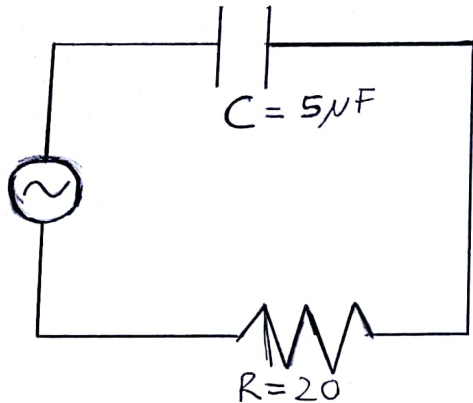


Tema 8: Circuitos de corriente alterna.

1

Problemas propuestos.

1) Circuito RC



Calcular la intensidad que circula por el circuito.

$$C = 5 \mu F = 5 \cdot 10^{-6} F$$

$$R = 200 \Omega$$

$$V = \underline{200\sqrt{2}} \text{ sen } 1000t \text{ Voltios.}$$

$$V = \underset{\downarrow}{V_0} \text{ sen } (\omega t + \theta) \quad \rightarrow \text{ Fase inicial}$$

$$-\bar{V} = V_e \angle \theta$$

$$V_e = \frac{V_0}{\sqrt{2}} = \frac{200\sqrt{2}}{\sqrt{2}} = 200$$

Como podemos observar no existe fase inicial.

$$\bar{V} = 200 \angle 0$$

- Ahora calculamos la impedancia (\bar{Z})

$$\bar{Z} = \bar{R} + \bar{X}_L + \bar{X}_C$$

$$\bar{Z} = R + j\left(L\omega - \frac{1}{C\omega}\right)$$

$$\bar{Z} = 200 + j\left(0 - \frac{1}{5 \cdot 10^{-6} \cdot 10^3}\right) = 200 - 200j$$

El valor obtenido lo pasamos a su forma polar. $\bar{Z} \angle \varphi$

$$Z = \sqrt{200^2 + (-200)^2} = 200\sqrt{2}$$

$$\bar{Z} = 200\sqrt{2} \angle -45^\circ$$

$$\varphi = \arctan \frac{-200}{200} = -45$$

$$\bar{I} = \frac{\bar{V}}{\bar{Z}} = \frac{200 \angle 0^\circ}{200\sqrt{2} \angle -45^\circ} = \frac{\sqrt{2}}{2} \angle 45^\circ \text{ A}$$

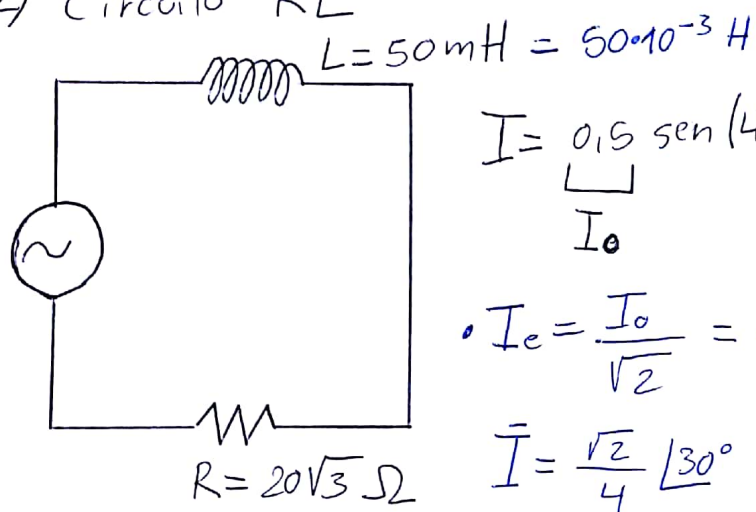
\downarrow
 I_e

$$I_e = \frac{I_0}{\sqrt{2}} \Rightarrow I_0 = \frac{\sqrt{2}}{2} \cdot \sqrt{2} = 1 \text{ A}$$

$$I = I_0 \sin(\omega t + \varphi)$$

$$I = 1 \sin(1000t + 45^\circ)$$

2) Circuito RL



$$I = \underbrace{0,5}_{I_0} \sin(400t + 30^\circ) \text{ A}$$

$$I_e = \frac{I_0}{\sqrt{2}} = \frac{0,5}{\sqrt{2}} = \frac{\sqrt{2}}{4} \text{ A}$$

$$\bar{I} = \frac{\sqrt{2}}{4} \angle 30^\circ$$

$$\bar{Z} = R + j(L\omega - \frac{1}{C\omega})$$

$$\bar{Z} = 20\sqrt{3} + j(50 \cdot 10^{-3} \cdot 400 - 0) = 20\sqrt{3} + 20j$$

Ahora lo pasamos a forma polar.

$$Z = \sqrt{(20\sqrt{3})^2 + 20^2} = 40$$

$$\bar{Z} = 40 \angle 30^\circ$$

$$\varphi = \arctg \frac{20}{20\sqrt{3}} = 30^\circ$$

$$\bar{I} = \frac{\bar{V}}{\bar{Z}} \Rightarrow \bar{V} = \bar{I} \cdot \bar{Z} = \frac{\sqrt{2}}{4} \angle 30^\circ \cdot 40 \angle 30^\circ = \underbrace{10\sqrt{2}} \angle 60^\circ$$

