

Group1_Project

Group_1

April 29, 2020

Introduction:

The background of this data comes from ...

Read In Data:

```
## Loading required package: ggplot2
## Loading required package: carData
##
## Attaching package: 'olsrr'
##
## The following object is masked from 'package:datasets':
##
##     rivers
##
## Loading required package: KernSmooth
## KernSmooth 2.23 loaded
## Copyright M. P. Wand 1997-2009
##
## Attaching package: 'MPV'
##
## The following object is masked from 'package:olsrr':
##
##     cement
```

Performing variable selection:

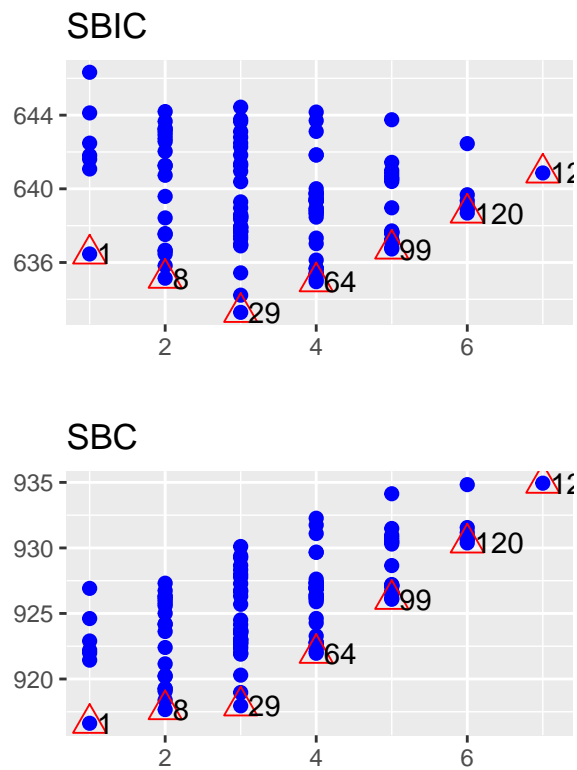
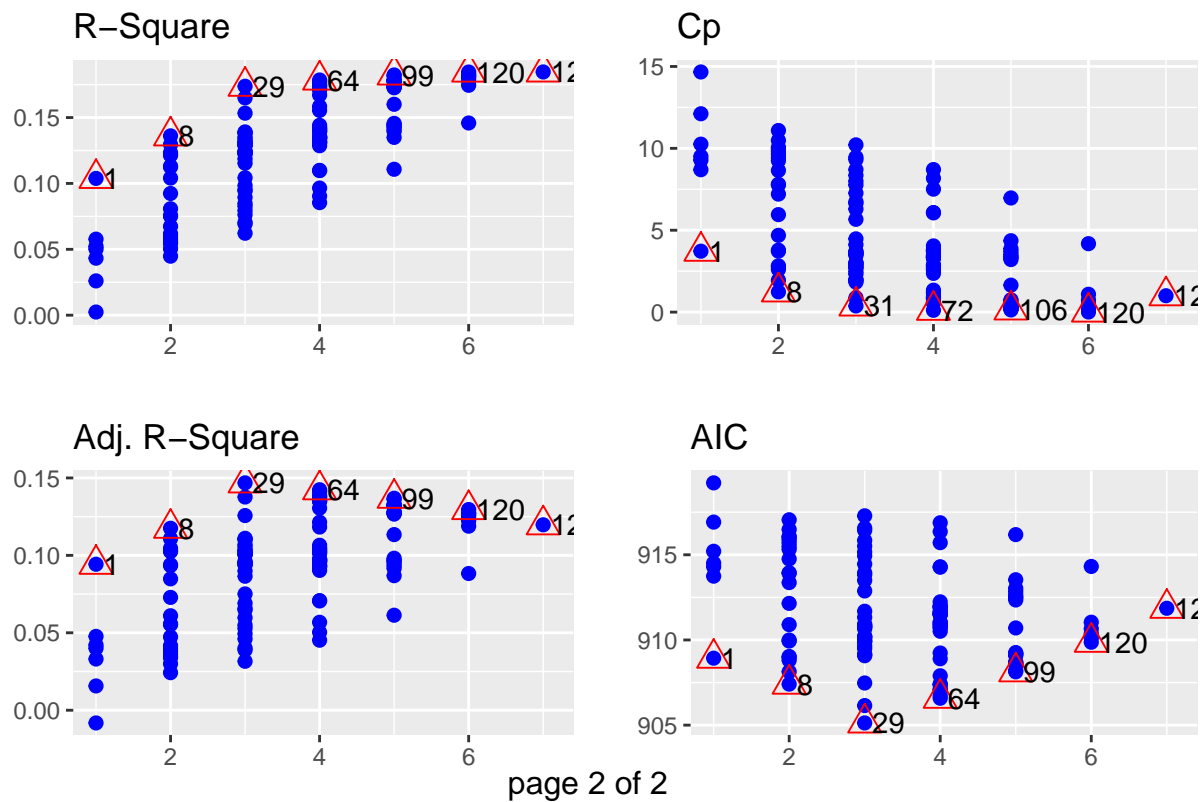
