

4)

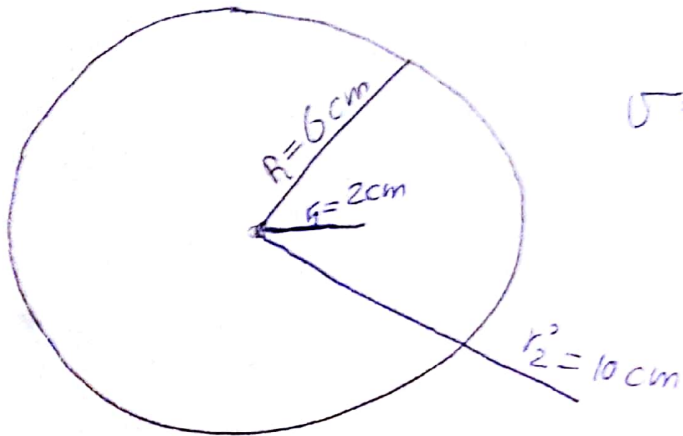
a)

$$\sigma = 9 \text{ nC/m}^2$$

$$\sigma = \frac{dq}{dS}$$

$$\sigma = \frac{Q}{S} \quad Q = \sigma S = 9 \cdot 10^{-9} \times 4\pi (0,06)^2$$

$$Q = 4,07 \cdot 10^{-10} \text{ C}$$

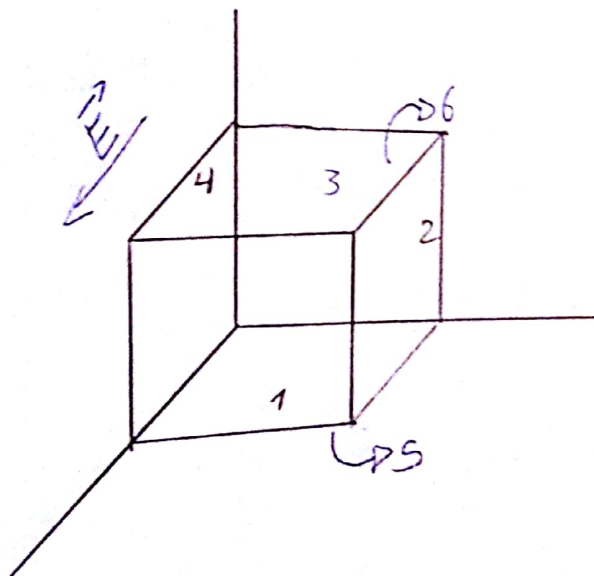


b) $r_1 = 2 \text{ cm} \Rightarrow \vec{E} = 0 \quad V = k \frac{Q}{R}$

$$r_2 = 10 \text{ cm} \Rightarrow \vec{E} = k \frac{Q}{r_2^2} = 9 \cdot 10^9 \cdot \frac{4,07 \cdot 10^{-10}}{(0,1)^2} = 3,66 \text{ V/m}$$

$$V = k \frac{Q}{r_2}$$

1)



$$\Phi = \vec{E} \cdot \vec{S} = ES \cos \alpha$$

$$\Phi_1 = ES = E_0 \cdot a^2$$

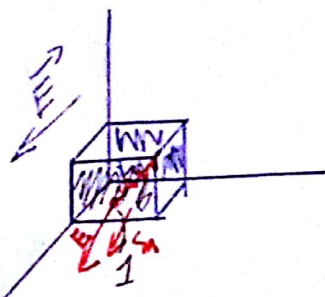
$$\Phi_2 = 0$$

$$\Phi_3 = -E_0 \cdot a^2$$

$$\Phi_4 = 0$$

$$\Phi_5 = 0$$

$$\Phi_6 = 0$$



3) a)

