

Quantum Computers: Should we worry?

Dr. Morton Swimmer
FTR, Trend Micro Research

HH.Security Meetup 2024-12-5



Summary of NATO's Quantum Technologies Strategy

16 Jan. 2024 - | Last updated: 17 Jan. 2024 11:32

English | [French](#)

- NATO has developed, adopted and implemented frameworks, policies and standards for both software and hardware to enhance interoperability;
 - Allies have cooperated in the development of quantum technologies with a view to maintain NATO's technological edge and Allies' abilities in the field;
 - NATO has identified, understood and capitalised on evolving quantum technologies advancements, including with enabling technologies and in convergence with other EDTs;
 - NATO has a Transatlantic Quantum Community to strategically engage with government, industry and academia from across our innovation ecosystems;
 - NATO has transitioned its cryptographic systems to quantum-safe cryptography;
 - Relevant quantum strategies, policies and action plans are dynamically updated and executed; and
 - Allies have become aware of, and act to prevent, on a voluntary basis, adversarial investments and interference into our quantum ecosystems, which can include, on a national basis, the examination of relevant supply chains.
5. Further, NATO will provide the leading transatlantic forum for quantum technologies

Why We Can't Afford to Ignore Quantum Computing, Even if We Don't Completely Understand It

TAG Infosphere

Wed, December 4, 2024 at 3:00 PM GMT+1 • 3 min read

Available For Free Download**NEW YORK, NY / ACCESSWIRE**

the fear that the Y2K bug provoked even panic—that when the calendar and systems that could only accommodate would come crashing down, wreaking many deaths.

If that sounds like a distant memory about Y2Q, the shorthand cyber experts use, it's because it is. Though quantum computing is still about it can come across as geeky danger it poses to the global internet.

Experts agree that it's only a matter of time before quantum computing technology will be able to crack the secrets that keep the internet secure. Current safeguards with post-quantum potential catastrophe seems years away, but the quantum technology being developed is advancing.

The new issue of the Security Annals has four articles and a short story interview with Peter Shor, the mathematician whose quantum algorithm that now bears his name will likely be another decade before capable of cracking the code. But don't hurry.

QUANTUM COMPUTING KILLS ENCRYPTION

by: **Elliot Williams**

79 Comments

September 29, 2015



COULD ADVANCED QUANTUM COMPUTING POSE A RISK TO BITCOIN SECURITY?

Rapid progress in quantum computing could pose a risk to certain types of bitcoin transactions. So how can we combat this risk?

DEBANJAN CHATTERJEE • OCT 16, 2021

HOME > TECHNICAL



Rapid progress in quantum computing is predicted by some to have crucial ramifications in domains using public-key cryptography, such as the Bitcoin ecosystem.

Bitcoin's "asymmetric cryptography" is based on the principle of "one-way function," implying that a public key can be easily derived from its corresponding private key but not vice versa. This is because classical algorithms require an astronomical amount of time to perform such computations and consequently are impractical. However, Peter Shor's polynomial-time quantum algorithm run on a sufficiently-advanced quantum

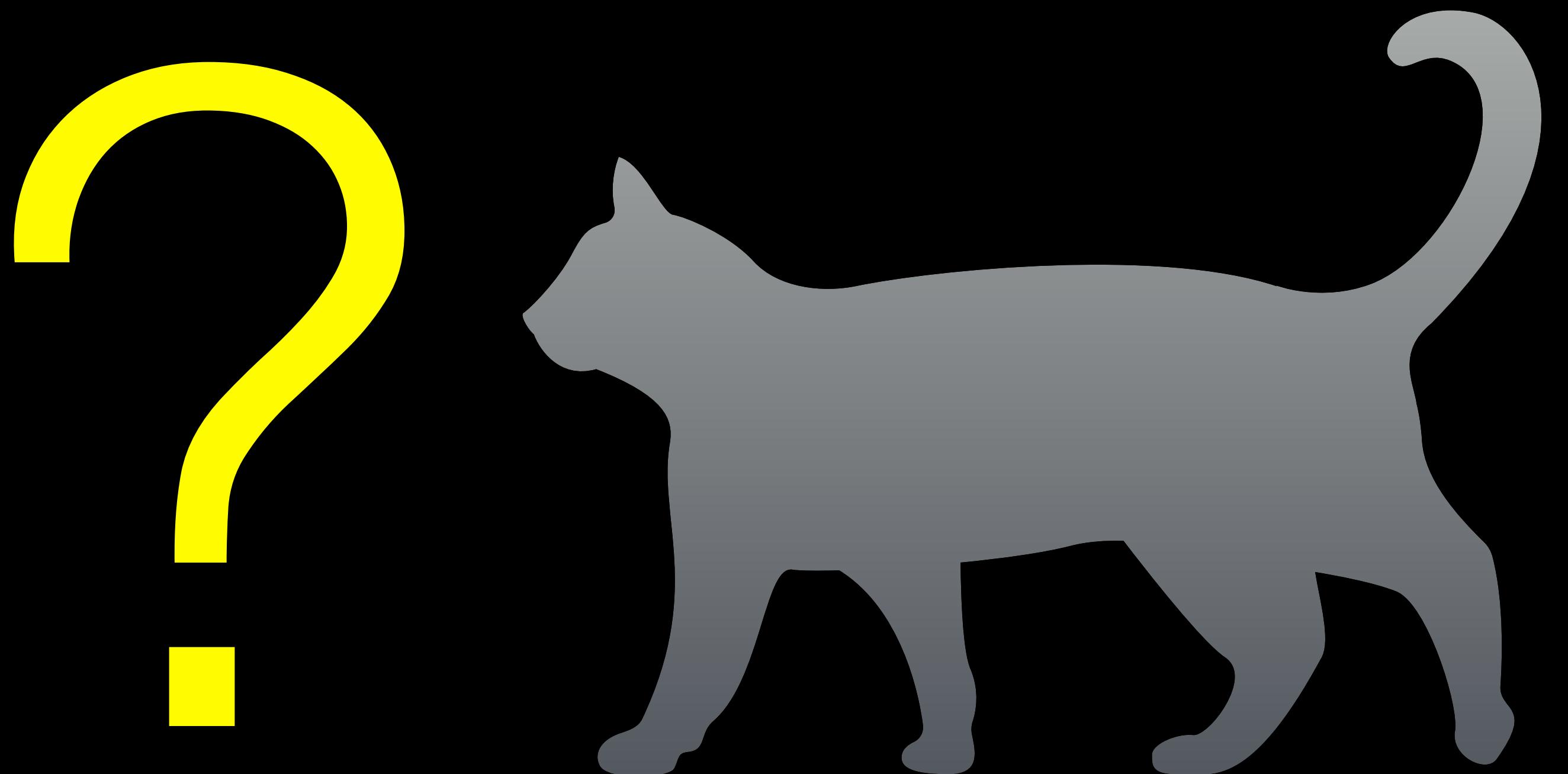
HOW BAD IS IT?

If you take the development of serious quantum computers seriously, the current state of affairs based on factoring primes or doing modular exponentiations and **Diffie-Hellman** are all in trouble. Specifically, **Shor's algorithm** will render the previously difficult math problems that underpin most of our security protocols irrespective of chosen key length. That covers most currently used encryption methods, such as RSA that's used in negotiating an SSL connection. That is (or was) the case for nearly every important encrypted transaction that touches the web.

All is not doom and gloom, however. There are other families of public-key algorithms that aren't solved by Shor's algorithm or any of the other known quantum algorithms, although they haven't been subjected to as much (classical) cryptanalysis and the algorithms and protocols aren't as polished yet. (More on this topic below.)

Three questions

- What is the threat?
- How real is the threat?
- What can we do about it?





What is the threat?

Harvesting attack

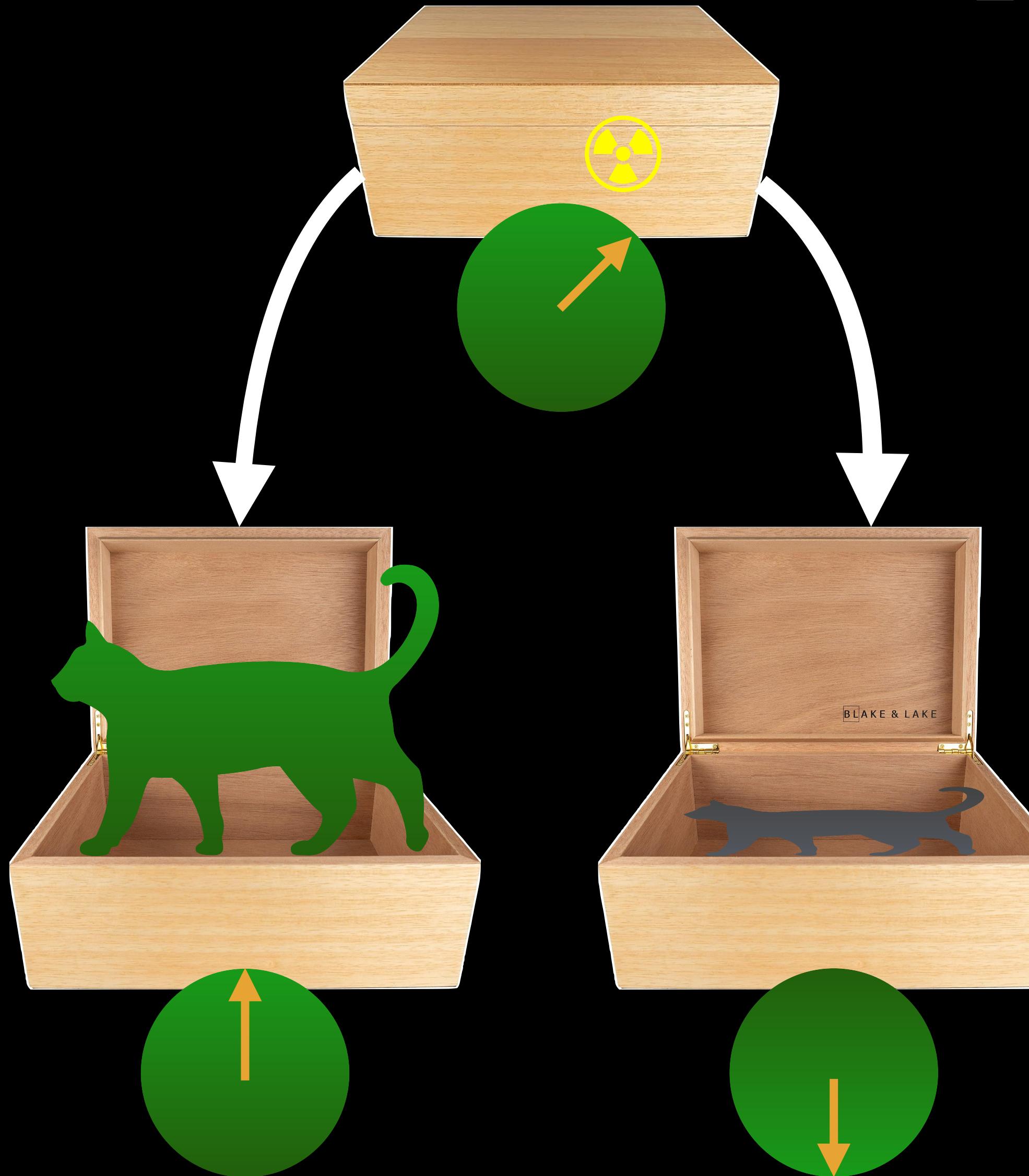
- We assume that our communications are secure when encrypted
 - Quantum computers may break this assumption
- Harvesting attack
 - Capture traffic now, decrypt later
 - Requirements on secrecy vary
 - 'later' may be later than we care about or never late enough

Quantum Computers

- Not an evolution of classical
- Based on Superposition and Entanglement
- Built with Qubits and Gates