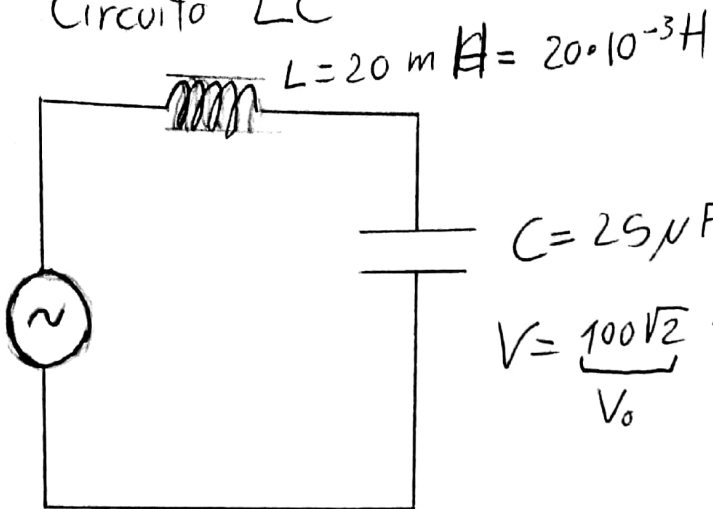
$$V = V_0 \sin(\omega t + \varphi)$$

$$V_e = \frac{V_0}{\sqrt{2}} \Rightarrow V_0 = 10\sqrt{2} \cdot \frac{V_e}{\sqrt{2}} = 20 \text{ V}$$

$$[V = 20 \sin(400t + 60^\circ) \text{ V}]$$

3)

Circuito LC



$$C = 25 \mu F = 25 \cdot 10^{-6}$$

$$V = \frac{100\sqrt{2}}{V_0} \sin(\underbrace{2000t}_w + 45^\circ) \text{ Voltios}$$

$$V_e = \frac{V_0}{\sqrt{2}} = \frac{100 \cdot \cancel{\sqrt{2}}}{\cancel{\sqrt{2}}} = 100$$

$$\vec{V} = V_e \angle \theta$$

$$\vec{V} = 100 \angle 45^\circ$$

$$\vec{Z} = R + j \left(L\omega - \frac{1}{C\omega} \right)$$

$$\vec{Z} = 0 + j \left(20 \cdot 10^{-3} \cdot 2000 - \frac{1}{25 \cdot 10^{-6} \cdot 2000} \right) = 20j$$

$$Z = \sqrt{0^2 + (20)^2} = 20$$

$$\varphi = \arctg \frac{20}{0} \Rightarrow 90^\circ$$

El ángulo es 90° ya que el único ángulo donde la tangente es infinita.

IMP En n° complejos no existe 270° , existe 90° o -90°

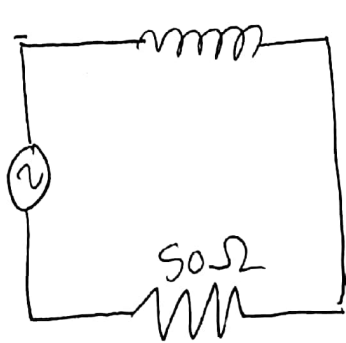
$$\text{En forma polar} \Rightarrow \vec{Z} = 20 \angle 90^\circ$$

$$\vec{I} = \frac{\vec{V}}{\vec{Z}} = \frac{100 \angle 45^\circ}{20 \angle 90^\circ} = \underbrace{5}_{I_e} \angle -45^\circ$$

$$I_e = \frac{I_0}{\sqrt{2}} \Rightarrow I_0 = 5\sqrt{2}$$

$$I = 5\sqrt{2} \sin(2000t - 45^\circ) A$$

4 Tema 8



Circuito RL

Datos

$$V = 200\sqrt{2} \sin(5000t + 45^\circ) V$$

La intensidad está desfasada 45° con respecto a la tensión

$$R = 50$$

$$V = \underbrace{200\sqrt{2}}_{V_0} \sin(\underbrace{5000}_{\omega} t + 45^\circ)$$

$$V_0$$

$$\omega = 5000 \text{ rad/s}$$

$$V_e = \frac{V_0}{\sqrt{2}} = \frac{200\sqrt{2}}{\sqrt{2}} = 200$$

$$\vec{V} = 200 \angle 45^\circ$$

Calculamos la impedancia.

$$\vec{Z} = R + j(L\omega - \frac{1}{C\omega}) = 50 + j(L \cdot 5000) = 50 + 5000Lj$$

$$\varphi = \arctg \frac{5000L}{50}$$

$$\vec{I} = \frac{\vec{V}}{\vec{Z}} = \frac{200 \angle 45^\circ}{\vec{Z}}$$

$$45^\circ = \arctg \frac{5000L}{50}$$

Sabemos que \vec{I} está desfasado 45° con V , así pues

$$\theta = 0^\circ$$

$$\frac{\arctg 45 \cdot 50}{5000} = L$$

$$L = 0,01$$

Para que $\theta = 0^\circ \Rightarrow \varphi = 45^\circ$

$$\bar{Z} = 50 + 5000Lj = \underbrace{50 + 50j}$$

$$L = 0,01 H \nearrow$$

$$\Downarrow$$

$$Z = \sqrt{50^2 + 50^2} = 50\sqrt{2}$$

$$\bar{I} = \frac{200 \angle 45^\circ}{50\sqrt{2} \angle 45^\circ} = 2\sqrt{2} \angle 0^\circ$$