$$\sigma = 3 \text{ C/m}^2$$

$$\vec{F} = q \cdot \vec{E}$$

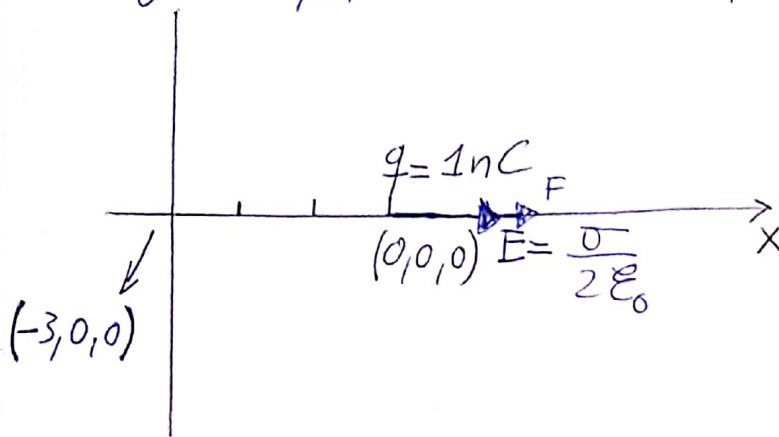
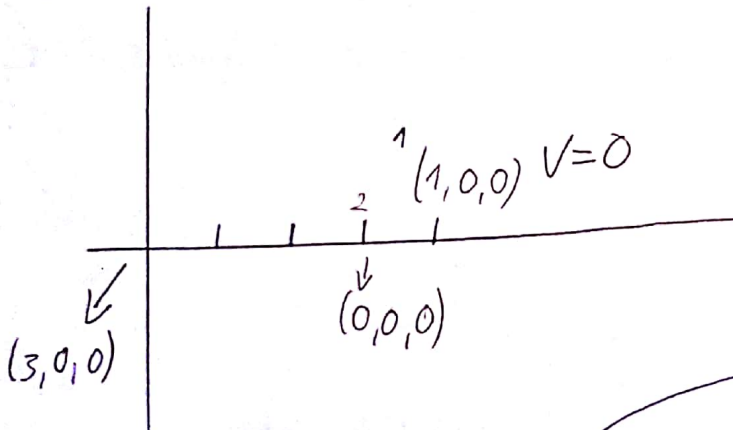
$$\Downarrow$$