Superposition

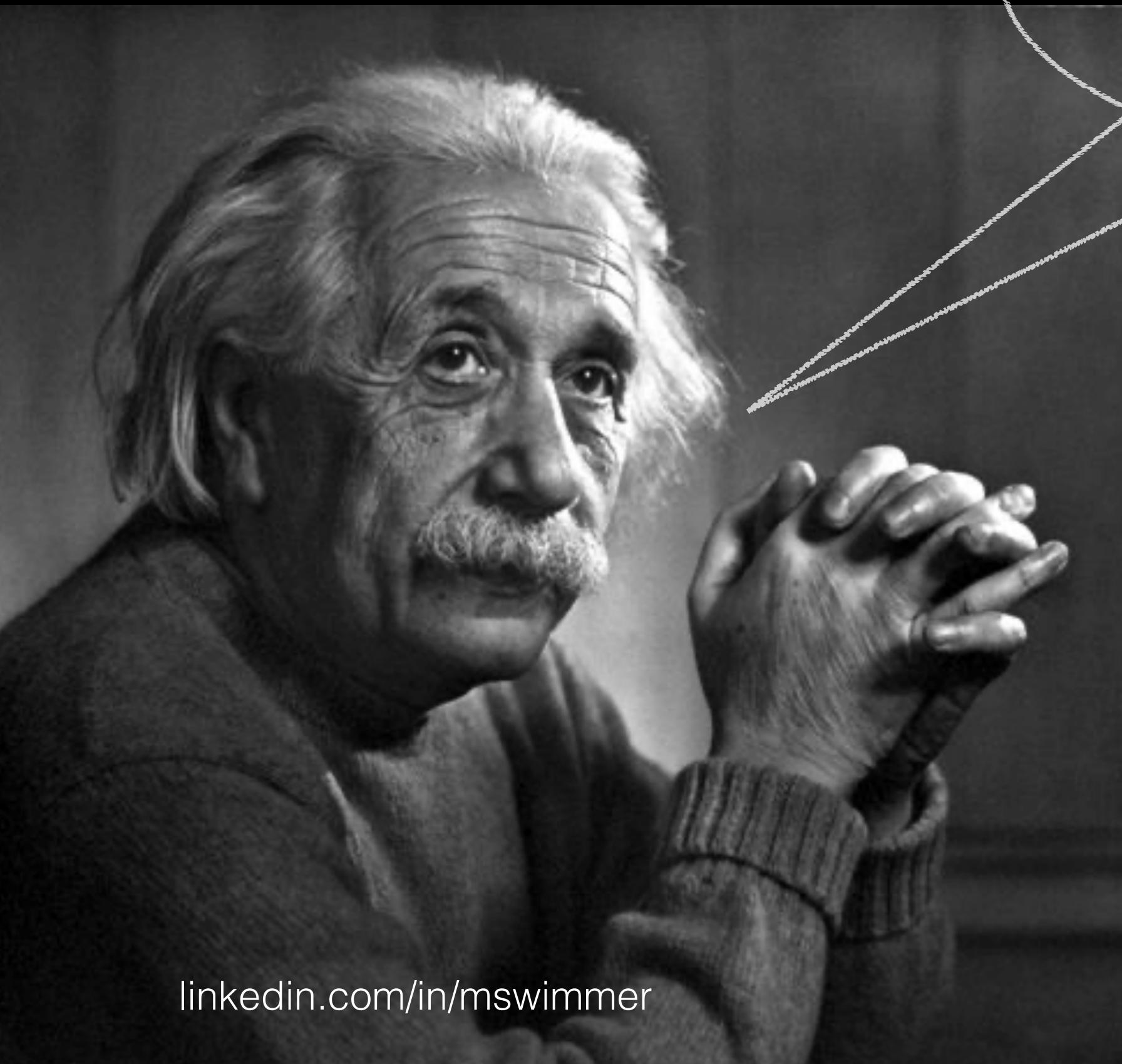


- Classical bit {0,1}
- A qubit {0..1}
- This will "collapse" when measured

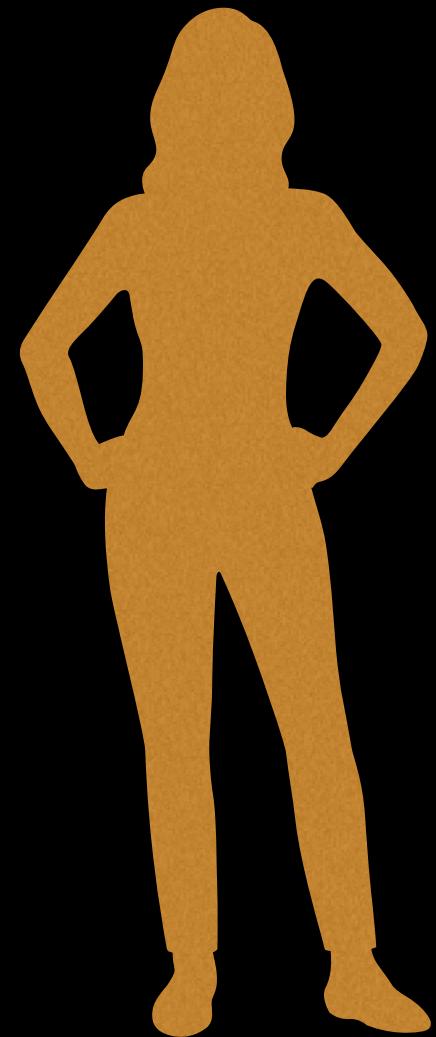
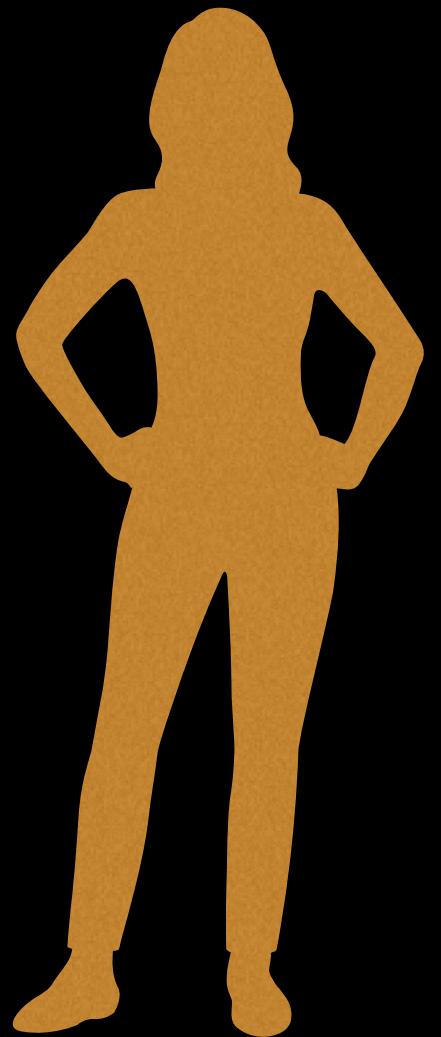
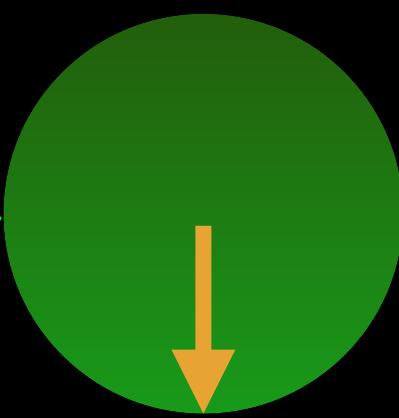
Our goal is to create a system
that cancels out wrong
answers and leaves the right
answers

"Verschränkung"

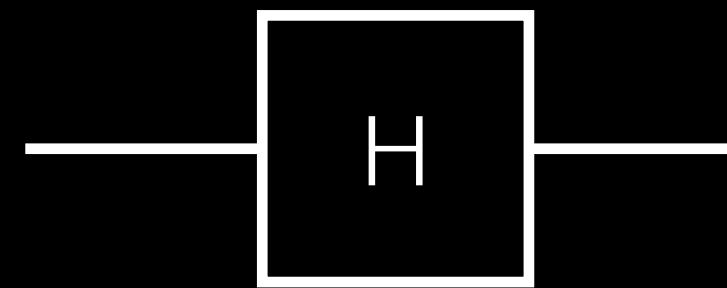
Entanglement



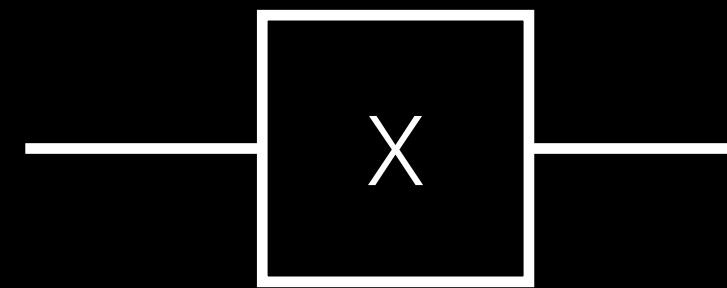
"Spukhafte
Fernwirkung"



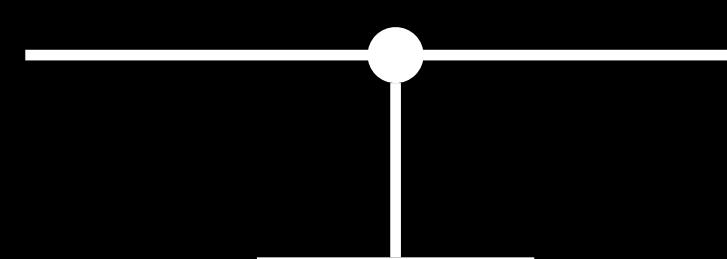
Quantum gates



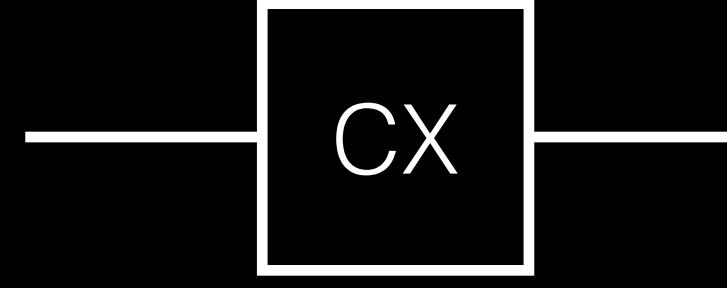
Hadamard



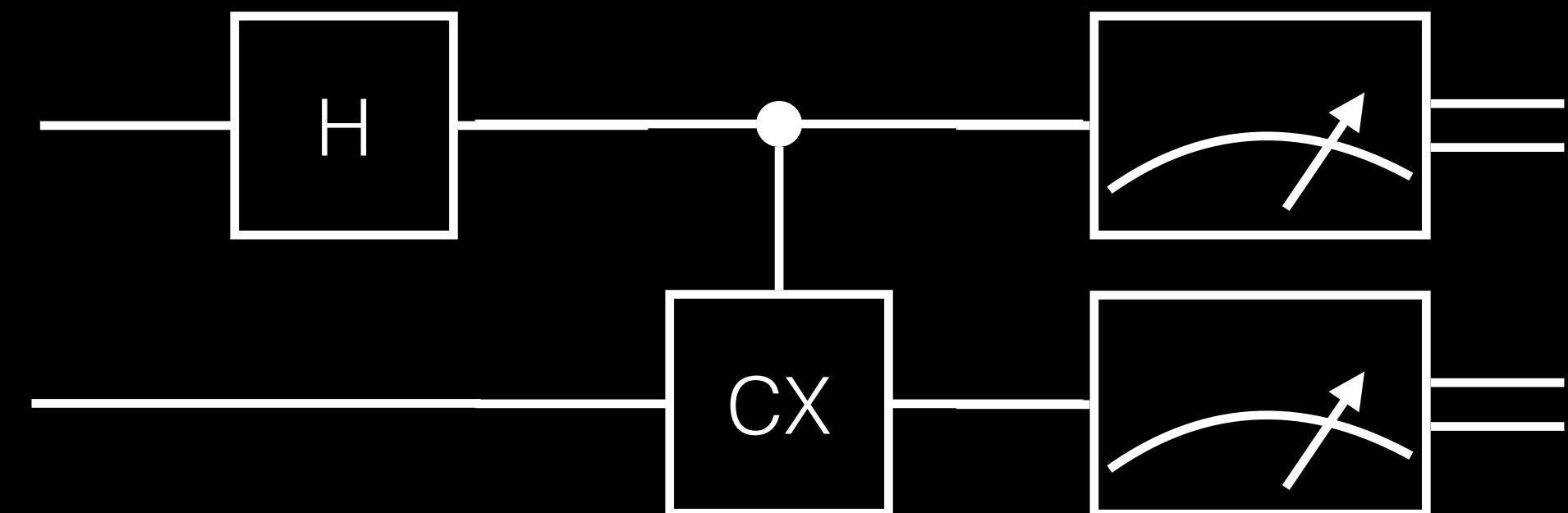
NOT



Controlled NOT



and many more



Measurement
resulting in a classical bit

Breaking RSA

Disclaimer

No cryptographers were permanently damaged in
the production of the following slides



BUT, there will be math

Breaking RSA

This means factoring large integers

$$s \times t = N$$

N is shared, s and t are secret

The attacker's goal: find s or t

Factoring is hard: Naive approach

```
def calculate_primes_up_to(n):
    primes = set()
    for a in range(2, int(n/2)+1):
        if not any(a % b == 0 for b in primes):
            primes.add(a)
    return sorted(primes)
```

```
def naive_factor(N, primes):
    for i in primes:
        for j in [p for p in primes if p < i]:
            if i * j == N:
                return i, j
```

Factor a 38 bit integer: 249976000567

```
N = 249976000567
primes = calculate_primes_up_to(N)
s, t = naive_factor(N, primes)
print(s, t, s * t)
```