$$I_e = \frac{V_o}{\sqrt{2}}$$

$$I_o = 2\sqrt{2} \cdot \sqrt{2} = 4$$

$$I = 4 \sin(5000t + 0^\circ)$$

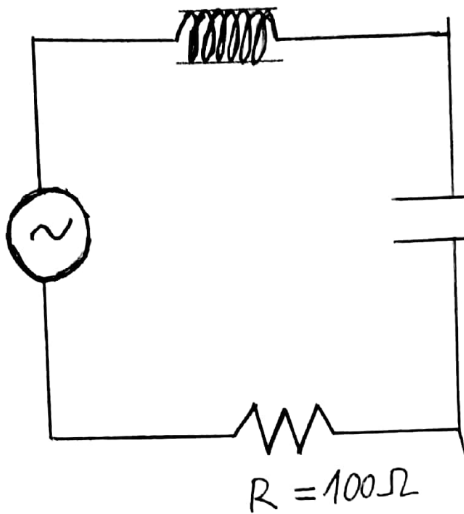
5)

Circuito RLC

$$L = 190 \text{ mH} = 190 \cdot 10^{-3} \text{ H}$$

$$I = 200 \sqrt{2} \sin(100\pi t + 30^\circ) \text{ A}$$

$$I_e = \frac{I_0}{\sqrt{2}} = \frac{\sqrt{2}}{\sqrt{2}} = 1 \text{ A}$$



$$C = 20 \mu\text{F} = 20 \cdot 10^{-6} \text{ F}$$

$$\bar{I} = I_e \angle \varphi = 1 \angle 30^\circ$$

a) $\bar{Z} = ?$

$$\bar{Z} = R + j\left(L\omega - \frac{1}{C\omega}\right) = 100 + j\left(0,19 \cdot 100\pi - \frac{1}{20 \cdot 10^{-6} \cdot 100\pi}\right) =$$

$$= 100 - j \cdot 99,46$$

Ahora lo pasamos a forma polar

$$Z = \sqrt{100^2 + (99,46)^2} = 141$$

$$\varphi = \arctan \frac{-99,46}{100} = -44,84 = -45^\circ$$

$$\bar{Z} = 141 \angle -45^\circ \Omega$$

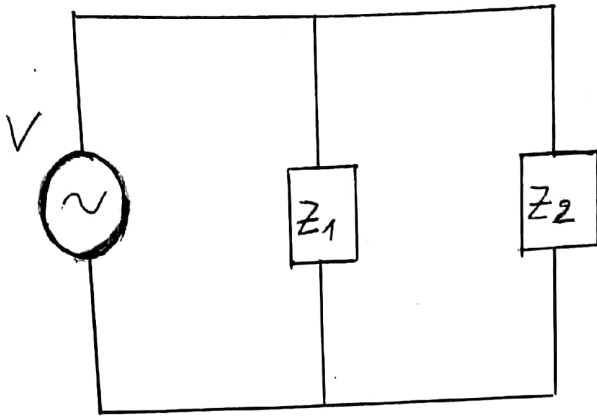
b)

$$\bar{I} = \frac{\bar{V}}{\bar{Z}} \Rightarrow \bar{V} = \bar{I} \cdot \bar{Z} = 1 \angle 30^\circ \cdot 141 \angle -45^\circ = \underbrace{141 \angle -15^\circ}_{V_e}$$

$$V_e = \frac{V_0}{\sqrt{2}} \Rightarrow V_0 = 141\sqrt{2}$$

$$V = 141\sqrt{2} \sin(100\pi t - 15^\circ) \text{ Voltios}$$

6)



$$\bar{V} = 220 \angle 0^\circ \text{ V}$$

$$\bar{Z}_1 = 40 \angle 60^\circ \Omega$$

$$\bar{Z}_2 = 30 \angle -30^\circ \Omega$$

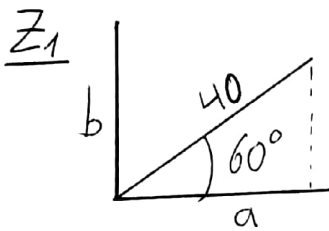
a) Z_e

$$\frac{1}{Z_e} = \frac{1}{Z_1} + \frac{1}{Z_2} \Rightarrow \frac{1}{Z_e} = \frac{Z_2 + Z_1}{Z_1 \cdot Z_2} \Rightarrow Z_e = \frac{Z_1 \cdot Z_2}{Z_1 + Z_2}$$

$$Z_e = \frac{40 \angle 60^\circ \cdot 30 \angle -30^\circ}{40 \angle 60^\circ + 30 \angle -30^\circ} = \frac{1200 \angle 30^\circ}{45,98 + 19,64j} = \frac{1200 \angle 30^\circ}{50 \angle 23,13^\circ} = 24 \angle 6,87^\circ$$

Lo pasamos a su forma polar

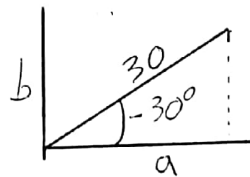
1- Lo pasamos a forma binómica



$$a = 40 \cdot \cos 60^\circ = 20$$

$$b = 40 \cdot \sin 60^\circ = 20\sqrt{3}$$

$$\bar{Z}_1 = 20 + 20\sqrt{3}j$$

 Z_2 

$$a = 30 \cos -30 = 15\sqrt{3}$$

$$b = 30 \sin -30 = -15$$

$$\bar{Z}_2 = 15\sqrt{3} - 15j$$

$$\bar{Z}_e = 45,98 + 19,64j$$

2-

$$Z_e = \sqrt{45,98^2 + 19,64^2} = 50$$

$$\varphi = \arctan \frac{19,64}{45,98} = 23,13$$

$$\bar{Z}_e = 50 \angle 23,13^\circ$$

b) Intensidad por cada rama.