$$F = 1 \cdot 10^{-9} \cdot \frac{\sigma}{2 \epsilon_0} = 54 \pi \text{ N}$$

$$k = \frac{1}{4 \pi \epsilon_0}$$

$$\vec{F} = 54 \pi \vec{i}$$

$$\epsilon_0 = \frac{1}{4 \pi k}$$

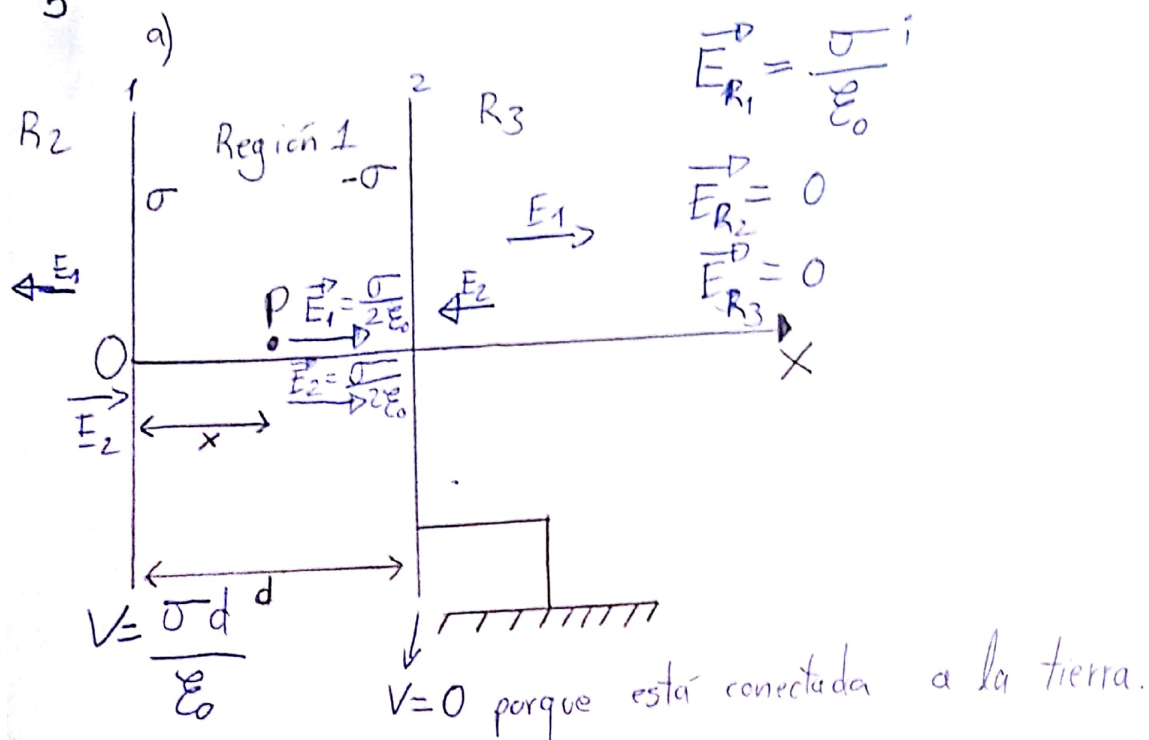
b) $U = ?$ $U = q \cdot V$ 

$$\int_1^2 dV = \int_1^2 -\vec{E} \cdot d\vec{r}$$

$$V(0, 0, 0) - V(1, 0, 0) = -\frac{\sigma}{2 \epsilon_0} \int_{(1, 0, 0)}^{(0, 0, 0)} dx =$$

$$= -\frac{\sigma}{2 \epsilon_0} (0 - 1) = \left(\frac{\sigma}{2 \epsilon_0} \right)$$

$$U = 1 \cdot 10^{-9} \cdot \frac{\sigma}{2 \epsilon_0} =$$



b) V en todos los puntos.

$$\int dV = -\int \vec{E} \cdot d\vec{r}$$

$$V = -\int \frac{\sigma}{\epsilon_0} dx = -\frac{\sigma}{\epsilon_0} x + C$$

$$V_{R1} = -\frac{\sigma}{\epsilon_0} x + C_1$$

$$V_{R1} = -\frac{\sigma}{\epsilon_0} x + C_1 = -\frac{\sigma}{\epsilon_0} x + \frac{\sigma}{\epsilon_0} d$$

$$V_{R1} = 0 = -\frac{\sigma}{\epsilon_0} d + C_1$$

$$[C_1 = \frac{\sigma}{\epsilon_0} d]$$

$$V_{R1} = \frac{\sigma}{\epsilon_0} (d - x)$$

Si no hay campo el potencial es constante.

$$V_{R2} = C_2 = 0$$

$$d_{R2} V = -\vec{E} \cdot d\vec{r}$$

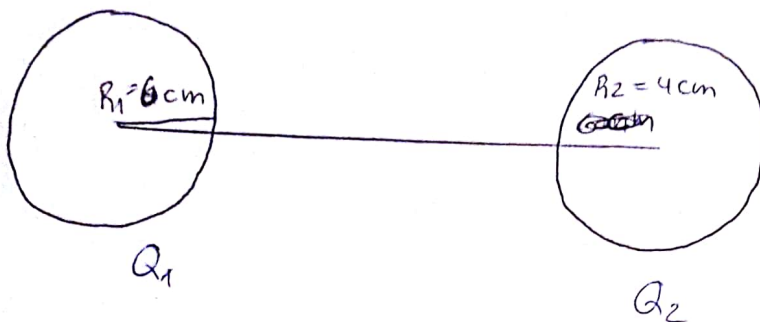
$$dV = 0$$

$$V_{R2} = \text{cte} = C_2 = \frac{\sigma}{\epsilon_0} \cdot d$$

Si no ponen límites de integración ponemos la constante de integración.