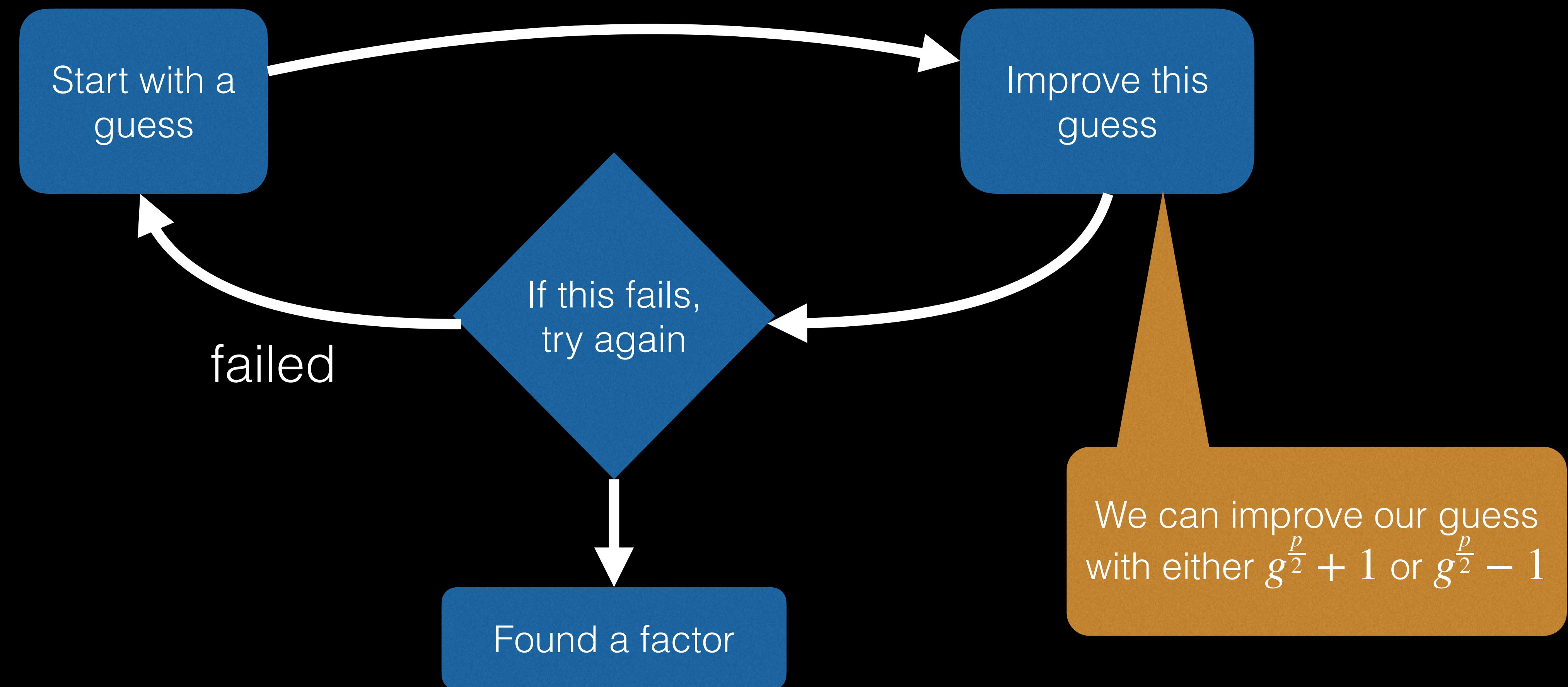
Never completed on my machine. A 25 bit key solved in over 5 hours.

RSA challenges solved up to 829 bits

Guess and check

g

$$(g^{\frac{p}{2}} + 1) \times (g^{\frac{p}{2}} - 1) = m \times N$$



N=15

1. Guess $g = 3$
2. $\gcd(15, 3) == 3$
3. Found factors: 3, 5

N=15

1. Guess $g = 7$
2. No common divisor
3. Let's improve our guess with $g^{\frac{p}{2}} - 1$
4. Trying $p=2$
5. New guess $7^{\frac{2}{2}} - 1 = 7 - 1 = 6$
6. $\gcd(15, 6) == 3$
7. Found factors: 3, 5

N=15

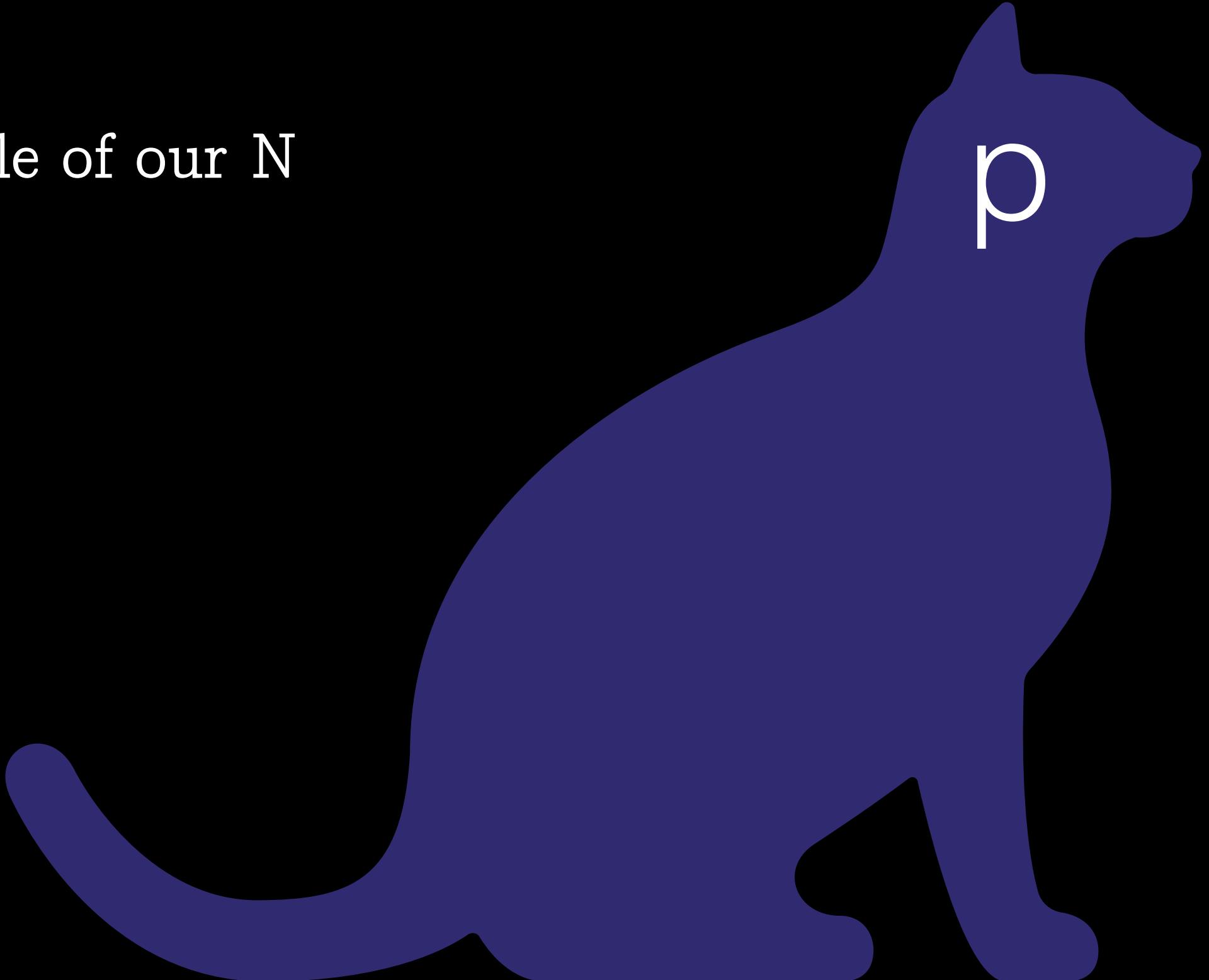
1. Guess $g = 2$
2. No common divisor
3. Let's improve our guess with $g^{\frac{p}{2}} - 1$
4. Trying $p=2$
5. new guess: $2^{\frac{2}{2}} - 1 = 2 - 1 = 1$
6. 1 is a trivial divisor and is rejected
7. Let's use $g^{\frac{p}{2}} + 1$ instead
8. new guess: $2^{\frac{2}{2}} + 1 = 2 + 1 = 3$
9. $\gcd(15, 3) == 3$
10. Found factors: 5, 3

But sometimes we don't get an answer

1. Guess $g = 14$
2. $\gcd(15, 14) == 1$ is trivial
3. Trying to find p for $g=14$
4. Trying $p=2$
5. fail
6. Trying $p=4$
7. fail
8. Trying $p=6$
9. fail
10. Trying $p=8$
11. fail
12. Trying $p=10$
13. fail
14. ...

p is the problem

- For large values of N, it becomes hard to find the right p
- Reflecting on this method
 - We have $(g^{\frac{p}{2}} + 1) \times (g^{\frac{p}{2}} - 1) = m \times N$
 - Multiplying our two guess candidates we get some multiple of our N
- Multiply this out
 - $g^p = m \times N + 1$
 - Special case of $g^p = m \times N + r$
 - Meaning g^p is some multiple of N plus a remainder



$$N = 15, g = 7$$

$$g^x = m \times N + r$$

$$7^0 = 1 = 0 \times 15 + 1$$

$$7^1 = 7 = 0 \times 15 + 7$$

$$7^2 = 49 = 3 \times 15 + 4$$

$$7^3 = 343 = 22 \times 15 + 13$$

$$7^4 = 2401 = 160 \times 15 + 1$$

$$7^5 = 16807 = 1120 \times 15 + 7$$

$$7^6 = 117649 = 7843 \times 15 + 4$$

$$7^7 = 823543 = 54902 \times 15 + 13$$

$$7^8 = 5764801 = 384320 \times 15 + 1$$

$$7^9 = 40353607 = 2690240 \times 15 + 7$$

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We need to find p so that

$$g^{1+0} \cong g^{p+x} \cong g^{2p+x} \cong \dots \pmod{N}$$

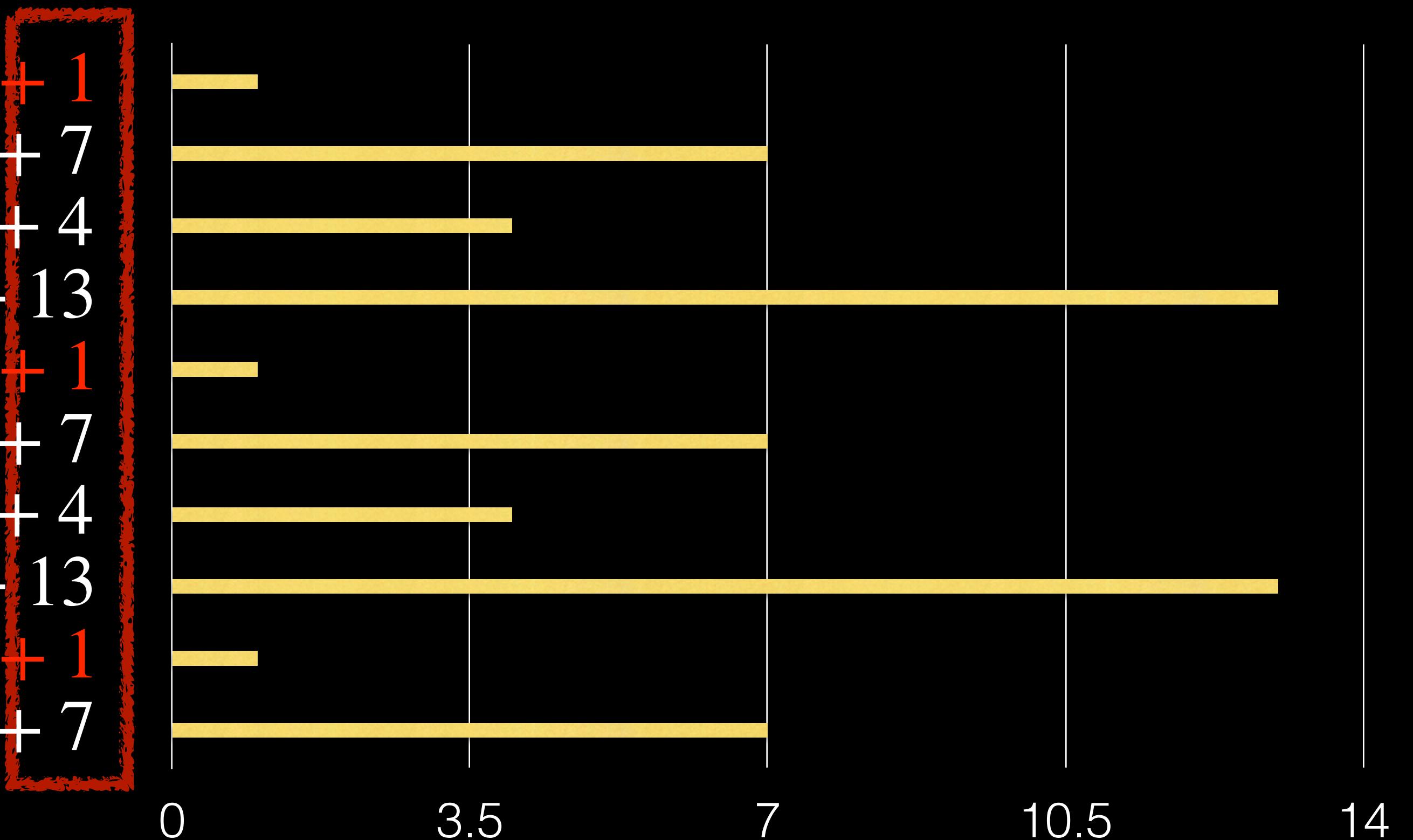
$$N = 15, g = 7$$

$$\begin{aligned}7^0 &= 1 = 0 \times 15 + 1 \\7^1 &= 7 = 0 \times 15 + 7 \\7^2 &= 49 = 3 \times 15 + 4 \\7^3 &= 343 = 22 \times 15 + 13 \\7^4 &= 2401 = 160 \times 15 + 1 \\7^5 &= 16807 = 1120 \times 15 + 7 \\7^6 &= 117649 = 7843 \times 15 + 4 \\7^7 &= 823543 = 54902 \times 15 + 13 \\7^8 &= 5764801 = 384320 \times 15 + 1 \\7^9 &= 40353607 = 2690240 \times 15 + 7\end{aligned}$$

