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(* Rotor Angle  $\theta$  is a function of time *)
 $\theta = \theta[t]$ ;

(* Assuming sinusoidally varying phase inductances
   Ld is the inductance of a phase when the d-axis of the rotor is aligned with it
   Lq is the inductance of a phase when the q-
   axis of the rotor is aligned with it *)
Ld = Lq;
La =  $(1/2) * (Ld + Lq) + (1/2) * (Ld - Lq) * \cos[-2 * \theta]$ ;
Lb =  $(1/2) * (Ld + Lq) + (1/2) * (Ld - Lq) * \cos[2 * (2 * \pi/3 - \theta)]$ ;
Lc =  $(1/2) * (Ld + Lq) + (1/2) * (Ld - Lq) * \cos[-2 * (-2 * \pi/3 - \theta)]$ ;

(* Sinusoidally varying flux linkage *)

 $\lambda_a = \lambda * \cos[-\theta] + \lambda_2 * \cos[-5 * \theta]$ ;
 $\lambda_b = \lambda * \cos[2 * \pi/3 - \theta] + \lambda_2 * \cos[5 * (2 * \pi/3 - \theta)]$ ;
 $\lambda_c = \lambda * \cos[-2 * \pi/3 - \theta] + \lambda_2 * \cos[5 * (-2 * \pi/3 - \theta)]$ ;

 $\lambda_r = \{\{\lambda_a\}, \{\lambda_b\}, \{\lambda_c\}\}$ ;
d $\lambda_r = D[\lambda_r, t]$ ;

(* Construct inductance matrix assuming no mutual inductances*)
L = {{La, 0, 0},
      {0, Lb, 0},
      {0, 0, Lc}};

(* Construct resistance matrix *)
R = {{r, 0, 0},
      {0, r, 0},
      {0, 0, r}};

(* Phase currents *)
i = {{ia[t]}, {ib[t]}, {ic[t]}};

idq = {{id[t]}, {iq[t]}, {i0[t]}};

(* Dq0 Transform *)
T =  $(2/3) * \{\{\cos[\theta], \cos[\theta - 2 * \pi/3], \cos[\theta + 2 * \pi/3]\},$ 
           $\{-\sin[\theta], -\sin[\theta - 2 * \pi/3], -\sin[\theta + 2 * \pi/3]\},$ 
           $\{1/2, 1/2, 1/2\}\}$ ;

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invT = Simplify[Inverse[T]];

λdq = Simplify[T.λr];
dλdq = Chop[Simplify[T.D[λr, t]]];

(*T*(L.D[i, t] + D[L, t].i + D[λr, t] + R.i)*)

t ∈ Reals;
L ∈ Reals;
θ ∈ Reals;
R ∈ Reals;
λr ∈ Reals;
i ∈ Reals;
idq ∈ Reals;

(*vdq = T.(L.D[i, t] + D[L, t].i + D[λr, t] + R.i);*)
vdq = T.(L.D[invT.idq, t] + D[L, t].(invT.idq) + R.(invT.idq)) + dλdq;

(*Simplify[vdq, (ia+ib+ic)==0];*)

vd = Chop[Simplify[vdq[[1, All]]]]
vq = Chop[Simplify[vdq[[2, All]]]]

idq = T.i;
didq = D[idq, t];

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Out[57]= $\{r \text{ id}[t] + Lq \text{ id}'[t] - (Lq \text{ iq}[t] + 5 \lambda 2 \sin[6 \theta[t]]) \theta'[t]\}$

Out[58]= $\{r \text{ iq}[t] + Lq \text{ iq}'[t] + (\lambda - 5 \lambda 2 \cos[6 \theta[t]] + Lq \text{ id}[t]) \theta'[t]\}$