6)

$$Q = 20 \mu\text{C}$$



$$Q_T = Q_1 + Q_2$$

$$E_1 = K \cdot \frac{Q_1}{R_1^2} = 10$$

$$E_2 = K \cdot \frac{Q_2}{R_2^2}$$

$$V_1 = K \frac{Q_1}{R_1}$$

$$V_2 = K \frac{Q_2}{R_2}$$

$$V_1 = V_2$$

$$K \cdot \frac{Q_1}{R_1} = K \cdot \frac{Q_2}{R_2}$$

$$Q_1 = \frac{Q_2 R_1}{R_2}$$

$$Q_1 + Q_2 = 20 \cdot 10^{-6}$$

$$Q_1 = Q_2 \frac{R_1}{R_2}$$

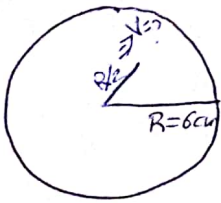
$$Q_2 \frac{R_1}{R_2} + Q_2 = 20 \cdot 10^{-6}$$

$$Q_2 = 8 \cdot 10^{-6} \text{ C}$$

$$Q_1 = 12 \cdot 10^{-6} \text{ C}$$

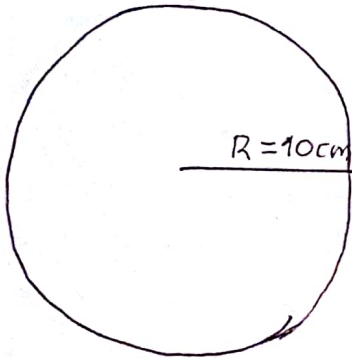
6) b

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El potencial es el mismo que en la superficie de ambas esferas, y a que como no hay cargas dentro de la esfera el V es constante.

g)



a) $V = 500 \text{ V}$ $R = 10 \text{ cm} \Rightarrow 0,01 \text{ m}$

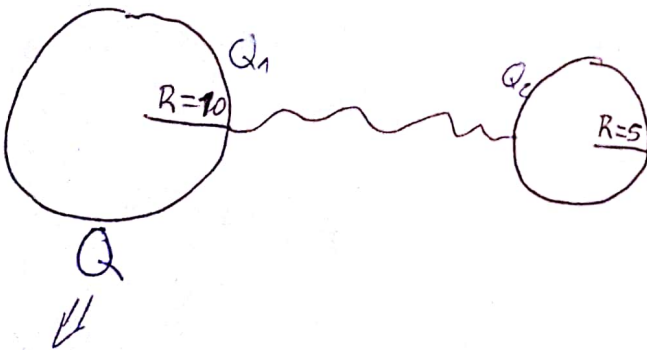
$$V = k \cdot \frac{Q}{R}$$

$$500 = 90 \cdot 10^9 \cdot \frac{Q}{0,01^2}$$

$$\frac{500 \cdot (0,01)^2}{90 \cdot 10^9} = Q$$

$$Q = 56 \cdot 10^{-9} \text{ C}$$

b)



$$Q = Q_1 + Q_2$$

$$V_1 = k \frac{Q_1}{R_1}$$

$$V_2 = k \frac{Q_2}{R_2}$$

$$V_1 = V_2$$

$$\cancel{k} \frac{Q_1}{R_1} = \cancel{k} \frac{Q_2}{R_2}$$

$$Q_1 = Q_2 \cdot \frac{R_1}{R_2}$$

$$\left. \begin{aligned} Q &= Q_1 + Q_2 \\ Q_1 &= Q_2 \cdot \frac{R_1}{R_2} \end{aligned} \right\}$$

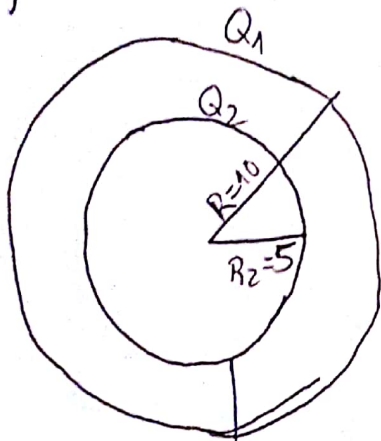
$$Q = Q_2 \cdot \frac{R_1}{R_2} + Q_2$$

$$Q_2 = 1'86 \cdot 10^{-9} C$$

$$Q_1 = 3,7 \cdot 10^{-9} C$$

$$V_1 = k \cdot \frac{3,7 \cdot 10^{-9}}{0,01} = 333 V$$

c)