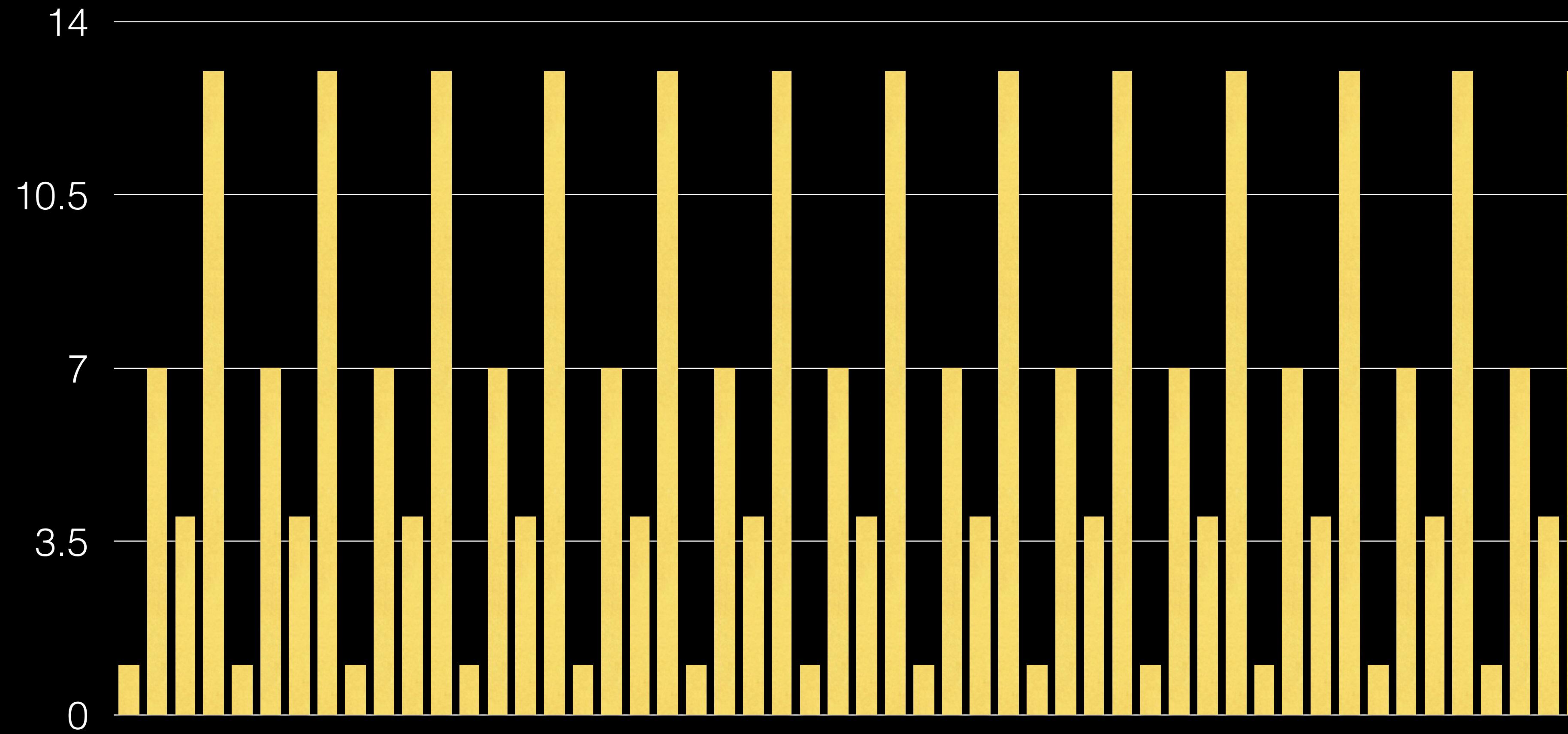
There is a pattern to the remainders

$N = 15, g = 7$

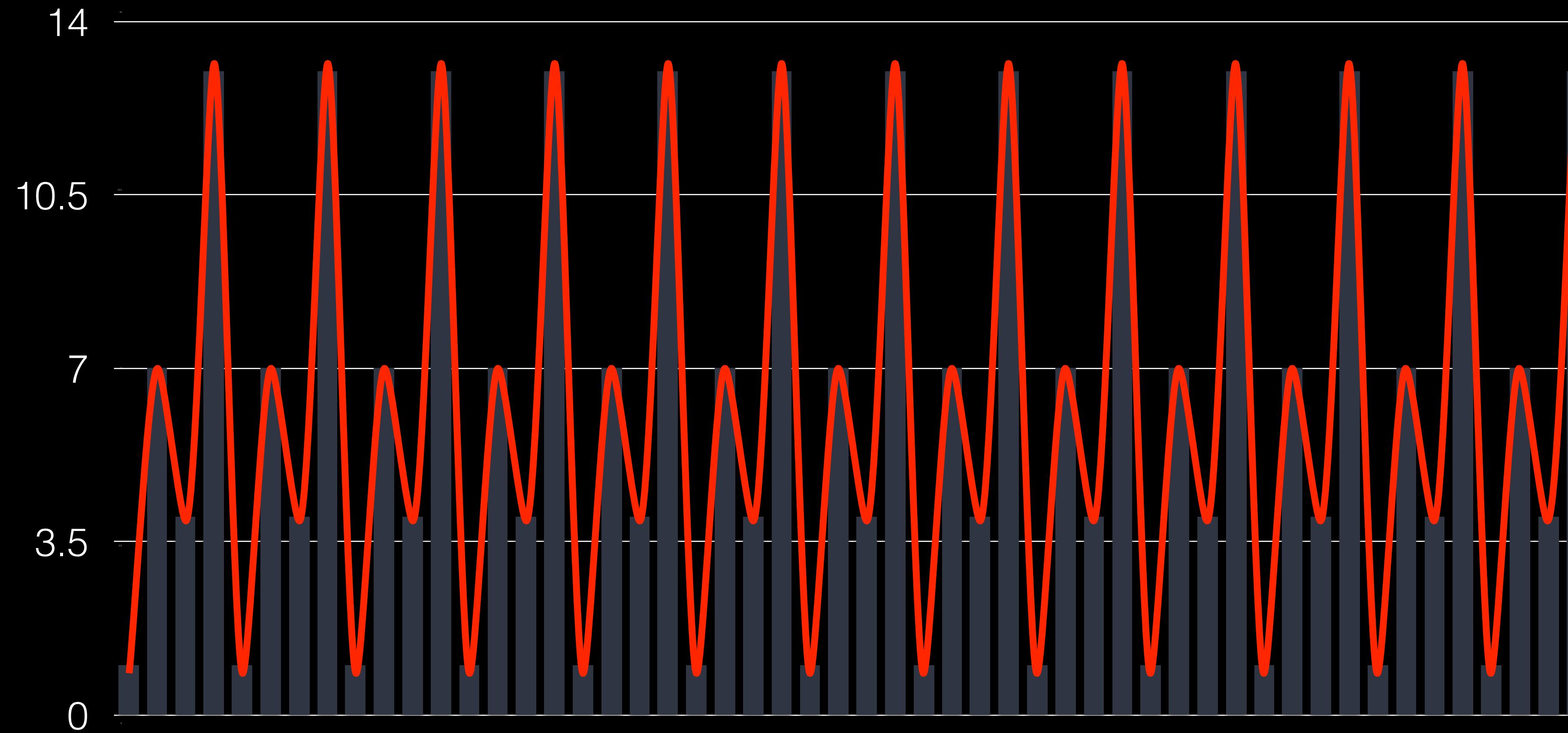
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$N = 15, g = 7$