$$\bar{I} = \frac{\bar{V}}{\bar{Z}}$$

$$[\bar{I}_1 = \frac{\bar{V}}{\bar{Z}_1} = \frac{220 \angle 0^\circ}{40 \angle 60^\circ} = 5,5 \angle -60^\circ]$$

$$[\bar{I}_2 = \frac{\bar{V}}{\bar{Z}_2} = \frac{220 \angle 0^\circ}{30 \angle -30^\circ} = 7,3 \angle 30^\circ]$$

c) Potencia activa de la fuente (P_{Ac})

$$\bar{I} = \frac{\bar{V}}{\bar{Z}} = \frac{220 \angle 0^\circ}{24 \angle 6,87^\circ} = 9,17 \angle -6,87^\circ$$

I_e

$$[V_e = \frac{V_o}{\sqrt{2}} \Rightarrow V_o = 9,17 \sqrt{2}] \text{ Innecesario.}$$

$$P = I_e^2 R$$

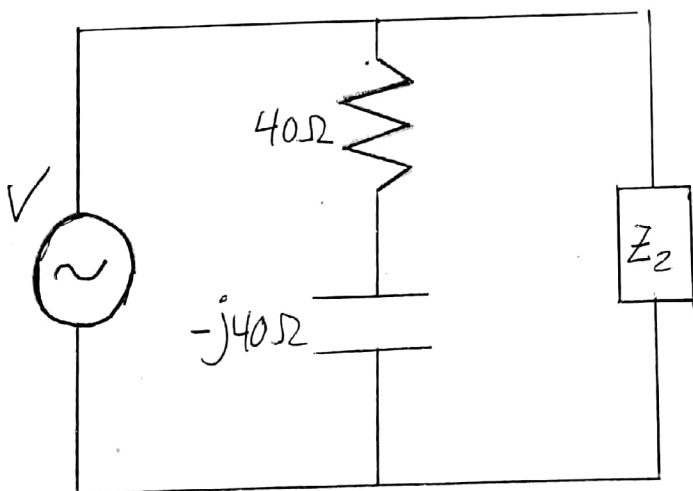
↳ Potencia disipada en una resistencia.

$$P_{Ac} = I_e V_e \cos \varphi$$

↙ P_{Activa}

$$[P_{Ac} = 9,17 \cdot 220 \cos 6,87^\circ = 2002,92 = 2002 \text{ W}]$$

7



$$V = 100 \angle 30^\circ \text{ V}$$

$$I_t = 2,15 \angle 47,6^\circ \text{ A}$$

• Empezamos calculando \bar{Z}_1

$$\bar{Z}_1 = R + j(L\omega - \frac{1}{C\omega}) = 40 - j40$$

Ahora lo pasamos a forma polar

$$\bar{Z}_1 = \sqrt{40^2 + (-40)^2} = 40\sqrt{2} \quad \varphi = \arctg \frac{-40}{40} = -45^\circ \quad \left. \vphantom{\bar{Z}_1} \right\} \bar{Z}_1 = 40\sqrt{2} \angle -45^\circ$$

Ahora calculamos I_1

$$I_1 = \frac{\bar{V}}{\bar{Z}_1} = \frac{100 \angle 30^\circ}{40\sqrt{2} \angle -45^\circ} = \frac{5\sqrt{2}}{4} \angle 75^\circ$$

$$\underline{I}_2 = \underline{I}_+ + \underline{I}_1 = 2,15 \angle 47,6^\circ - \frac{5\sqrt{2}}{4} \angle 75^\circ = 1,45 + 1,59j - (0,46 + 1,71j) = 0,99 - 0,12j$$

Para efectuar esta operación lo pasamos a forma binómica

$$\begin{aligned} \underline{I}_+ \\ a = 2,15 \cos 47,6^\circ = 1,45 \\ b = 2,15 \sin 47,6^\circ = 1,59 \end{aligned} \left. \vphantom{\begin{aligned} a = 2,15 \cos 47,6^\circ = 1,45 \\ b = 2,15 \sin 47,6^\circ = 1,59 \end{aligned}} \right\} \underline{I}_+ = 1,45 + 1,59j$$

$$\begin{aligned} \underline{I}_1 \\ a = \frac{5\sqrt{2}}{4} \cos 75^\circ = 0,46 \\ b = \frac{5\sqrt{2}}{4} \sin 75^\circ = 1,71 \end{aligned} \left. \vphantom{\begin{aligned} a = \frac{5\sqrt{2}}{4} \cos 75^\circ = 0,46 \\ b = \frac{5\sqrt{2}}{4} \sin 75^\circ = 1,71 \end{aligned}} \right\} \underline{I}_1 = 0,46 + 1,71j$$

$$\underline{I}_2 = \sqrt{0,99^2 + (-0,12)^2} = 1$$

$$\varphi = \arctg \frac{-0,12}{0,99} = -6,9$$

$$\underline{\bar{Z}}_2 = \frac{\underline{V}}{\underline{I}_2} = \frac{100 \angle 30^\circ}{1 \angle -6,9^\circ} =$$