##	Index	N	Predictors	R-Square	Adj. R-Square	Mallow's Cp
## 1	1	1	x1	0.10381011	0.094276177	4.719250
## 2	2	1	x2	0.05771212	0.047687785	9.694270
## 5	3	1	x5	0.05223762	0.042155039	10.285094
## 7	4	1	x7	0.05016001	0.040055334	10.509314
## 6	5	1	x6	0.04324888	0.033070675	11.255183
## 4	6	1	x4	0.02603395	0.015672614	13.113064
## 3	7	1	x3	0.00239633	-0.008216475	15.664101
## 12	8	2	x1 x6	0.13609838	0.117519847	3.234613
## 13	9	2	x1 x7	0.12950341	0.110783053	3.946359
## 11	10	2	x1 x5	0.12339323	0.104541471	4.605787
## 27	11	2	x5 x7	0.12181247	0.102926715	4.776387
## 8	12	2	x1 x2	0.12135810	0.102462571	4.825424
## 26	13	2	x5 x6	0.11302532	0.093950600	5.724719
## 10	14	2	x1 x4	0.11249746	0.093411385	5.781688
## 9	15	2	x1 x3	0.10408452	0.084817518	6.689635
## 16	16	2	x2 x5	0.09237954	0.072860824	7.952868
## 23	17	2	x4 x5	0.08077039	0.061002009	9.205760