Cuando una esfera está dentro de otra y queremos calcular el potencial de la mayor lo que hacemos es: Calcular

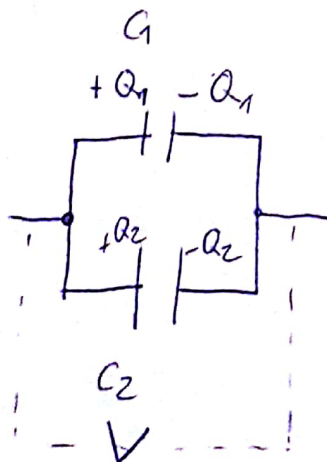
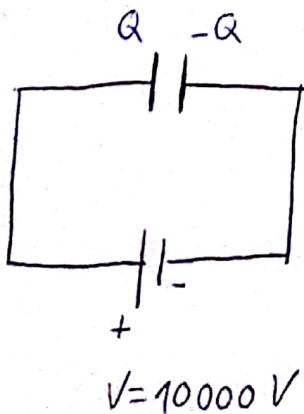
el V en la esfera mayor y sumarle el V que crea la Q de la esfera pequeña.

$$V_1 = k \cdot \frac{Q_1}{R_1} + k \cdot \frac{Q_2}{R_1}$$

$$V_2 = k \cdot \frac{Q_2}{R_2} + k \cdot \frac{Q_1}{R_1}$$

11/10/2017

14/ $C_1 = 0,1 \mu F$
 $V = 10000 V$



$$C_2 = 93 \mu F$$

la diferencia de V será la misma para ambos.

$$Q_1 + Q_2 = Q$$

$$Q_1 + Q_2 = 10^{-3}$$

$$V = \frac{Q_1}{C_1}$$

$$V = \frac{Q_2}{C_2}$$

$$Q_1 + Q_2 = 10^{-3}$$

$$\frac{Q_1}{C_1} = \frac{Q_2}{C_2}$$

$$C = \frac{Q}{V} \Rightarrow Q = CV = 0,1 \cdot 10^{-6} \cdot 10^4 = 10^{-3} C$$

$$\left. \begin{aligned} Q_1 + Q_2 &= 10^{-3} \\ Q_1 &= Q_2 \cdot \frac{C_1}{C_2} \end{aligned} \right\}$$

$$\begin{aligned} Q_1 &= 25 \cdot 10^{-5} \text{ C} \\ Q_2 &= 75 \cdot 10^{-5} \text{ C} \end{aligned}$$

$$V = \frac{Q_1}{C_1} = 2500 \text{ V}$$

$$b) U = \frac{1}{2} C V^2 \quad // \quad \frac{Q^2}{2C}$$

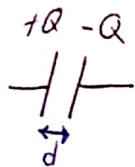
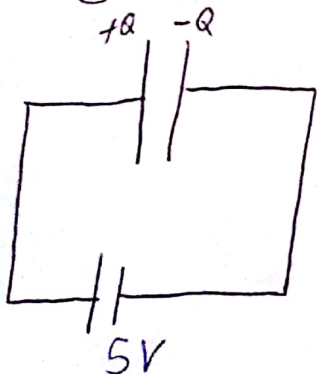
$$U_1 = \frac{1}{2} C_1 V^2 =$$

$$U_2 = \frac{1}{2} C_2 V^2 =$$

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17/10/2017

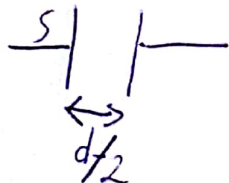
$$C = 20 \text{ nF} = 20 \cdot 10^{-9} \text{ F}$$



