M. Boady, B. Char, J. Johnson, G. Long, S. Earth

### 1 Introduction

You may work in teams of **one** or **two** students. Submit one copy for the entire group.

Write your answers on this lab sheet. Only what is written on this lab sheet will be graded.

This lab is due at the end of the class period. You may not continue to work on it once class has ended. This lab contains 4 questions.

#### Grading

- 25 points Putting everyones names on this page
- 20 points Earned for each correct question (Answer is fully correct)
- 5 points Earned for **partial credit** any question

No additional point amounts can be earned. You cannot earn 7 points on a question for example.

The maximum score for a lab is 100. If you get everything correct, that adds up to 105 points but will be reduced to 100.

A question will be marked correct as long as it covers all requirements of the question. It does not need to be perfect, but must be fully correct. A single typo or very minor issue where the intention is clear and all requirements are met would still earn full points.

We want you to complete questions fully, not try to earn partial credit on multiple questions. You may ask your Professor/Course assistant questions during lab.

Labs must be done in the presence of an instructor and/or course assistant or credit will not be given.

Partners should alternate each class day which person is physically typing and submitting the lab.

Do not split up the problems or you risk not finishing on time due to the cumulative nature of the questions.

Enter the name of the stu	ident in the group
Member 1 (submitter):	Joshua Koo
Member 2: Elar	n Rubin

### Question 1:

Variables have the following meaning in this question.

Let S = "it is currently saturday"

Let V = "I am playing video games"

(a) Translate the following argument to plain english.

$$S \implies V, V :: S$$

If it is Saturday, I am playing video games. I am playing video games. Therefore, it currently Saturday.

(b) Prove or Disprove the argument from the previous part.

To Prove: Prove the following using Proof by Deduction. You must write out your proof as the answer to this question. Only what is written on this paper is graded. You may use https://proofs.openlogicproject.org to helpsolve the proof and verify your correctness. Nothing done in the Proof Checker is graded, only what you write on this lab sheet. You may only use Basic Rules. Any Derived Rules are forbidden.

**To Disprove**: Show a counterexample. Give a case where the premises are true and the conclusion is false.

If it is Saturday, I am playing video games. It is Monday. I am playing video games. Therefore it is Saturday

Let M = "It is Monday"

 $S \Rightarrow V, V, M : S$ 

### Question 2:

Prove the following using **Proof by Deduction**. You **must** write out your proof as the answer to this question. **Only** what is written on this paper is graded.

You may use https://proofs.openlogicproject.org to help solve the proof and verify your correctness. Nothing done in the Proof Checker is graded, only what you write on this lab sheet.

You may only use Basic Rules. Any Derived Rules are forbidden.

Prove:  $P \wedge (Q \vee R), P \implies \neg R : Q \vee E$ 

## Construct a proof for the argument: $P \wedge (Q \vee R)$ , $P \rightarrow \neg R : Q \vee E$

1
 
$$P \wedge (Q \vee R)$$

 2
  $P \rightarrow \neg R$ 

 3
  $P$ 
 $\wedge E 1$ 

 4
  $\neg R$ 
 $\rightarrow E 2, 3$ 

 5
  $Q \vee R$ 
 $\wedge E 1$ 

 6
  $R$ 
 $\neg E 4, 6$ 

 7
  $\bot$ 
 $\neg E 4, 6$ 

 8
  $Q$ 
 $\lor I 8$ 

 10
  $Q$ 

 11
  $Q \vee E$ 
 $\lor I 10$ 

 12
  $Q \vee E$ 
 $\lor E 5, 6-9, 10-11$ 

T NEW LINE

**I** NEW SUBPROOF

© Congratulations! This proof is correct.

#### Question 3:

Prove the following using **Proof by Deduction**. You **must** write out your proof as the answer to this question. **Only** what is written on this paper is graded.

You may use https://proofs.openlogicproject.org to help solve the proof and verify your correctness. Nothing done in the Proof Checker is graded, only what you write on this lab sheet.

You may only use Basic Rules. Any Derived Rules are forbidden.

Prove:  $Q = \Rightarrow (Q \land \neg Q) :: \neg Q$ 

# Construct a proof for the argument: $Q \rightarrow (Q \land \neg Q) : \neg Q$

1 
$$Q \rightarrow (Q \land \neg Q)$$
  
2  $Q$   
3  $(Q \land \neg Q)$   $\rightarrow$  E 1, 2  
4  $Q$   $\land$  E 3  
5  $\neg Q$   $\land$  E 3  
6  $\bot$   $\neg Q$   $\neg$  E 4, 5  
7  $\neg Q$   $\neg$  I 2-6

© Congratulations! This proof is correct.

### Question 4:

Prove the following using **Proof by Deduction**. You **must** write out your proof as the answer to this question. **Only** what is written on this paper is graded.

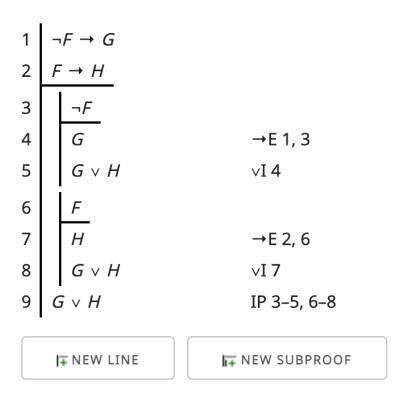
You may use https://proofs.openlogicproject.org to help solve the proof and verify your correctness. Nothing done in the Proof Checker is graded, only what you write on this lab sheet.

You may only use Basic Rules. Any Derived Rules are forbidden.

Prove:  $\neg F \implies G, F \implies H : G \lor H$ 

Hint: Use an Indirect Proof

### Construct a proof for the argument: $\neg F \rightarrow G$ , $F \rightarrow H$ : $G \lor H$



Sorry there were errors.

Line 9: Cites too many ranges of lines for the rule IP.