wedge p3) \Rightarrow p2)$	p
1	1	1	0	0	1	1
1	1	0	0	0	1	1

1	0	1	1	1	0	0
0	1	1	0	0	0	0
0	0	1	0	0	1	1
0	1	0	0	0	0	0
1	0	1	1	1	0	0
1	0	0	1	0	0	0
0	0	0	0	0	1	1

This is wrong. Correcting the correct ones

Logical implication truth table

p1	p2	p1 => p2
1	1	1
1	0	0
0	1	1
0	0	1

Logical implication is ONLY false when 1 0 = 0

p1	p2	p3	(p1 ∧ ¬p2)	(p1 ∧ ¬p2) ∧ p3	(((p1 ∧ ¬p2) ∧ p3) ⇒ p2)	p
0	1	1	0	0	0	1

Question 3

A formula P is called **satisfiable** if there exists an interpretation I such that $I \models P$. Which of the following formulas are satisfiable? Check using truth tables

- $(\neg p_1 \wedge p_2)$

p_1	p_2	$\neg p_1$	$\neg p_1 \wedge p_2$
1	1	0	0
1	0	0	0
0	1	1	1
0	0	1	0

Thus this is satisfiable for $p_1 = 0$ and $p_2 = 1$

- $(p_1 \Rightarrow \neg p_1)$

p_1	$\neg p_1$	$p_1 \Rightarrow \neg p_1$
1	0	0
0	1	1

Thus this is satisfiable for $p_1 = 0$.

- $(p_1 \Leftrightarrow \neg p_1)$

p_1	$\neg p_1$	$p_1 \Leftrightarrow \neg p_1$
1	0	0
0	1	0

1	0	0
0	1	0

Not satisfiable.

• $(p_1 \wedge (\neg p_2 \vee \neg p_1))$

p1	p2	~p1	~p1	(~p2 V ~p1)	(p1 ∧ (~p2 v ¬p1))
1	1	0	0	0	0
1	0	0	1	1	1
0	1	1	0	1	0
0	0	1	1	1	0

Question 4

Consider a formula P with n atomic propositions. How many rows does the truth table for P have?

2^n rows. Because a proposition is either true or false (2).

Question 5

Consider $P = (((((\neg p_1 \wedge p_2) \vee p_3) \wedge p_4) \vee p_5) \Rightarrow p_1)$. Show without using truth tables that P is satisfiable.

Let $p_1 = 1$.

Then

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p1	anything	anything -> p1
1	1	1
0	1	1

Therefore as long as p1 is 1, anything on the left hand side will always be satisfiable as it either results in a 0 or a 1.

Question 6

Consider $P = (((((\neg p_1 \wedge p_2) \vee p_3) \wedge p_4) \vee p_5) \wedge (p_6 \wedge \neg p_6))$. Show without using truth tables that P is not satisfiable

$(p_6 \wedge \neg p_6)$ is never satisfiable. Therefore the left hand side is never satisfiable because it is an and statement.

Question 7