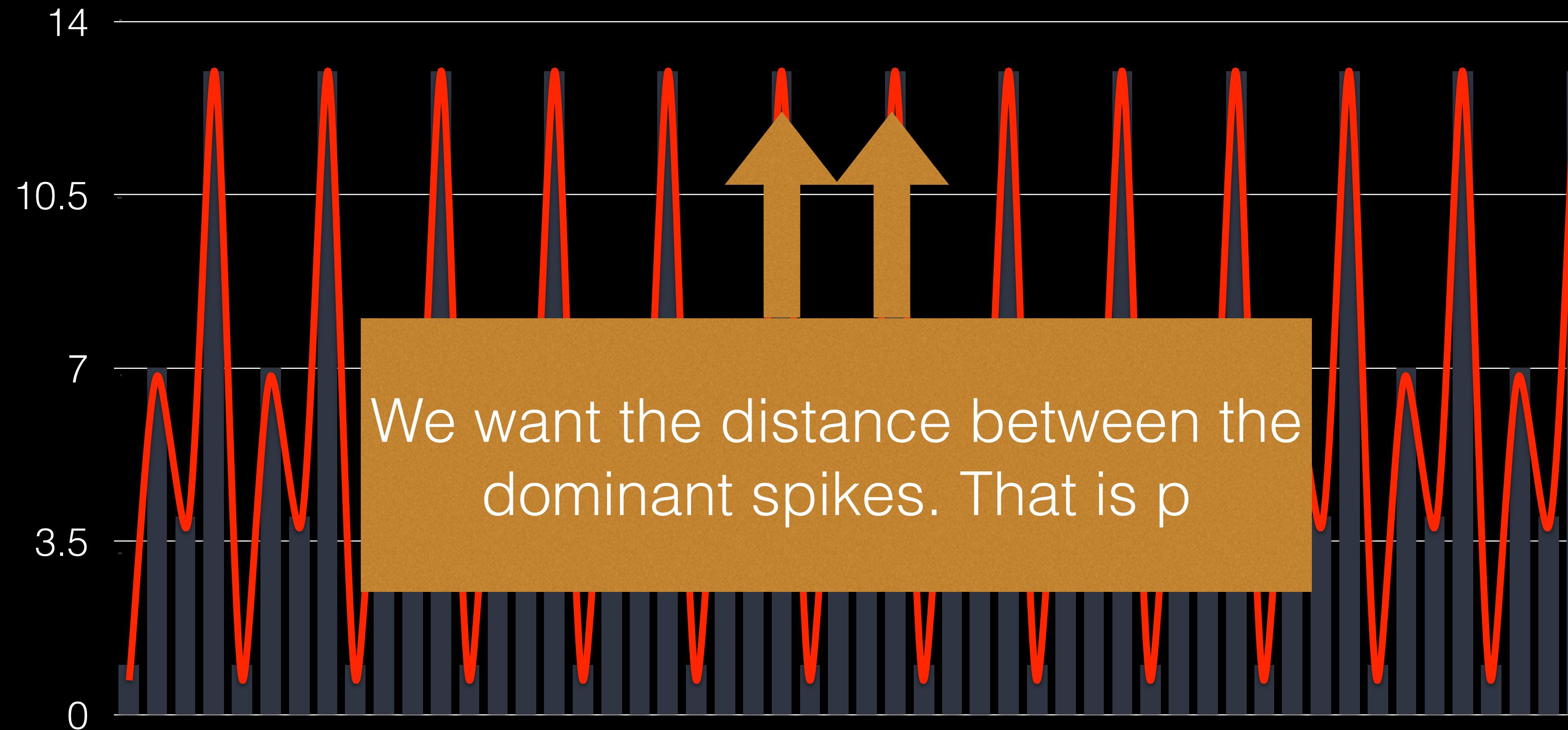


N = 15, g = 7



The remainders look like a signal

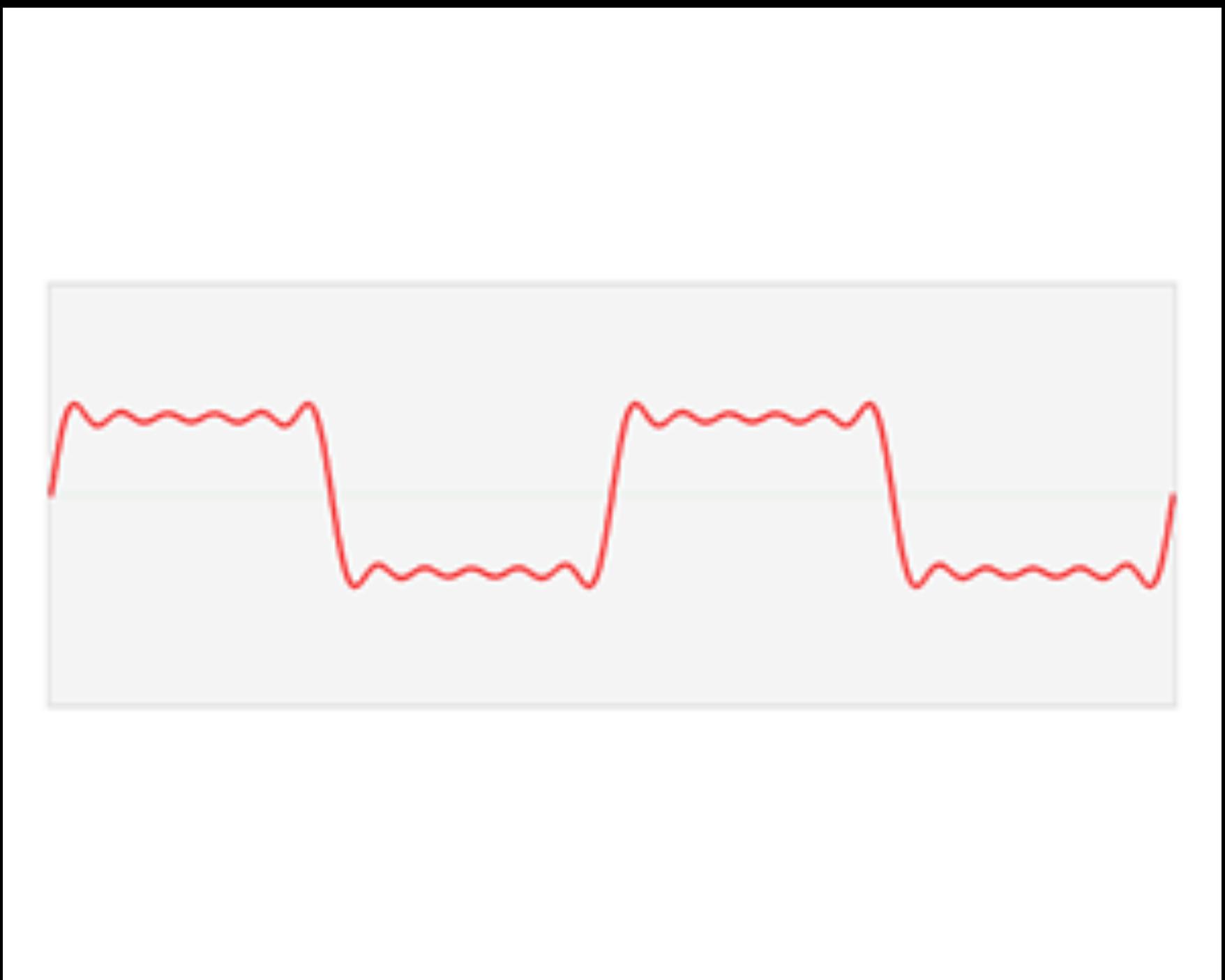
$N = 15, g = 7$



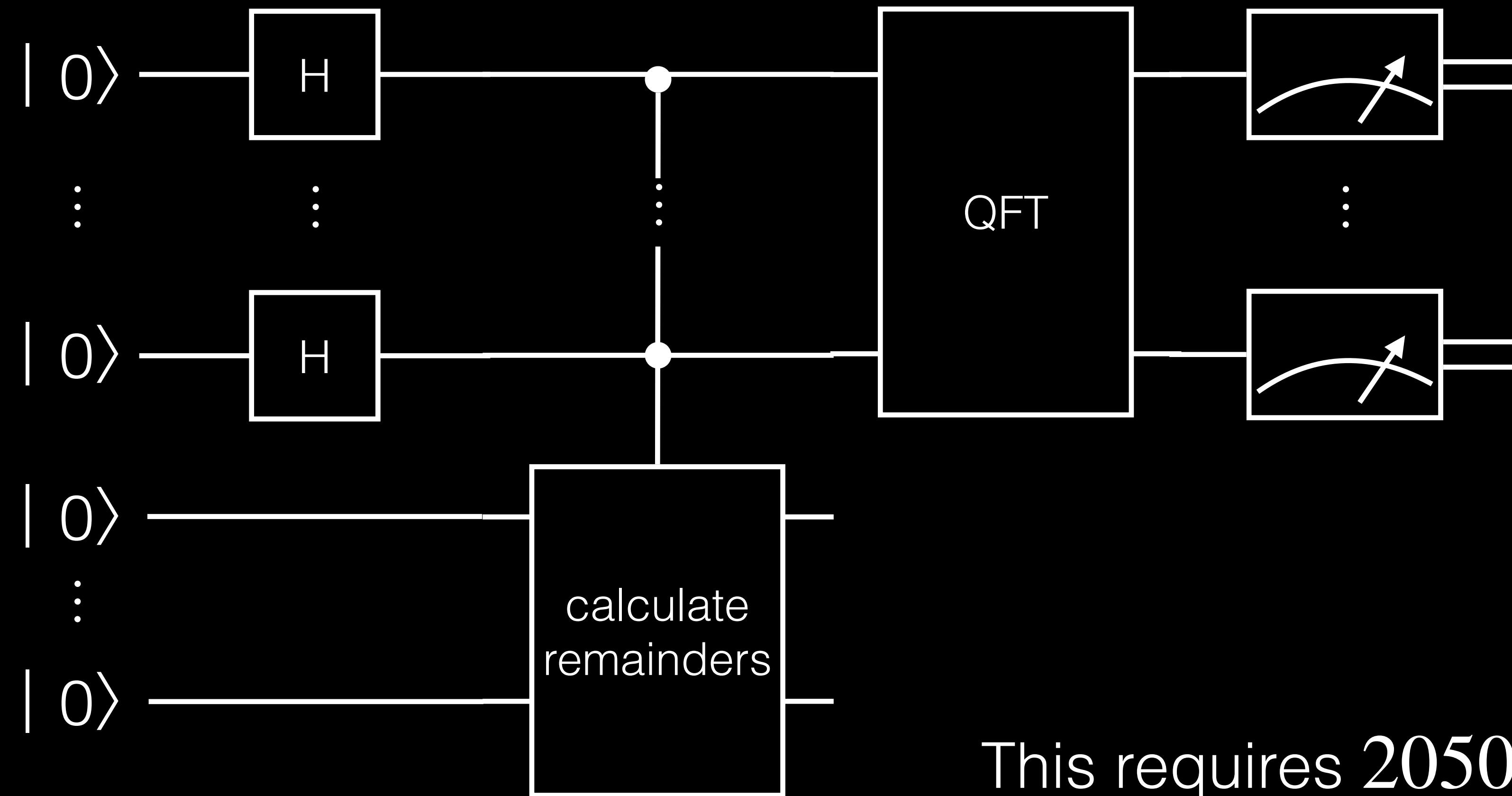
Can we use a Fourier Transform?

The trouble starts

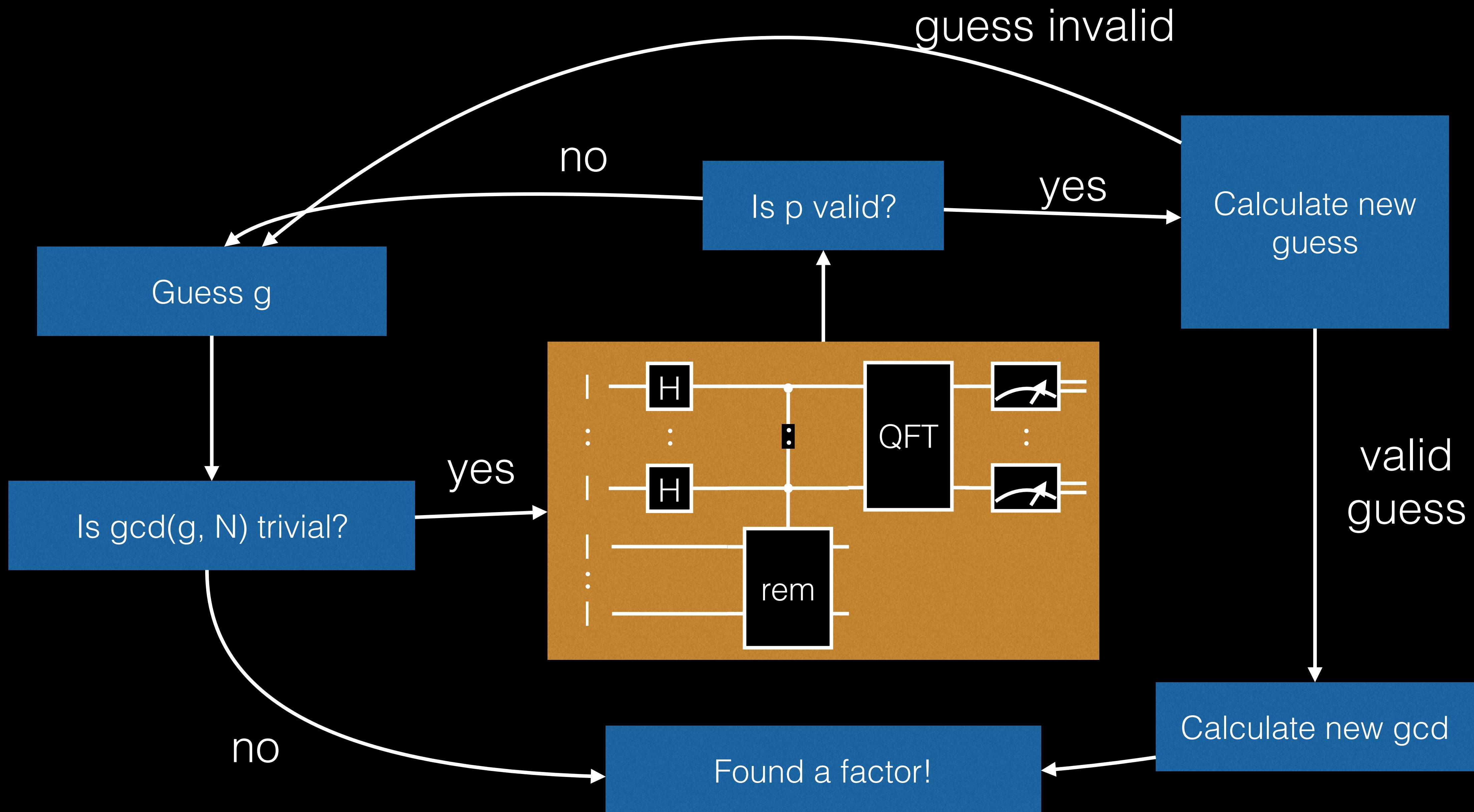
- Fourier Transforms can help us find the composite wave functions
- And therefore the dominant wave
- BUT, 'Fast' Fourier Transforms are not fast enough for large N
- Enter the Quantum Fourier Transform



*By Lucas V. Barbosa - Own work, Public Domain,
<https://commons.wikimedia.org/w/index.php?curid=24830373>*

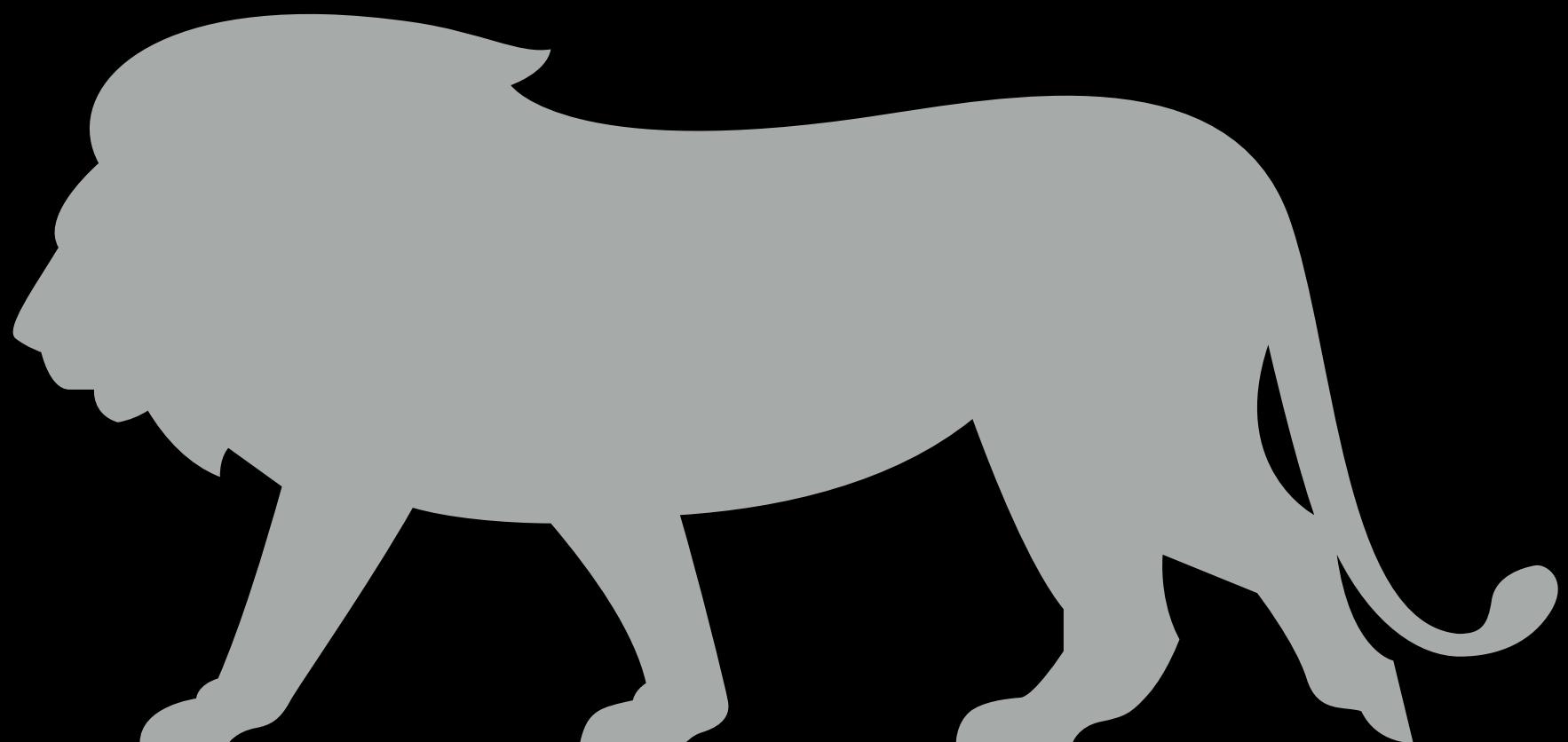


This requires 2050 completely noise-free qubits and $4.81 \cdot 10^{12}$ gates for RSA-1024



