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The proposed time complexity for my code regarding this assignment is $O(n)$. My assignment consists of one algorithm that conducts a few checks by comparing `waterAvalible` with `waterRequired` at each table to produce `waterLevel`, and $O(1)$ operations such as addition and subtraction inside a while loop. This loop always terminates after iterating the arrays passed in twice due to a boolean value. As such, the while loop is $O(n)$ since it iterates through the array twice, at most (meaning going from 0 to $n-1$ twice), without moving backwards.

We make the algorithm $O(n)$ by making use of the idea that if we start at table X and the water level becomes invalid at table $X + i$ meaning the `waterLevel` drops below 0 then all tables between $[1, X + i]$ inclusive are also invalid. In other words, if we start at table 1 and on table 6 the `waterLevel` drops below 0 then we know tables $[2,6]$ are invalid. This is because when we start at table 1 (assuming table 1 is valid) it is possible to gain an extra W amount of water if `waterAvalible` > `waterRequired` and the minimum amount we “enter” table 2 from table 1 is zero water if `waterAvalible` == `waterRequired` (we assume table 1-> 2 is valid), but when we start at table 2 we start with 0 water in the reservoir. If the extra W water gained at table 1 was not enough to keep `waterLevel` > 0, then table 2 cannot provide us with enough water since `waterstartX` ≥ `waterstartX-1` (assuming table $X \rightarrow X-1$) is valid and so on for all tables until $X+i$.

Using this observation, we start at table X (X goes from 1 to `waterAvalible.length`) and iterate through `waterAvalible` and `waterRequired` until we reach table X again which means table X is valid. The second key idea to reducing this algorithm from $O(n^2)$ to $O(n)$ is that we keep track of the current water level at each table by iterating `waterAvalible` and `waterRequired` simultaneously and updating our variables likes so. Once we encounter a nonvalid table we know all the tables prior are also invalid, so we don’t need to check again from table $X+1$. We do this instead of iterating through `waterRequired` once for every table in `waterAvalible` until we hit a valid table which would be $O(n^2)$. As all checks and updates to our pointers are composed of adding or subtracting values and comparisons between `waterRequired` with `waterAvalible` using array accesses they are $O(1)$ which is negligible compared to $O(n)$. Overall, this makes the best case of the algorithm $O(n)$ (where table 1 is valid or no table is valid) and worst case $2O(n)$ if only table N is valid since we must iterate through 0 to N twice.