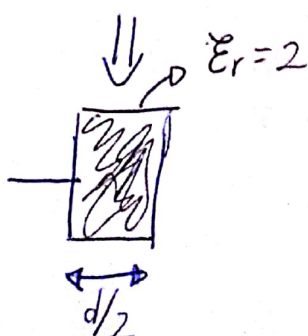
$$C = \frac{Q}{V}$$

$$Q = CV = 20 \cdot 10^{-9} \cdot 5 = 100 \cdot 10^{-9} \text{ C} = 10^{-7} \text{ C}$$

$$C = \epsilon_0 \frac{S}{d}$$



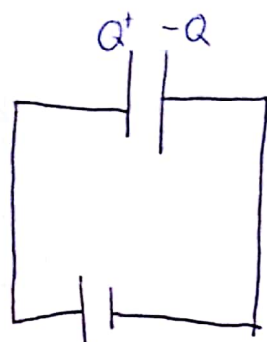
$$\Rightarrow C_1 = \epsilon_0 \frac{S}{d/2} = 2 \epsilon_0 \frac{S}{d} = 2C$$



$$\epsilon_r = \frac{\epsilon}{\epsilon_0}$$

$$C_2 = \epsilon_r C_1 = 2 \cdot 2C = 4C = 4 \cdot 20 \cdot 10^{-9} = 80 \cdot 10^{-9} \text{ F}$$

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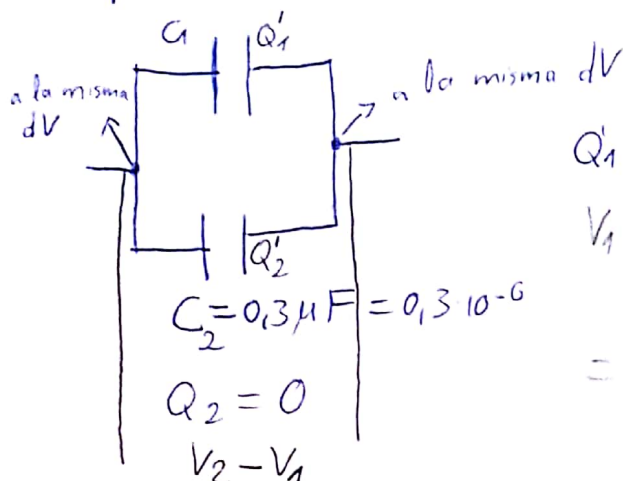


$$V = 10000V$$

$$Q_1 = C_1 \cdot V = 0,1 \cdot 10^{-6} \cdot 10000 = 10^{-3}C$$

$$V_1 = \frac{Q_1}{C_1}$$

$$C_1 = 0,1 \mu F = 0,1 \cdot 10^{-6} F$$



$$C_2 = 0,3 \mu F = 0,3 \cdot 10^{-6}$$

$$Q_2 = 0$$

$$V_2 - V_1$$

$$Q_1 + Q_2 = Q_1$$

$$V_1 = \frac{Q_1}{0,1 \cdot 10^{-6}} = V_2 = \frac{Q_2}{0,3 \cdot 10^{-6}}$$

$$Q_1 = 25 \cdot 10^{-9}$$

$$Q_2 = 75 \cdot 10^{-9}$$

$$V_1 = V_2 = \frac{25 \cdot 10^{-9}}{0,1 \cdot 10^{-6}} = 2500V$$

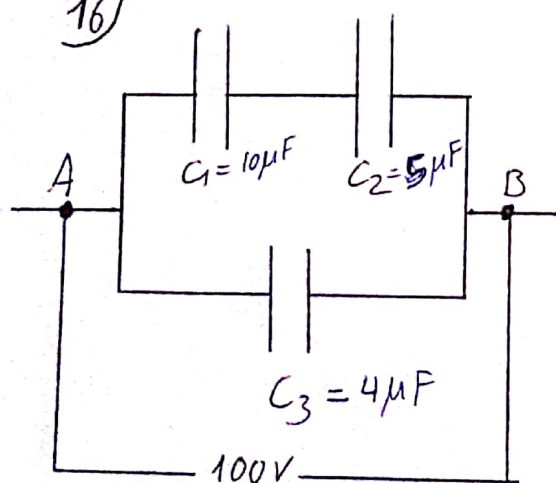
$$U = \frac{1}{2} \frac{Q^2}{C} = \frac{1}{2} C V^2 = \frac{1}{2} Q V$$