$$= 100 \angle 36,9^\circ$$

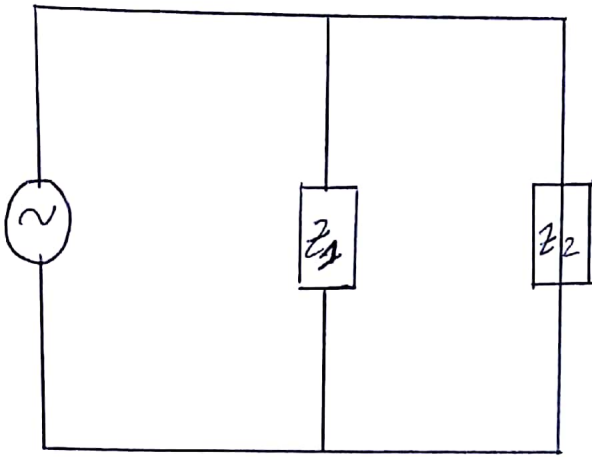
$$a = 100 \cos 36,9^\circ = 80$$

$$b = 100 \sin 36,9^\circ = 60$$

$$\underline{\bar{Z}}_2 = 80 + 60j \Omega$$

$$8) \quad V_e = 220 \text{ V} \quad \gamma = 50 \text{ Hz}$$

$$\underline{\bar{Z}}_1 = 200 \angle 60^\circ \Omega$$



Datos

$$\bar{V} = 100 \angle 45^\circ \text{ V}$$

$$\bar{Z}_1 = 40\sqrt{3} + j40 \Omega$$

$$\bar{Z}_2 = 50 - j50\sqrt{3} \Omega$$

Calcula la potencia aparente, activa y reactiva de cada una de las ramas del circuito.

$$|\bar{S}| = P_{\text{aparente}} = I_e \cdot V_e$$

$$P = P_{\text{activa}} = I_e V_e \cos \phi$$

$$Q = P_{\text{reactiva}} = I_e V_e \sin \phi$$

Pasamos las impedancias a forma polar.

$$|\bar{S}| = P + jQ$$

$$\bullet \bar{Z}_1 = 40\sqrt{3} + j40$$

$$\bullet \bar{Z}_2 = 50 - j50\sqrt{3}$$

$$Z_1 = \sqrt{(40\sqrt{3})^2 + (40)^2} = 80$$

$$Z_2 = \sqrt{50^2 + (-50\sqrt{3})^2} = 100$$

$$\phi = \arctan \frac{40}{40\sqrt{3}} = 30^\circ$$

$$\phi = \arctan \frac{-50\sqrt{3}}{50} = -60^\circ$$

$$[\bar{Z}_1 = 80 \angle 30^\circ]$$

$$[\bar{Z}_2 = 100 \angle -60^\circ]$$

Rama 1

Primero calculamos la intensidad (\bar{I}_1) que circula por esta rama.

$$\bar{I}_1 = \frac{\bar{V}}{\bar{Z}_1} = \frac{100 \angle 45^\circ}{80 \angle 30^\circ} = 1,25 \angle 15^\circ \text{ A}$$

Una vez calculada ya podemos calcular lo que nos piden.

$$P_{\text{aparente}} = I_e V_e = 1,25 \cdot 100 = 125 \text{ W}$$

$$P_{\text{activa}} = I_e V_e \cos \varphi = 1,25 \cdot 100 \cdot \cos 30^\circ = 108,25 \text{ W}$$

$$P_{\text{reactiva}} = I_e V_e \sin \varphi = 1,25 \cdot 100 \cdot \sin 30^\circ = 62,5 \text{ W}$$

Ahora pasamos a la rama 2.

Rama 2

Al igual que en la rama 1 calculamos la intensidad que circula.

$$\bar{I}_2 = \frac{\bar{V}}{\bar{Z}_2} = \frac{100 \angle 45^\circ}{100 \angle -60^\circ} = 1 \angle 105^\circ \Leftrightarrow 1 \angle 15^\circ$$

$$P_{\text{aparente}} = I_e \cdot V_e = 1 \cdot 100 = 100 \text{ W}$$

$$P_{\text{activa}} = I_e V_e \cdot \cos \varphi = 1 \cdot 100 \cdot \cos -60 = 50 \text{ W}$$

$$P_{\text{reactiva}} = I_e V_e \sin \varphi = 1 \cdot 100 \cdot \sin -60 = -50\sqrt{3} = -86,6 \text{ W}$$

Ahora que hemos calculado los valores tanto de la rama 1 y la rama 2, pasamos a calcular los valores de la fuente.

Fuente.

Como las impedancias están en paralelo lo que tenemos que hacer es calcular la impedancia total (\bar{Z}_e).

$$\frac{1}{\bar{Z}_e} = \frac{1}{\bar{Z}_1} + \frac{1}{\bar{Z}_2} \Rightarrow \bar{Z}_e = \frac{\bar{Z}_1 \bar{Z}_2}{\bar{Z}_1 + \bar{Z}_2}$$

$$\bar{Z}_e = \frac{80 \angle 30^\circ \cdot 100 \angle -60^\circ}{(40\sqrt{3} + j40) + (50 - j(50\sqrt{3}))} = \frac{8000 \angle -30^\circ}{119 - 46,6j} = \frac{8000 \angle -30^\circ}{128,8 \angle -21^\circ} = 62,5 \angle -9^\circ$$

$$Z_e = \sqrt{119^2 + (-46,6)^2} = 128,8$$

$$\varphi = \arctg \frac{-46,6}{119} = -21^\circ$$

$$I_e = \frac{\bar{V}}{\bar{Z}_e} = \frac{100 \angle 45^\circ}{62,5 \angle -9} = 1,6 \angle 54^\circ \text{ A}$$

