

13. Exponential and logarithmic functions

There are two log keys on your calculator, with their associated exponential keys. The latter are accessed by first using the shift key:

$$3^2 = 9 \rightarrow \log_3 9 = 2$$

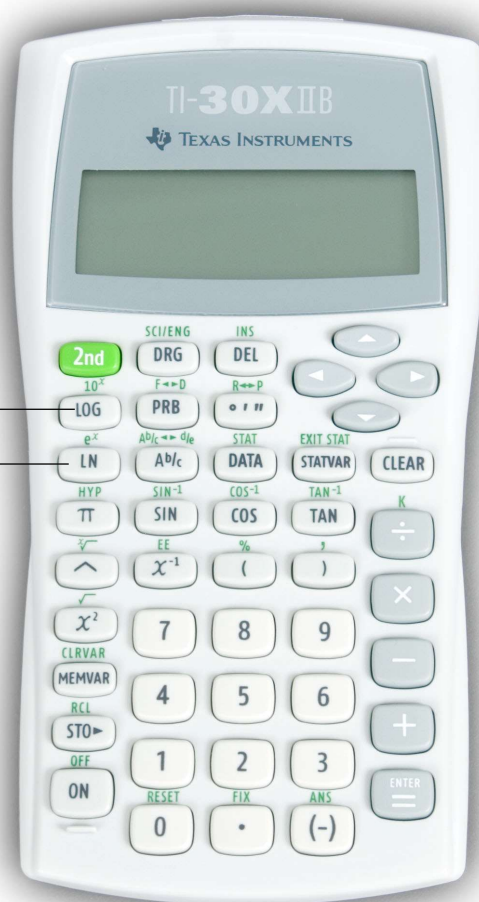
Base 10
log key

10^x
LOG

Natural
log key

e^x
LN

$$10^4 = 10000 \rightarrow \log_{10} 10000 = 4$$



$$a^0 = 1 \rightarrow \log_a 1 = 0$$

The 'log' key uses base 10 and the 'ln' key uses base e (natural logarithm).

Example 1

Solve equation $2^a = 20$

Taking logs of both sides;

$$\log 2^a = \log 20$$

$$\Rightarrow a \log 2 = \log 20$$

$$\Rightarrow a = \frac{\log 20}{\log 2}$$

To find the value of a , the keystrokes are:



The display should read 4.3219281.

So, $2^{4.32} \approx 20$. Confirm this by using the \wedge key.

Example 2

Given $\log y = 1.584$, find the value of y

$$\log y = 1.584$$

$$\Rightarrow y = 10^{1.584}$$

The 10^x key is above the log key. Hence the keystrokes are:



The display should read 38.370725

Example 3 (harder)

Given $\log_x 6 = 1.5$, find the value of x

$$\log_x 6 = 1.5$$

$$\Rightarrow \frac{\log 6}{\log x} = 1.5$$

$$\Rightarrow \frac{\log 6}{1.5} = \log x$$

To find $\log x$, the calculator keystrokes are:



The display should read 0.5187675.

Since this is the value of $\log x$, you still need to find x where $x = 10^{0.5187675}$

Without removing the answer of 0.5187675 on your display, press:



Your display should now read 3.3019272

Note: You could use the 'ln' key instead of the 'log' key – the answer would still be the same. Try it!



$$\log_7 x = 2$$

$$\frac{\log x}{\log 7} = 2$$

$$\log x = 2 \log 7$$

$$= 1.6902$$

$$x = 10^{1.6902} = 49$$

$$x^{1.5} = 6$$

$$\log x^{1.5} = \log 6$$

$$1.5 \log x = \log 6$$

$$1.5 = \frac{\log 6}{\log x}$$

$$\log x = \frac{\log 6}{1.5}$$

$$= 0.5188$$

$$10^{0.5188} = 3.3019 = x$$

$$\text{or } 3.3019^{1.5} = 5.999 \approx 6$$