Conclusions

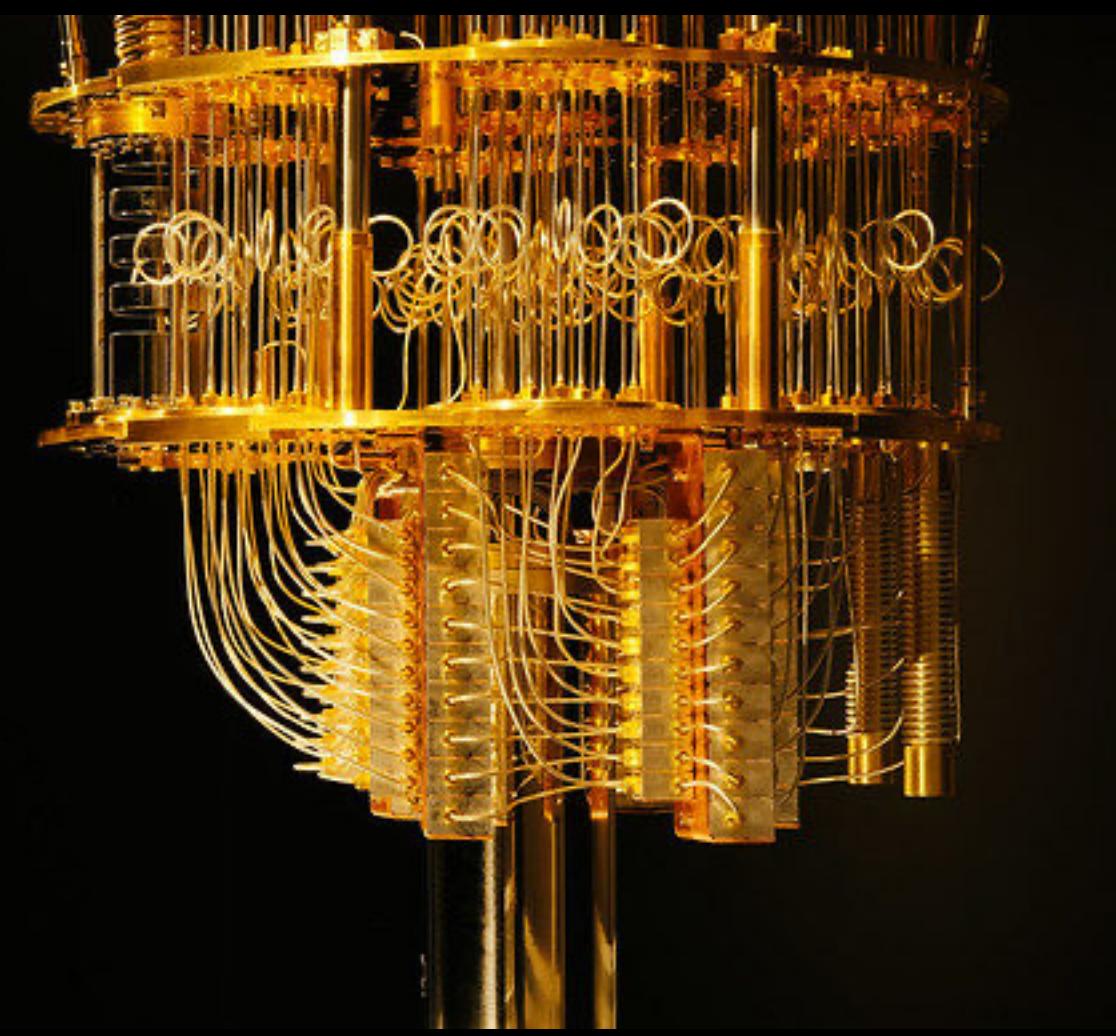
- We can break RSA
- This allows for the Harvesting Attack
- Discrete logarithmic problems 'reducible' to integer factorization
 - so, DHE and ECDHE will also be broken
- But it needs a sh*t-ton of qubits and gates



Interlude: Symmetric cryptography and hashing

- AES
 - Normally, search space of AES-128 is 2^{127}
 - Grover's speeds this up to 2^{64}
 - Therefore, why worry? Use AES-256 and be happy! For now
- Hashing
 - Also attackable by Grover's
 - But doubling the hash size will protect you for a generation

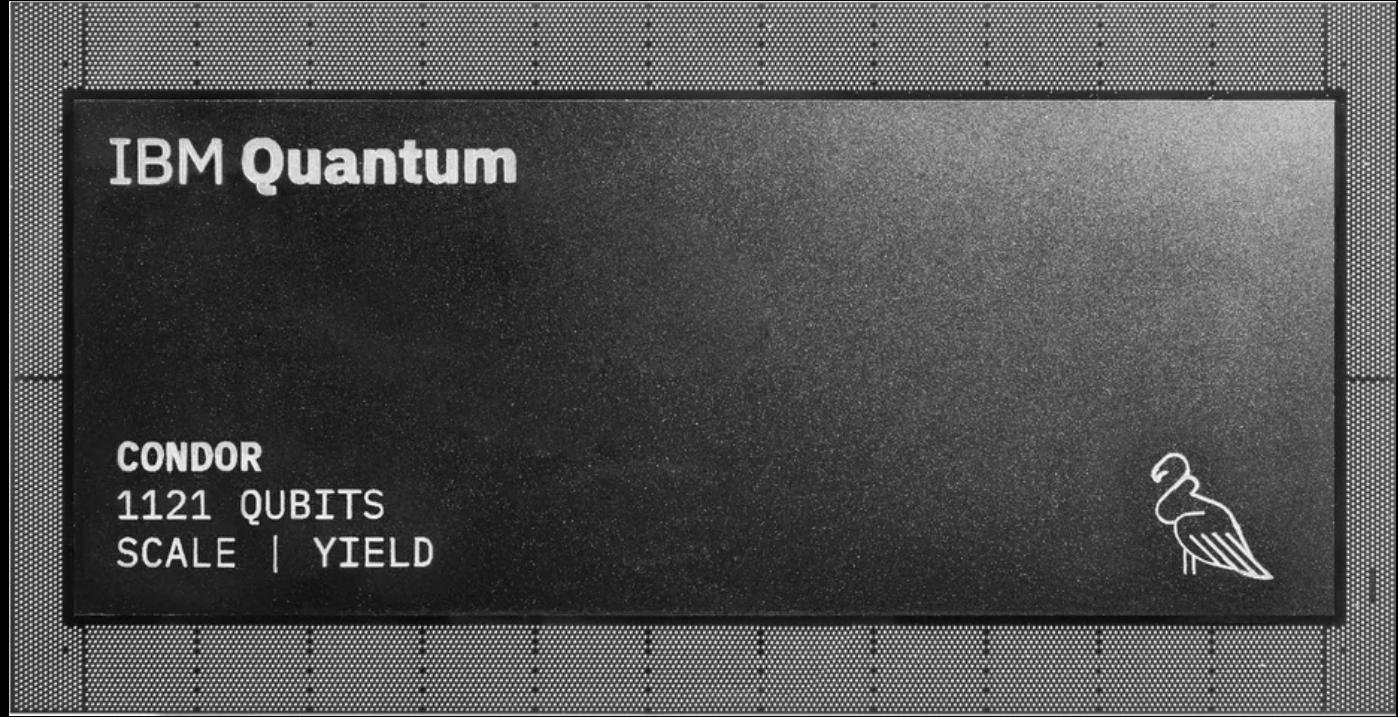




How real is the threat?

Quantum Computers are not there yet

- Three criteria: Qubit count, gate count, gate performance
- IBM's Condor QPU is 1121 qubits with the maybe >1000 gates
 - IBM Heron has better gate performance but only 133 qubits
 - These are noisy qubits
 - Noise mitigation requires 10-100x number of qubits!
 - Horizontal scaleout will need a rethink of algorithms

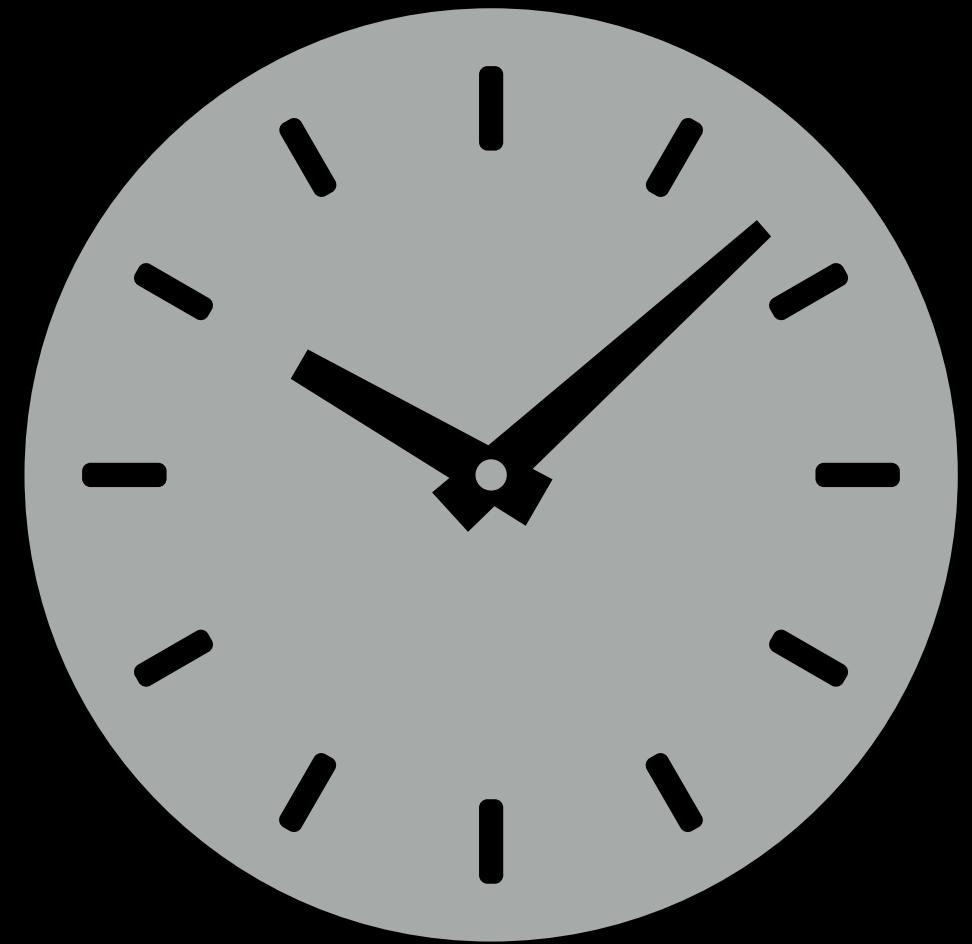


Remember what we said:

"This requires 2050 completely noise-free qubits and $4.81 \cdot 10^{12}$ gates for RSA-1024"

The 'if's

- 5 years from usable machines
- 10 years away from breaking Shor's
- But this could be brought forward if
 - There is a major breakthrough in noise reduction
 - Horizontal scaling does not impact performance
 - A new approach to factoring is found