$$C = \frac{Q}{V}$$

$$U_1 = \frac{1}{2} C_1 V^2 = \frac{1}{2} \cdot 0,1 \cdot 10^{-6} \cdot (2500)^2 = 0,31J$$

$$U_2 = \frac{1}{2} C_2 V^2 = \frac{1}{2} \cdot 0,3 \cdot 10^{-6} \cdot (2500)^2 = 0,9375J$$

16/



$$C = \frac{Q}{V}$$

$$Q_1 = C_1 \cdot V = 10 \cdot 10^{-6} \cdot 100$$

Resistencias en serie se suman

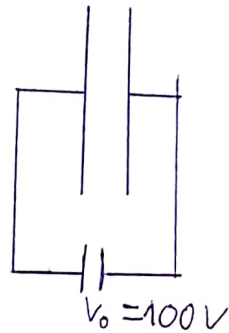
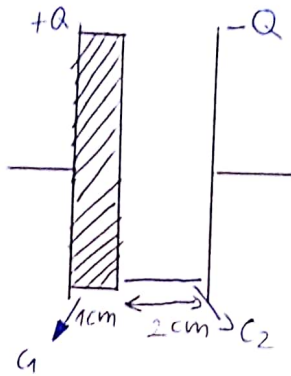
Conductores " " no se suman

$$\frac{1}{C_e} = \frac{1}{C_1} + \frac{1}{C_2} = \frac{C_1 + C_2}{C_1 C_2}$$

$$C_e = \frac{C_1 C_2}{C_1 + C_2}$$

Conductores en paralelo se suman

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$$dV = -\vec{E} \cdot d\vec{l}$$

$$V_0 = E_0 l \Rightarrow E_0 = \frac{V_0}{d}$$

Al poner el dieléctrico es como si hubieran 2 condensadores

$$C_1 = \epsilon \frac{1}{1}$$

$$C_2 = \epsilon_0 \frac{1}{2}$$

$$\frac{1}{C_e} = \frac{1}{C_1} + \frac{1}{C_2}$$

$$C_e = \frac{1}{C_1} + \frac{1}{C_2}$$

$$C_e = \frac{C_1 C_2}{C_1 + C_2}$$

$$C' = \epsilon_r C_0$$

$$E = \frac{E}{\epsilon_r}$$

$$V = \frac{V_0}{\epsilon_r}$$

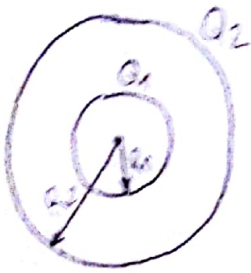
$$\epsilon_r = \frac{\epsilon}{\epsilon_0}$$

$$C_0 = \epsilon_0 \frac{S}{d} = \frac{1}{4\pi \times 10^9} \frac{1}{0.03} =$$

$$C_0 = \frac{Q}{V_0}$$

$$Q = C_0 V_0 = 3 \times 10^{-8} \text{ C}$$

a)



$$R_1 = 10 \text{ cm} = 0.1 \text{ m}$$

$$R_2 = 20 \text{ cm} = 0.2 \text{ m}$$

densidad de carga

$$\sigma = \frac{Q_2}{4\pi R_2^2}$$

5.5.10

$$Q_2 = 10^{-10} \text{ C}$$

$$V_1 - V_2 = 10000 \text{ V}$$

$$Q_1 = ?$$

a) La carga Q_1 de la superficie interior.