$$P_{\text{aparente}} = I_e \cdot V_e = 1,6 \cdot 100 = 160 \text{ W}$$

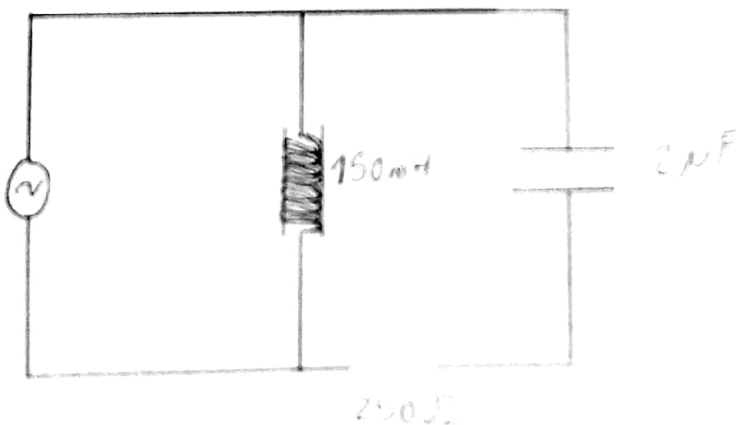
$$P_{\text{activa}} = I_e V_e \cos \varphi = 1,6 \cdot 100 \cos -9 = 158 \text{ W}$$

$$P_{\text{reactiva}} = I_e V_e \sin \varphi = 1,6 \cdot 100 \cdot \sin -9 = -25, \text{ W}$$

Yá que tenemos todos los datos los organizamos de forma más clara en una tabla

	Rama 1	Rama 2	Fuente
$S(P_{\text{ap}})$	125	100	160
$P(P_{\text{ad}})$	108,25	50	158
$Q(P_{\text{react}})$	62,5	-86,6	-25

10



Datos

$$L = 150 \text{ mH} = 0,15 \text{ H}$$

$$R = 250 \Omega$$

$$C = 2 \mu\text{F} = 2 \cdot 10^{-6} \text{ F}$$

$$V = \underbrace{300\sqrt{2}}_{V_0} \sin(2000t + 60^\circ)$$

$$V_e = \frac{V_0}{\sqrt{2}} = \frac{300\sqrt{2}}{\sqrt{2}} = 300$$

$$\bar{V} = 300 \angle 60^\circ$$

a) Las corrientes (I) que circulan por la bobina y por el condensador.

$$\bar{I}_1 = \frac{\bar{V}}{\bar{Z}_1} = \frac{300 \angle 60^\circ}{300 \angle 90^\circ} = 1 \angle -30^\circ \Rightarrow I_e = 1 \quad I_e = \frac{I_o}{\sqrt{2}} \Rightarrow I_o = 1 \cdot \sqrt{2}$$

Calculamos \bar{Z}_1 .

$$\bar{Z}_1 = \underline{0} + j(L\omega - 0) = jL\omega = j(0,15 \cdot 2000) = 300j$$

ya que no hay resistencia.

Ahora lo pasamos a la forma polar

$$\left. \begin{aligned} Z_1 &= \sqrt{0^2 + 300^2} = 300 \\ \varphi &= \arctg \frac{300}{0} = 90^\circ \end{aligned} \right\} [\bar{Z}_1 = 300 \angle 90^\circ]$$

$$I_2 = \frac{\bar{V}}{\bar{Z}_2} = \frac{300 \angle 60^\circ}{250\sqrt{2} \angle -45^\circ} = \frac{1,2}{\sqrt{2}} \angle 105^\circ = \frac{1,2}{\sqrt{2}} \angle 15^\circ$$

• Calculamos \bar{Z}_2

$$\bar{Z}_2 = 250 + j\left(0 - \frac{1}{\omega C}\right) = 250 + j\left(-\frac{1}{2 \cdot 10^{-6} \cdot 2000}\right) = 250 - 250j \Omega$$

Lo pasamos a la forma polar.

$$\left. \begin{aligned} Z_2 &= \sqrt{250^2 + (-250)^2} = 250\sqrt{2} \\ \varphi &= \arctg \frac{-250}{250} = -45^\circ \end{aligned} \right\} \bar{Z}_2 = 250\sqrt{2} \angle -45^\circ$$

$$\varphi = \arctg \frac{-250}{250} = -45^\circ$$

$$I_e = \frac{1,2}{\sqrt{2}}$$

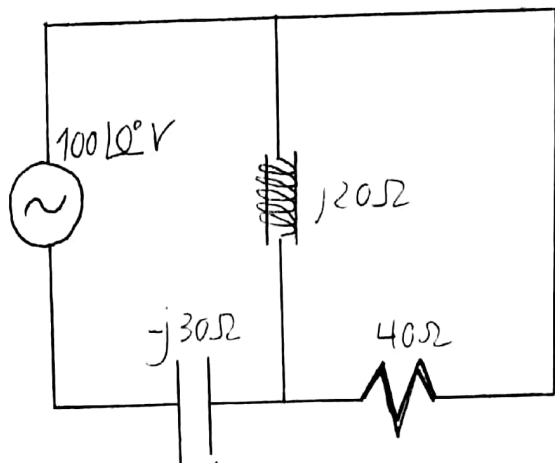
$$I_e = \frac{I_o}{\sqrt{2}} \Rightarrow I_o = \frac{1,2 \cdot \sqrt{2}}{\sqrt{2}} = 1,2 A$$

$$I_2 = 1,2 \sin(2000t + 15^\circ) A.$$

b) La potencia disipada en la resistencia.