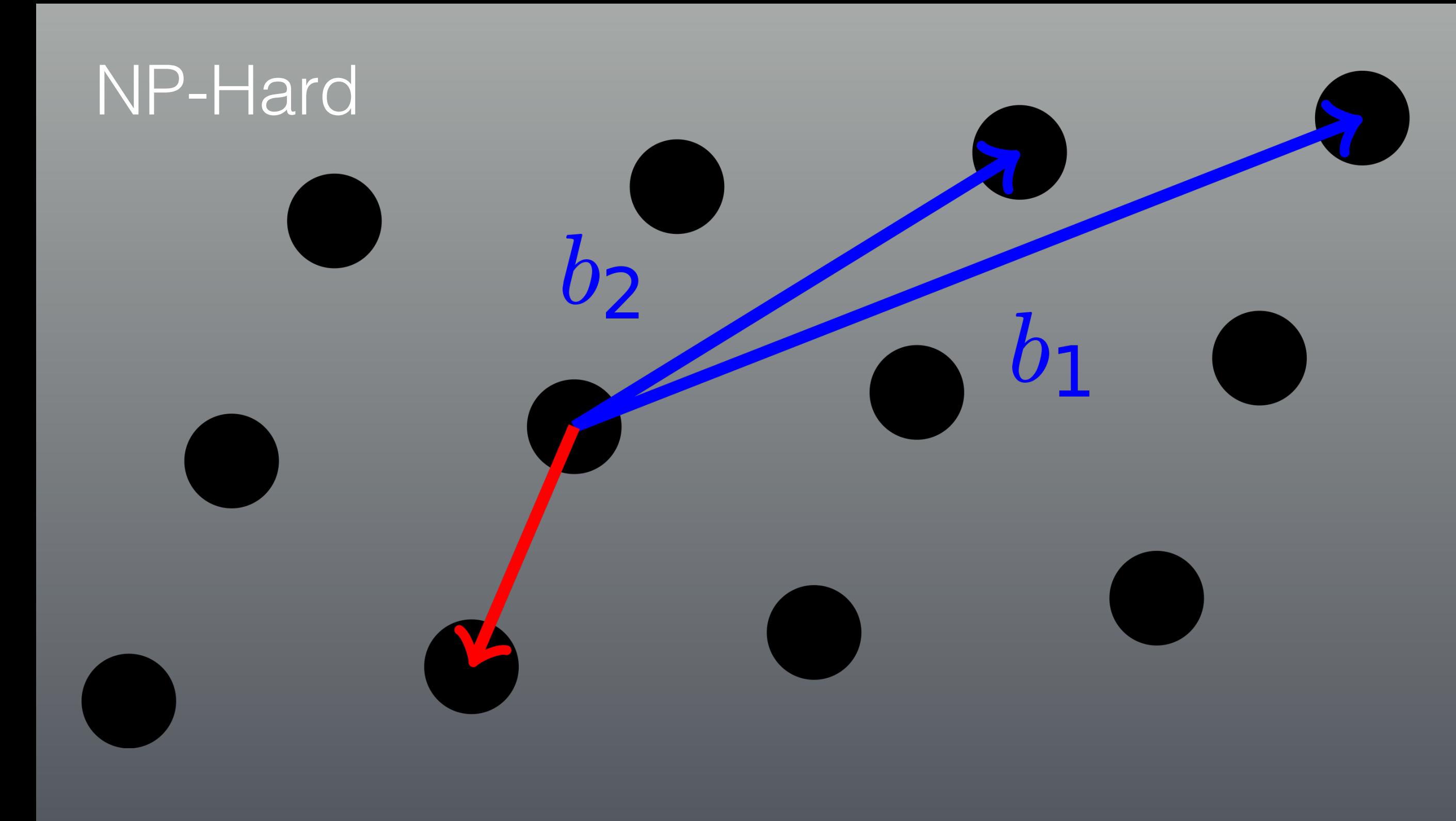


What can we do about it?

Post-Quantum Cryptography

The approaches

- Learning with Errors
- Lattice-based
- Isogenies
- Code-based
- Hash-based



Key Establishment Candidates

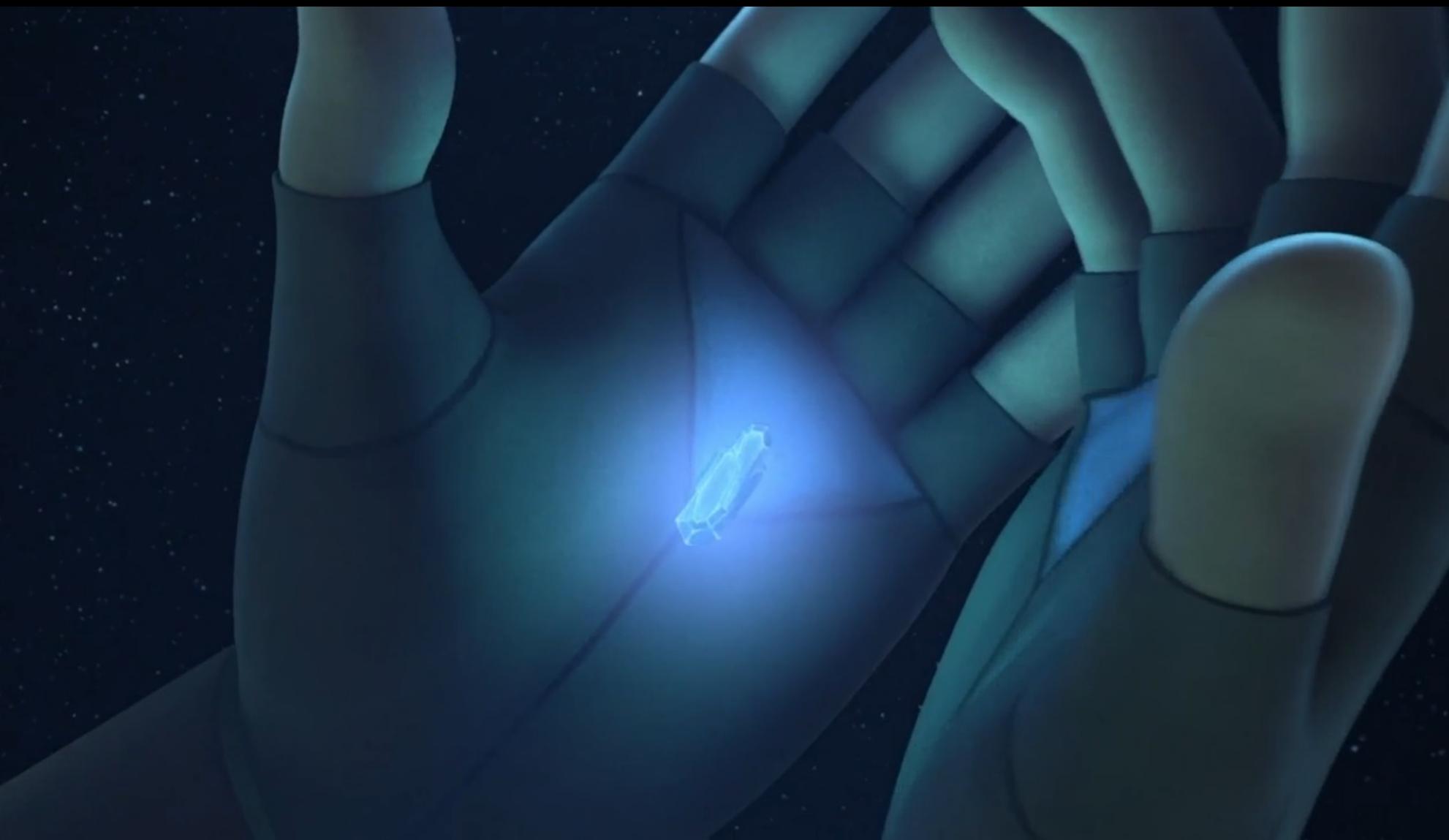
Algorithm	Standard	Assumption	Status
ML-KEM CRYSTALS KYBER	FIPS 203	Lattices&LWE	Will be standardized
Classic McEliece		Code	Round 4
BIKE		Code	Round 4
HQC		Code	Round 4
SIKE		Isogenies	Retracted

Digital Signature Candidates

Algorithm	Standard	Assumption	Status
ML-DSA CRYSTALS-DILITHIUM	FIPS 204	Lattice	Will be standardized
FALCON		Lattice	Will be standardized (probably as FN-DSA and FIPS-206)
SLH-DSA SPHINCS+	FIPS 205	Hash-based	Will be standardized
XMSS	RFC 8391		
Leighton-Micali	RFC 8554		

ML-KEM

- Was CRYSTALS-KYBER
- First implementation bugs found
- So far, no protocol weaknesses
- Approximate 3× slower than ECDH
- Nearly 25× the key size



ML-DSA



- Was CRYSTALS-Dilithium
- Approximately 5× slower than ECDSA for signing.
- Verification is fast though
- About 41× larger public keys

SLH-DSA

- Was SPHINCS+
- Also very slow signing
- But fast verification
- Signatures can be 40k in size



Falcon (FN-DSA?)

- Was and still is Falcon
- FFT over NTRU-Lattice
- Uniquely, it relies on floating point operations
- Hard to implement
- Not yet standardized but expected this year



Others

- SIKE vulnerability demonstrates risk
 - Follow German BSI advise: go hybrid
- What's up with FrodoKEM and NTRU Prime?
 - BSI still recommends FrodoKEM-976, FrodoKEM-1344 and Classic McEliece



Implementations

- Open Quantum Safe liboqc supports all candidates ++ ->

- OpenSSL somewhat?

- OpenSSH > 9.0

- Wireguard (using Rosenpass)

- AWS, Cloudflare,..

- Chrome, Signal, iMessage, ...

Cloudflare Research: Post-Quantum Key Agreement

On essentially all domains served through Cloudflare, including this one, we have enabled hybrid post-quantum key agreement. Read [our blog](#) for the details.

You are using X25519 which is **not post-quantum secure**.

Deployed key agreements

Available with TLSv1.3 including HTTP/3 (QUIC)

Key agreement	TLS identifier
X25519Kyber768Draft00	0x6399 (recommended) and 0xfef31 (obsolete)
Curve25519	0xfe30
Hybrid of X25519 and Kyber/xDraft00	(in that order).

Turn on TLS 1.3 hybridized Kyber support (`enable-tls13-kyber`) in chrome://flags.

Upstream only supports `0x6399`; for the others use our old [fork](#).

Work of Firefox.

[new!]

You can reach us directly at ask-research@cloudflare.com with questions and feedback.

 Cloudflare Research

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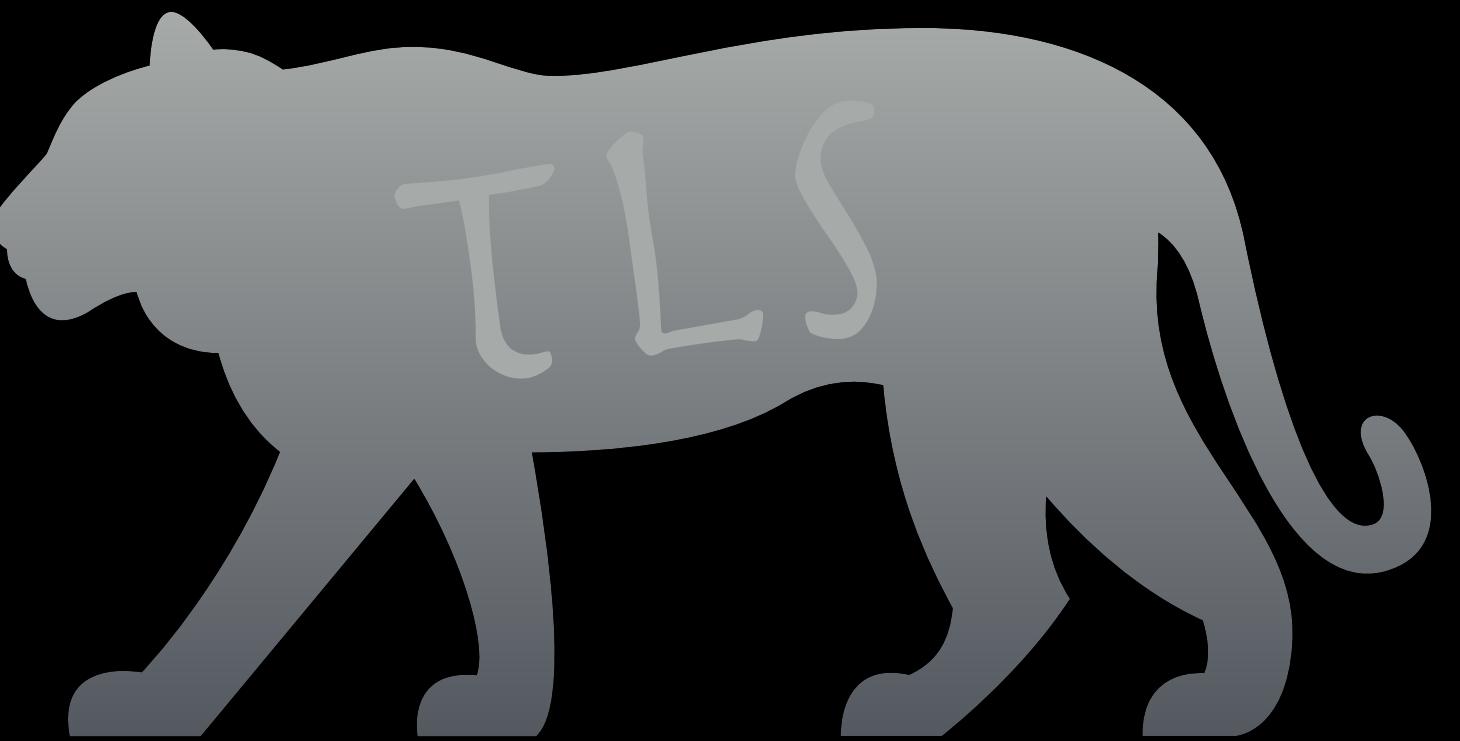
[new!]

You can reach us directly at ask-research@cloudflare.com with questions and feedback.