$$V = K \cdot \frac{Q}{R}$$

$$V_1 - V_2 = 10000 \text{ V}$$

$$K \cdot \frac{Q_1}{R_1} - K \cdot \frac{Q_2}{R_2} = 10000$$

$$9 \cdot 10^9 K \left(\frac{Q_1}{R_1} - \frac{Q_2}{R_2} \right) = 10000$$

$$\frac{Q_1}{R_1} - \frac{Q_2}{R_2} = \frac{10000}{K}$$

$$Q_1 = \frac{10000 R_1 R_2}{K} + Q_2$$

$$Q_1 = \frac{10000 \cdot 0.1 \cdot 0.2}{9 \cdot 10^9} + 10^{-10} = 2.23 \cdot 10^{-8} \text{ C}$$

$$V_1 = K \frac{Q_1}{R_1} + \frac{K Q_2}{R_2}$$

$$V_2 = K \frac{Q_2}{R_2} + K \frac{Q_1}{R_2}$$

$$V_1 - V_2 = 10000$$

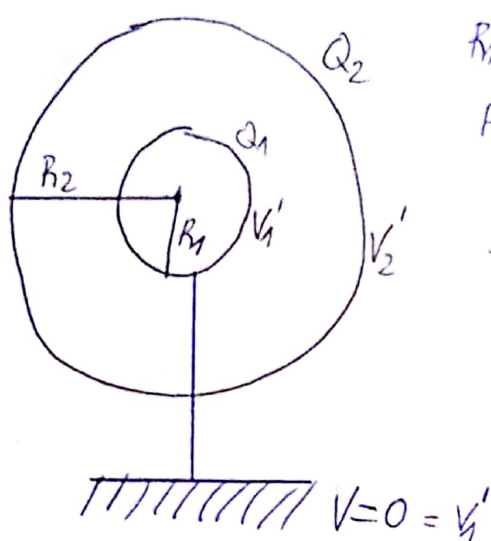
$$K \frac{Q_1}{R_1} + \frac{K Q_2}{R_2} - \frac{K Q_2}{R_2} + K \frac{Q_1}{R_2} = 10000$$

$$K \left(\frac{Q_1}{R_1} + \frac{Q_1}{R_2} \right) = 10000$$

$$Q_1 \left(\frac{1}{R_1} + \frac{1}{R_2} \right) = \frac{10000}{K}$$

 \Rightarrow

b) Si la superficie interna se conecta a la tierra a que potencial queda la superficie externa.



$$R_1 = 0,1 \text{ m}$$

$$R_2 = 0,2 \text{ m}$$

Valores iniciales de las cargas: $Q_1 = 2,22 \cdot 10^{-7} \text{ C}$
 $Q_2 = 10^{-10} \text{ C}$

$$b) V_1' = k \cdot \frac{Q_1'}{R_1} + k \cdot \frac{Q_2'}{R_2} = 0$$

$$V_2' = k \cdot \frac{Q_1'}{R_2} + k \cdot \frac{Q_2'}{R_2}$$

$Q_2' = Q_2 \Rightarrow$ Porque la esfera exterior no se ha conectado a ~~no~~ la tierra.

$$V_2' = k \cdot \frac{Q_1' + Q_2'}{R_2} = 9 \cdot 10^9$$

$$= 9 \cdot 10^9 \frac{(-0,5 \cdot 10^{-10} + 10^{-10})}{0,2} =$$

$$= [2,25 \text{ V}]$$

Si conectamos una carga a tierra los e^- de la tierra pasan a la carga o al contrario, esto lo hace para conseguir 0

$$\cancel{k} \cdot \frac{Q_1'}{R_1} = -\cancel{k} \cdot \frac{Q_2'}{R_2}$$

$$Q_1' = -Q_2 \frac{R_1}{R_2} = -10^{-10} \cdot \frac{0,1}{0,2} =$$

$$= [-0,5 \cdot 10^{-10} \text{ C}] \Rightarrow -5 \cdot 10^{-11} \text{ C}$$

\hookrightarrow la carga es negativa p^q la carga Q_2 atrae cargas positivas

$$\Rightarrow \frac{10000}{k} = Q_1 \cdot 5$$

$$Q_1 = 2,22 \cdot 10^{-7} \text{ C}$$