$$P = I_e^2 R = \left(\frac{1,2}{\sqrt{2}}\right)^2 \cdot 250 = 180 \text{ W}$$

11)



Datos

a) La impedancia equivalente.

$$\bar{Z}_1 = 0 + (-j30) \parallel (j20) = \bar{Z}_1 = 0 - j10$$

$$\begin{aligned} \bar{Z}_1 \cdot \sqrt{(-10)^2} &= 100 \\ \varphi &= \arctan \frac{-10}{0} = 90^\circ \end{aligned} \left\{ \begin{aligned} \bar{Z}_1 &= 100 \angle 90^\circ \end{aligned} \right.$$

$$\bar{Z}_2 = 40 + j20$$

$$\begin{aligned} \bar{Z}_2 &= \sqrt{40^2 + 20^2} = 20\sqrt{5} \\ \varphi &= \arctan \frac{20}{40} = 27^\circ \text{ ó } 26,6^\circ \end{aligned} \left\{ \begin{aligned} \bar{Z}_2 &= 20\sqrt{5} \angle 26,6^\circ \end{aligned} \right.$$

$$\bar{Z}_e = \frac{\bar{Z}_1 \cdot \bar{Z}_2}{\bar{Z}_1 + \bar{Z}_2} = \frac{100 \angle 90^\circ \cdot 20\sqrt{5} \angle 26,6^\circ}{(-j10) + (40 + j20)} = \frac{4472,14 \angle 26,6^\circ}{40 + j10} =$$

$$\bar{Z} = \sqrt{40^2 + 10^2} = 10\sqrt{17}$$

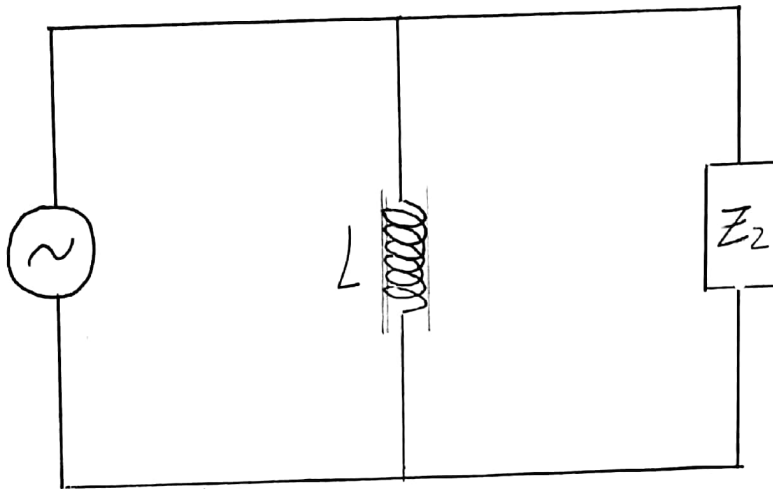
$$\varphi = \frac{10}{40} = 14^\circ$$

$$= \frac{4472,14 \angle 26,6^\circ}{10\sqrt{17} \angle 14^\circ}$$

b) La potencia disipada en la resistencia.

$$P = I_e^2 R$$

12)



Datos

$$V = 220\sqrt{2} \sin(250t - 30^\circ) V$$

$$L = 80 \text{ mH}$$

$$\bar{Z}_2 = 40 \angle -60^\circ \Omega$$

a) La impedancia equivalente (\bar{Z}_e).

• Como tenemos \bar{Z}_2 lo que haremos será calcular \bar{Z}_1

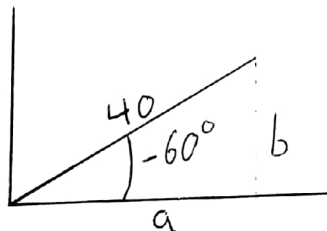
$$\bar{Z} = R + j(L\omega - \frac{1}{C\omega}) \Rightarrow \bar{Z}_1 = 0 + j(80 \cdot 10^{-3} \cdot 250 - 0) = 20j$$

$$Z = \sqrt{0^2 + 20^2} = 20$$

$$\varphi = \arctan \frac{20}{0} = 90^\circ \quad \left. \vphantom{\begin{matrix} Z = \sqrt{0^2 + 20^2} = 20 \\ \varphi = \arctan \frac{20}{0} = 90^\circ \end{matrix}} \right\} \bar{Z}_1 = 20 \angle 90^\circ \Omega$$

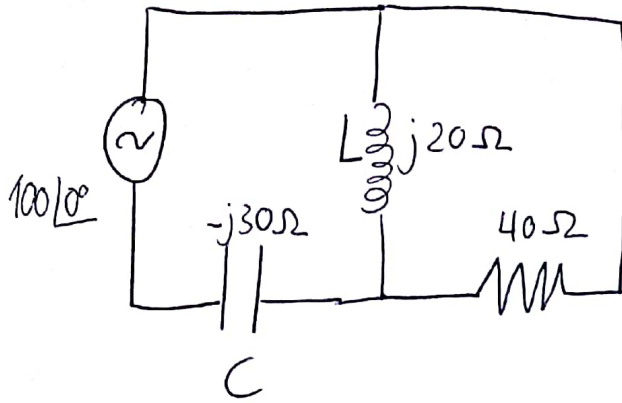
Ya que tenemos \bar{Z}_2 en forma polar lo pasaremos a forma binómica para efectuar la suma a la hora de calcular \bar{Z}_e

$$\bar{Z}_2 = 40 \angle -60^\circ$$



$$\left. \begin{matrix} \cos \alpha = \frac{a}{40} \\ \sin \alpha = \frac{b}{40} \end{matrix} \right\} \begin{matrix} a = 40 \cos -60 = 20 \\ b = 40 \sin -60 = -20\sqrt{3} \end{matrix} \Rightarrow$$

$$\Rightarrow \bar{Z}_2 = 20 - 20\sqrt{3}j \Omega$$



Datos

$$V = 100 \angle 0^\circ$$

$$R = 40 \Omega$$

$$\bar{Z}_L = 20j$$

$$\bar{Z}_C = -30j$$

a) \bar{Z}_e ?