 Cloudflare Research

TLS 1.3

- In draft mode:
 - ML-KEM-512, ML-KEM-768, and ML-KEM-1024
 - Hybrid approach being discussed
- Cloudflare:
 - Two percent of all TLS 1.3 are ML-KEM
- Implementations
 - BoringSSL, WolfSSL
- But no OpenSSL support yet

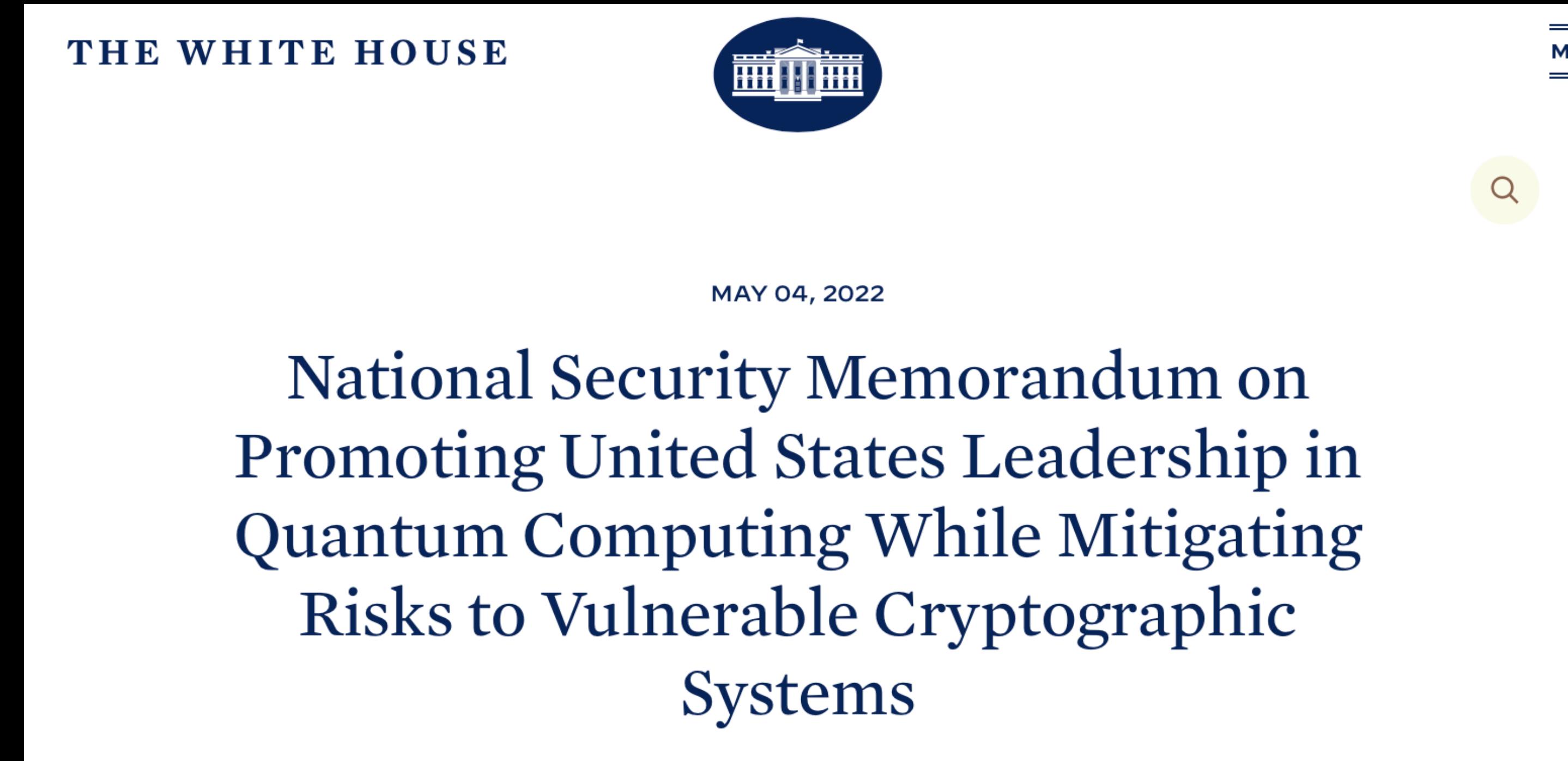


OpenSSH

- From 9.9 onwards
- Hybrid approach
 - ML-KEM and ECDH



PQC by 2035 (USA)



"the goal of mitigating as much of the quantum risk as is feasible by 2035"

Name confusion

- ML-KEM = FIPS 203 = CRYSTALS-Kyber = PQ3 (Apple)
- ML-DSA = FIPS 204 = CRYSTALS-Dilithium
- SLH-DSA = FIPS 205 = SPHINCS+ ????
- (FN-DSA = FIPS 206 = Falcon ???)



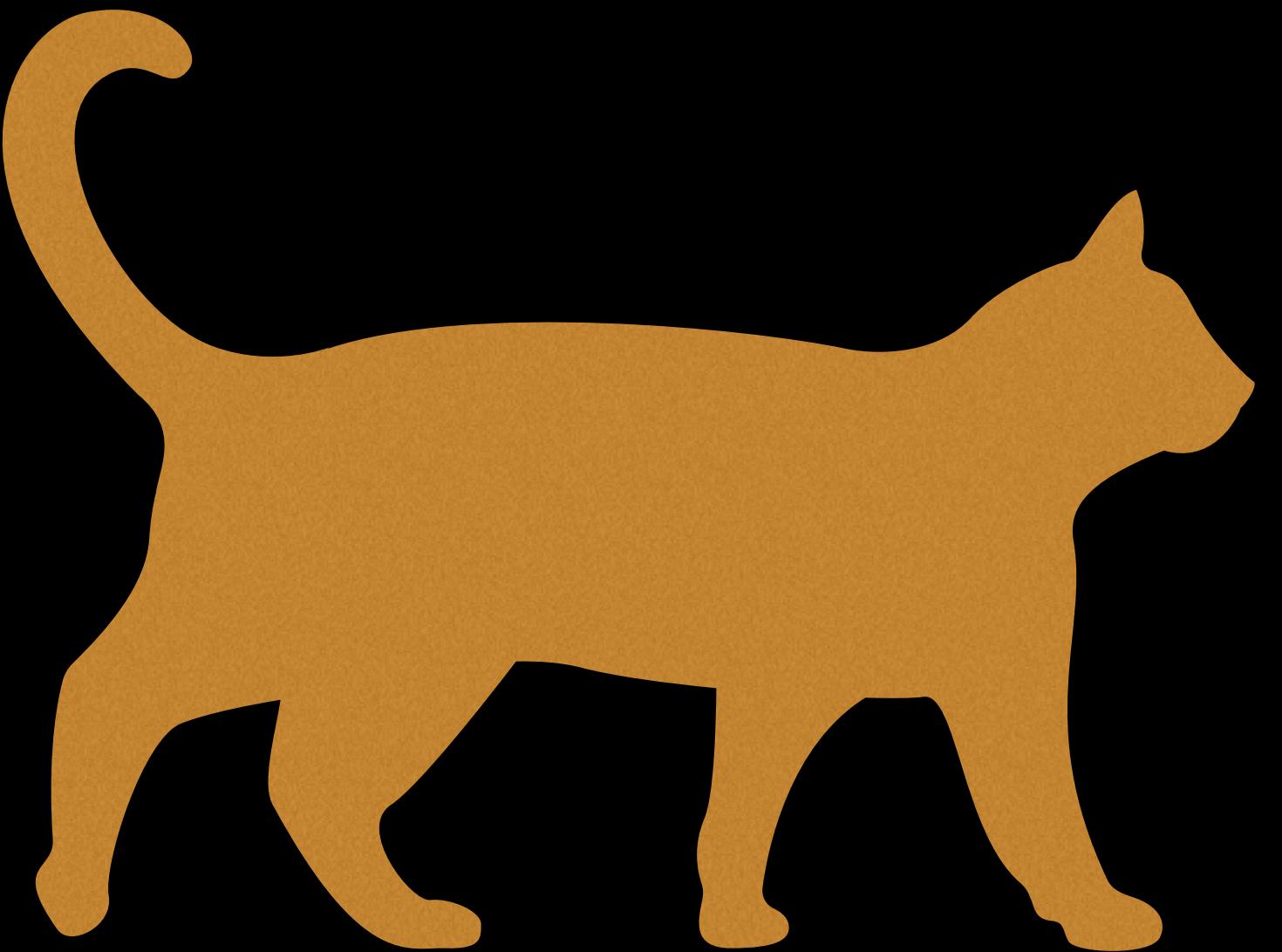
Quantum Key Distribution/BB84

- Provably secure
 - less sure about practical implementations
 - Limited usability
- Quantum Digital Signatures schemes also becoming usable

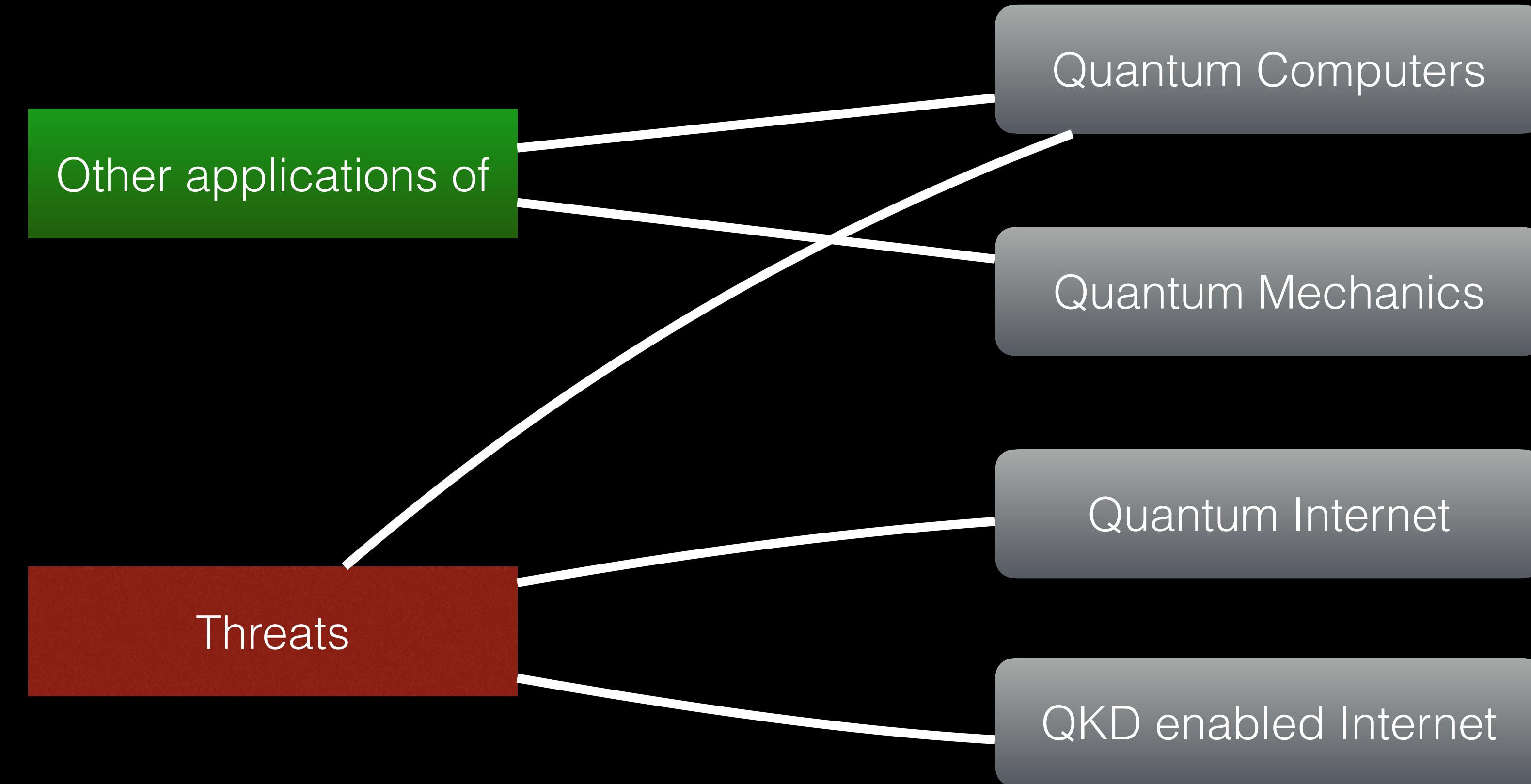


Main takeaway IMHO

- Threat to asymmetric cryptography is theoretically real
- > 10 years until sufficiently large quantum computers exist
- But the harvesting attack needs to be considered!
- Start planning now
 - PQC needs more space and time
 - Challenging in OT environments
 - Otherwise, wait until vendors do the work for you



What I'm watching



Will AI/ML eat quantum computer's lunch?

[https://www.trendmicro.com/vinfo/us/security/news/security-technology/...](https://www.trendmicro.com/vinfo/us/security/news/security-technology/)

diving-deep-into-quantum-computing-modern-cryptography

diving-deep-into-quantum-computing-computing-with-quantum-mechanics

post-quantum-cryptography-quantum-computing-attacks-on-classical-cryptography

post-quantum-cryptography-migrating-to-quantum-resistant-cryptography

the-realities-of-quantum-machine-learning