## 18	18 2	x2 x7	0.07548215	0.055600043	9.776481
## 21	19 2	x3 x6	0.07523058	0.055343063	9.803631
## 17	20 2	x2 x6	0.06739014	0.047334010	10.649793
## 14	21 2	x2 x3	0.06184974	0.041674465	11.247728
## 15	22 2	x2 x4	0.06017702	0.039965774	11.428252
## 19	23 2	x3 x4	0.05812812	0.037872815	11.649374
## 28	24 2	x6 x7	0.05636761	0.036074437	11.839374
## 20	25 2	x3 x5	0.05494962	0.034625957	11.992407
## 22	26 2	x3 x7	0.05435293	0.034016434	12.056804
## 25	27 2	x4 x7	0.05042085	0.029999793	12.481164
## 24	28 2	x4 x6	0.04477933	0.024236954	13.090012
## 36	29 3	x1 x3 x6	0.17375716	0.146814459	1.170374
## 57	30 3	x3 x5 x6	0.16492514	0.137694443	2.123549
## 39	31 3	x1 x4 x6	0.15332894	0.125720104	3.375043
## 43	32 3	x1 x6 x7	0.13908854	0.111015343	4.911906
## 41	33 3	x1 x5 x6	0.13863843	0.110550554	4.960483
## 32	34 3	x1 x2 x6	0.13819982	0.110097641	5.007819
## 33	35 3	x1 x2 x7	0.13525894	0.107060865	5.325207
## 37	36 3	x1 x3 x7	0.13378473	0.105538584	5.484307
## 31	37 3	x1 x2 x5	0.13170370	0.103389686	5.708899
## 40	38 3	x1 x4 x7	0.13131963	0.102993099	5.750348
## 63	39 3	x5 x6 x7	0.13122129	0.102891547	5.760961
## 42	40 3	x1 x5 x7	0.12979032	0.101413916	5.915395
## 34	41 3	x1 x3 x4	0.12906703	0.100667039	5.993455
## 52	42 3	x2 x5 x7	0.12900997	0.100608120	5.999613
## 58	43 3	x3 x5 x7	0.12886586	0.100459314	6.015165
## 61	44 3	x4 x5 x7	0.12478309	0.096243412	6.455789
## 38	45 3	x1 x4 x5	0.12385098	0.095280903	6.556385
## 35	46 3	x1 x3 x5	0.12369898	0.095123946	6.572789
## 29	47 3	x1 x2 x3	0.12350282	0.094921386	6.593960
## 30	48 3	x1 x2 x4	0.12273957	0.094133250	6.676332
## 60	49 3	x4 x5 x6	0.12237581	0.093757629	6.715589
## 51	50 3	x2 x5 x6	0.11863478	0.089894607	7.119332
## 54	51 3	x3 x4 x5	0.11536571	0.086518943	7.472138
## 46	52 3	x2 x3 x6	0.10430631	0.075098911	8.665699
## 48	53 3	x2 x4 x5	0.09846917	0.069071426	9.295659
## 44	54 3	x2 x3 x4	0.09529396	0.065792677	9.638336
## 45	55 3	x2 x3 x5	0.09429931	0.064765588	9.745682
## 47	56 3	x2 x3 x7	0.08944975	0.059757897	10.269059
## 59	57 3	x3 x6 x7	0.08485610	0.055014456	10.764818
## 55	58 3	x3 x4 x6	0.08273400	0.052823147	10.993842
## 50	59 3	x2 x4 x7	0.07942053	0.049401637	11.351440
## 53	60 3	x2 x6 x7	0.07619390	0.046069787	11.699667
## 49	61 3	x2 x4 x6	0.07049820	0.040188359	12.314362
## 62	62 3	x4 x6 x7	0.06917229	0.038819216	12.457458
## 56	63 3	x3 x4 x7	0.06218192	0.031600897	13.211878
## 97	64 4	x3 x5 x6 x7	0.17848419	0.142373608	2.660220
## 66	65 4	x1 x2 x3 x6	0.17726370	0.141099463	2.791939
## 79	66 4	x1 x3 x6 x7	0.17492850	0.138661621	3.043960
## 77	67 4	x1 x3 x5 x6	0.17404349	0.137737707	3.139473
## 75	68 4	x1 x3 x4 x6	0.17397322	0.137664349	3.147057
## 98	69 4	x4 x5 x6 x7	0.17157653	0.135162314	3.405714
## 87	70 4	x2 x3 x5 x6	0.17154573	0.135130155	3.409038
## 82	71 4	x1 x4 x6 x7	0.17140111	0.134979177	3.424646