Primero calculamos la impedancia entre R y L

$$\bar{Z}_{RL} = \frac{\bar{Z}_R \cdot \bar{Z}_L}{\bar{Z}_R + \bar{Z}_L} = \frac{40 \angle 0^\circ \cdot 20 \angle 90^\circ}{40 + 20j} = \frac{800 \angle 90^\circ}{20\sqrt{5} \angle 26,57^\circ} = 8\sqrt{5} \angle 63,43^\circ$$

$$\bar{Z}_C = -40 - 40j$$

$$\bar{Z}_L = 20j$$

$$\left. \begin{array}{l} Z = 20 \\ \varphi = 90^\circ \end{array} \right\} 20 \angle 90^\circ$$

$$Z = 20\sqrt{5}$$

$$\varphi = \arctan \frac{20}{40} = 26,57$$

Ahora sumamos \bar{Z}_C con \bar{Z}_{RL} para calcular \bar{Z}_e

$$\bar{Z}_e = \bar{Z}_{RL} + \bar{Z}_C = 8 + 16j + (-30j) = 8 - 14j$$

$$\left. \begin{array}{l} \bar{Z}_e = \sqrt{8^2 + (-14)^2} = 16,125 \\ \varphi = \arctan \frac{-14}{8} = -60,26^\circ \end{array} \right\} \Rightarrow$$

$$\bar{Z}_{RL} = 8\sqrt{5} \angle 63,43$$

$$a = 8\sqrt{5} \cos 63,43 = 8$$

$$b = 8\sqrt{5} \sin 63,43 = 16$$

$$8 + 16j = \bar{Z}_{RL}$$

$$\bar{Z}_e = 16,125 \angle -60,26^\circ$$

$$[\bar{Z}_e = 16,125 \angle -60,26^\circ]$$

\bar{Z}_C

b) Potencia disipada en la resistencia

$$P_R = I_e^2 \cdot R$$

Para calcular la potencia que disipa la resistencia
tenemos que calcular I_2

$$I_2 = \frac{\bar{V}}{\bar{Z}_{RL}} = \frac{100 \angle 0}{815 \angle 63,43} = 5,59 \angle -63,43$$

$$P_R = 5,59^2 \cdot 40 =$$

$$2,77 \angle 0 = \frac{100 \angle 0}{36,10}$$

$$2,77 = I_e$$

$$36,10$$

Ahora que ya tenemos calculado \bar{Z}_1 y \bar{Z}_2 en ambas formas (polar y binómica) procedemos a calcular \bar{Z}_e

$$\frac{1}{\bar{Z}_e} = \frac{1}{\bar{Z}_1} + \frac{1}{\bar{Z}_2} \Rightarrow \frac{1}{\bar{Z}_e} = \frac{\bar{Z}_1 + \bar{Z}_2}{\bar{Z}_1 \cdot \bar{Z}_2} \Rightarrow \bar{Z}_e = \frac{\bar{Z}_1 \cdot \bar{Z}_2}{\bar{Z}_1 + \bar{Z}_2}$$

$$[\bar{Z}_e = \frac{20 \angle 90^\circ \cdot 40 \angle -60^\circ}{20j + (20 - 20\sqrt{3}j)} = \frac{800 \angle 30^\circ}{20 - 14,64j} = \frac{800 \angle 30^\circ}{24,79 \angle -36,2^\circ} = 32,27 \angle 66,2^\circ]$$

$$\begin{aligned} \bar{Z} &= \sqrt{20^2 + (-14,64)^2} = 24,79 \\ \varphi &= \arctan \frac{-14,64}{20} = -36,2^\circ \end{aligned} \left. \vphantom{\begin{aligned} \bar{Z} &= \sqrt{20^2 + (-14,64)^2} = 24,79 \\ \varphi &= \arctan \frac{-14,64}{20} = -36,2^\circ \end{aligned}} \right\} 24,79 \angle -36,2^\circ$$

b) La potencia disipada en la impedancia \bar{Z}_2

Para calcular la potencia que ~~pasa~~ disipa \bar{Z}_2 tenemos que calcular la intensidad primero.

$$I_2 = \frac{\bar{V}}{\bar{Z}_2} = \frac{220 \angle 0^\circ}{40 \angle -60^\circ} = \frac{11}{2} \angle 60^\circ$$

$\hookrightarrow I_e$

$$V_0 = 220\sqrt{2}$$

$$V_e = \frac{V_0}{\sqrt{2}} = \frac{220\sqrt{2}}{\sqrt{2}} = 220 \text{ V}$$

$$P = I_e^2 \cdot R = \left(\frac{11}{2}\right)^2 \cdot 20 = 605 \text{ W}$$

$$\bar{Z}_2 = 40 \angle -60^\circ \Rightarrow \underbrace{20 - 20\sqrt{3}j}_R = \bar{Z}_2$$