

# Table of derivatives

Function $y$	Derivative $\frac{dy}{dx}$	Examples
$kx^n$	$n k x^{n-1}$	<p>Multiply by the power <math>n</math>, then reduce the power by 1.</p> <p><math>y = 3x^2 \Rightarrow \frac{dy}{dx} = 2 \times 3x^1 = 6x</math></p> <p><math>y = -4x = -4x^1 \Rightarrow \frac{dy}{dx} = 1 \times (-4x^0) = -4</math></p> <p><math>y = 3 = 3x^0 \Rightarrow \frac{dy}{dx} = 0 \times 3x^{-1} = 0</math></p>
$\sin(kx)$	$k \cos(kx)$	<p>Multiply by <math>k</math>, then swap sin to cos.</p> <p><math>y = \sin(2x) \Rightarrow \frac{dy}{dx} = 2 \cos(2x)</math></p>
$\cos(kx)$	$-k \sin(kx)$	<p>Multiply by <math>-k</math>, then swap cos to sin.</p> <p><math>y = -\cos(\frac{x}{2}) \Rightarrow \frac{dy}{dx} = \frac{x}{2} \sin(\frac{x}{2})</math></p>
$e^{kx}$	$k e^{kx}$	<p>Multiply by <math>k</math>.</p> <p><math>y = e^{2x} \Rightarrow \frac{dy}{dx} = 2e^{2x}</math></p>
$\ln(x)$	$\frac{1}{x}$	<p>Make sure you only have <math>\ln(x)</math> which has derivative <math>\frac{1}{x}</math>. (Remember the derivative of a constant is 0.)</p> <p><math>y = -\ln(3x) = -\ln(3) - \ln(x) \Rightarrow \frac{dy}{dx} = 0 - \frac{1}{x} = -\frac{1}{x}</math></p>

## An example

A function can be expressed as the sum of smaller expressions called terms. So

$$f(x) = \text{Term 1} + \text{Term 2} + \dots + \text{Term } k.$$

For example, the function  $f(x) = 3x^2 - 4x + 3 + \sin(2x) - \cos(\frac{x}{2}) + e^{2x} - \ln(3x)$  has terms:  $3x^2$ ,  $-4x$ ,  $3$ ,  $\sin(2x)$ ,  $-\cos(\frac{x}{2})$ ,  $e^{2x}$  and  $-\ln(3x)$ .

To find the derivative of a function, you can find the derivative of each term.

The examples in the table above give the derivatives of each of the terms in

$$f(x) = 3x^2 - 4x + 3 + \sin(2x) - \cos(\frac{x}{2}) + e^{2x} - \ln(3x)$$

so the derivative of  $f(x)$  is

$$f'(x) = 6x - 4 + 0 + 2\cos(2x) - \frac{1}{2}\sin(2x) + 2e^{2x} - \frac{1}{x} = 6x - 4 + 2\cos(2x) - \frac{1}{2}\sin(2x) + 2e^{2x} - \frac{1}{x}.$$