## 94	72 4	x3 x4 x5 x6	0.16711214	0.130501683	3.887523
## 80	73 4	x1 x4 x5 x6	0.15840802	0.121414967	4.826895
## 69	74 4	x1 x2 x4 x6	0.15542635	0.118302235	5.148685
## 67	75 4	x1 x2 x3 x7	0.14413821	0.106517911	6.366932
## 64	76 4	x1 x2 x3 x4	0.14232843	0.104628578	6.562249
## 88	77 4	x2 x3 x5 x7	0.14199863	0.104284284	6.597841
## 73	78 4	x1 x2 x6 x7	0.14085571	0.103091131	6.721188
## 71	79 4	x1 x2 x5 x6	0.14043845	0.102655525	6.766220
## 70	80 4	x1 x2 x4 x7	0.13945870	0.101632710	6.871957
## 83	81 4	x1 x5 x6 x7	0.13934523	0.101514250	6.884204
## 72	82 4	x1 x2 x5 x7	0.13547819	0.097477231	7.301545
## 91	83 4	x2 x4 x5 x7	0.13511568	0.097098785	7.340668
## 65	84 4	x1 x2 x3 x5	0.13505935	0.097039977	7.346748
## 84	85 4	x2 x3 x4 x5	0.13501751	0.096996305	7.351262
## 76	86 4	x1 x3 x4 x7	0.13493486	0.096910016	7.360183
## 93	87 4	x2 x5 x6 x7	0.13396382	0.095896297	7.464980
## 78	88 4	x1 x3 x5 x7	0.13378493	0.095709538	7.484287
## 68	89 4	x1 x2 x4 x5	0.13182026	0.093658510	7.696319
## 81	90 4	x1 x4 x5 x7	0.13139466	0.093214208	7.742250
## 74	91 4	x1 x3 x4 x5	0.13104014	0.092844106	7.780511
## 95	92 4	x3 x4 x5 x7	0.13071638	0.092506115	7.815452
## 90	93 4	x2 x4 x5 x6	0.12860550	0.090302449	8.043264
## 85	94 4	x2 x3 x4 x6	0.10990566	0.070780635	10.061402
## 89	95 4	x2 x3 x6 x7	0.10973595	0.070603461	10.079718
## 86	96 4	x2 x3 x4 x7	0.09650171	0.056787504	11.507992
## 92	97 4	x2 x4 x6 x7	0.09033265	0.050347271	12.173774
## 96	98 4	x3 x4 x6 x7	0.08541813	0.045216728	12.704163
## 117	99 5	x2 x3 x5 x6 x7	0.18231009	0.136882869	4.247319
## 119	100 5	x3 x4 x5 x6 x7	0.18160687	0.136140585	4.323212
## 112	101 5	x1 x3 x5 x6 x7	0.17867047	0.133041053	4.640116
## 104	102 5	x1 x2 x3 x6 x7	0.17814076	0.132481910	4.697285
## 111	103 5	x1 x3 x4 x6 x7	0.17784127	0.132165790	4.729606
## 102	104 5	x1 x2 x3 x5 x6	0.17778880	0.132110400	4.735269
## 100	105 5	x1 x2 x3 x4 x6	0.17739636	0.131696157	4.777622
## 109	106 5	x1 x3 x4 x5 x6	0.17409726	0.128213775	5.133670
## 114	107 5	x2 x3 x4 x5 x6	0.17351105	0.127594995	5.196935
## 113	108 5	x1 x4 x5 x6 x7	0.17324210	0.127311108	5.225961
## 118	109 5	x2 x4 x5 x6 x7	0.17316521	0.127229943	5.234259
## 107	110 5	x1 x2 x4 x6 x7	0.17262053	0.126654999	5.293043
## 105	111 5	x1 x2 x4 x5 x6	0.16007770	0.113415354	6.646699
## 101	112 5	x1 x2 x3 x4 x7	0.14560024	0.098133582	8.209146
## 103	113 5	x1 x2 x3 x5 x7	0.14430710	0.096768602	8.348705
## 115	114 5	x2 x3 x4 x5 x7	0.14410617	0.096556515	8.370390
## 99	115 5	x1 x2 x3 x4 x5	0.14277288	0.095149151	8.514282
## 108	116 5	x1 x2 x5 x6 x7	0.14107797	0.093360085	8.697201
## 106	117 5	x1 x2 x4 x5 x7	0.13945973	0.091651937	8.871846
## 110	118 5	x1 x3 x4 x5 x7	0.13494599	0.086887438	9.358981
## 116	119 5	x2 x3 x4 x6 x7	0.11074722	0.061344289	11.970578
## 126	120 6	x2 x3 x4 x5 x6 x7	0.18455359	0.129579671	6.005195
## 123	121 6	x1 x2 x3 x5 x6 x7	0.18233077	0.127207007	6.245087
## 125	122 6	x1 x3 x4 x5 x6 x7	0.18183780	0.126680797	6.298290
## 122	123 6	x1 x2 x3 x4 x6 x7	0.18023945	0.124974691	6.470788
## 120	124 6	x1 x2 x3 x4 x5 x6	0.17778881	0.122358838	6.735268
## 124	125 6	x1 x2 x4 x5 x6 x7	0.17450663	0.118855394	7.089489

```
## 121 126 6 x1 x2 x3 x4 x5 x7 0.14587398 0.088292448 10.179603
## 127 127 7 x1 x2 x3 x4 x5 x6 x7 0.18460172 0.119740493 8.000000
```

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Interpretation of variable Selection: In looking for the “best” model, certain criteria must be met inorder for proper variable selection of the regressor

equation. These criteria help us to be able to explain the data in the simplest way with redundant predictors removed in order to minimize cost and to avoid multi-collinearity in our regression model.

The criteria for our variable selection include: 1) Large R^2 value 2) Maximum Adjusted R^2 value 3) Minimum MSres 4) Minimum Mallows' Cp Statistic value

Based on the above criteria, the “best” candidate models are: 1) Model 29: $y \sim x_1 + x_3 + x_6$ 2) Model 64: $Y \sim x_3 + x_5 + x_6 + x_7$ 3) Model 99: $Y \sim x_2 + x_3 + x_5 + x_6 + x_7$ 4) Model 120: $Y \sim x_2 + x_3 + x_4 + x_5 + x_6 + x_7$

Once we identified the “best” candidate models, we compare its predicted residual error sum of squares (PRESS) statistic with other candidate models and selected the model with the smallest value. We also compare candidate models by performing a variance inflation factor (VIF) in order to quantify the severity of multicollinearity in the model.

```
## [1] 68704.26
## [1] 69789.7
## [1] 71110.33
## [1] 77659.85

##      x1      x3      x6
## 1.010615 2.528279 2.523045

##      x3      x5      x6      x7
## 2.617428 1.060150 3.650110 1.820798

##      x2      x3      x5      x6      x7
## 1.564314 2.622358 1.184723 3.883741 1.878902

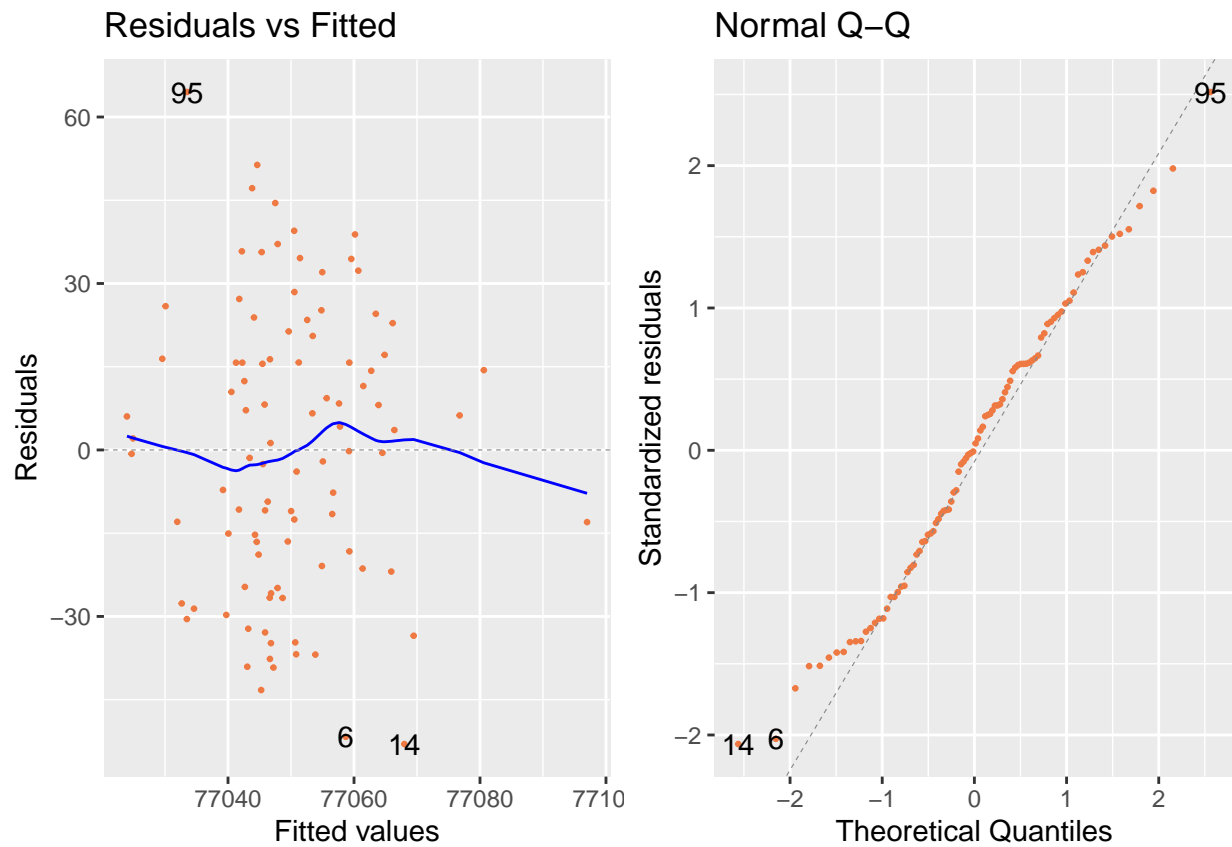
##      x2      x3      x4      x5      x6      x7
## 1.598317 6.222163 14.323819 1.290660 4.818502 4.102786
```

Interpretation of PRESS and Vif of candidate models:

The model with the lowest PRESS value is model 29, $Y = x_1 + x_3 + x_6$ and the same model does not show any evidence of multicollinearity in the variance inflation factor test of each regressor.

Plot of model:

```
autoplot(fit29, size = 0.5, colour = 'sienna2')[1:2]
```



other CSV links

```
#TX_gz_num <- read.csv("CSV/DATA/texas_Gazetteer_numeric.csv") #products <- read.csv("CSV/OTHER/products.csv")
#test_data <- read.csv("CSV/OTHER/test_data.csv") #TX_gz_obj <- read.csv("CSV/OTHER/texas_Gazetteer_object.csv")
#train_dat <- read.csv("CSV/OTHER/train_data.csv")
```