

# Good Node-subsets

**Time Limit**

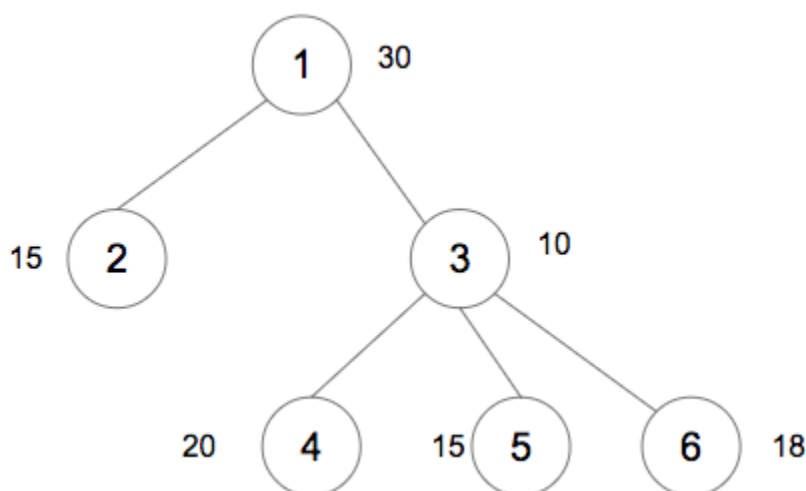
**Memory Limit**

1 second ([See Below](#))

512 MB

## Description

Alice and Bob like to play a game using trees. Let there be a tree with  $n$  nodes that are labeled from 1 to  $n$ . Let  $p[i]$  be the parent of node  $i$ , and let  $p[i] = 0$  if node  $i$  is the root. Lastly, let  $v[i]$  be the integer value of node  $i$  assigned to it.



For instance, the tree above describes the case where  $n = 6$ ,  $v = [30, 15, 10, 20, 15, 18]$  and  $p = [0, 1, 1, 3, 3, 3]$ . The number next to each node is the integer value assigned to it. In this tree,  $p[1] = 0$  indicates that node 1 is the root node. Notice that every node except for the root node has a parent node.

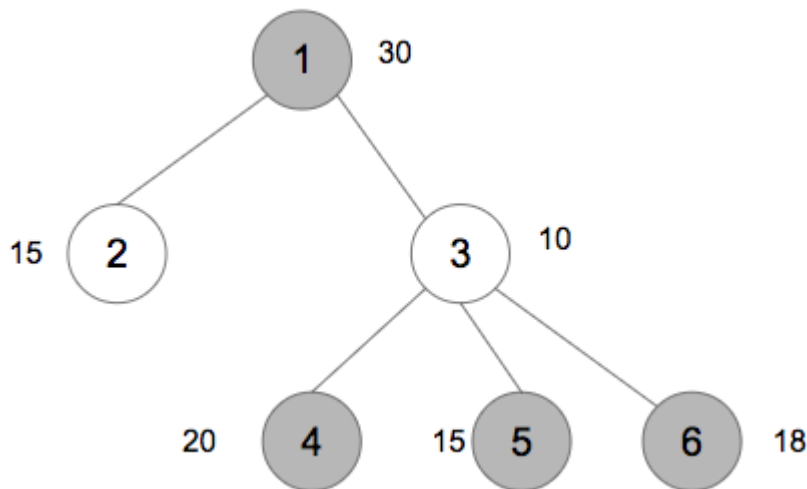
If a node-subset  $S$  of the tree satisfies the following conditions, then we call it a "good node-subset":

- Condition 1: If  $x$  is in  $S$ , then child/parent node(s) of  $x$  (that are connected to  $x$ ) are NOT in  $S$ .
- Condition 2: If  $x$  with 1 or more child node(s) is NOT in  $S$ , then at least one child node of  $x$  is in  $S$ .

In the tree above, consider the following node-subsets:

- $S = \{\}$ : Condition 2 is not satisfied -- Node 3 is not in  $S$ , and thus at least one of  $\{4, 5, 6\}$  must be in  $S$ . Hence it is not a good node-subset.
- $S = \{3\}$ : This is a good node-subset as it satisfies both conditions.
- $S = \{1, 2, 3\}$ : Condition 2 is satisfied, but condition 1 is not.
- $S = \{1, 4, 6\}$ : This is a good node-subset as it satisfies both conditions.
- $S = \{2, 3\}$ : This is a good node-subset as it satisfies both conditions.

Let  $\text{Score}(S)$  be the score of a good node-subset  $S$  where it is the sum of the values assigned to the nodes in  $S$ . In the above example, if  $S = \{1, 4, 5, 6\}$ , then  $\text{Score}(S) = 30 + 20 + 15 + 18 = 83$ , which is the highest score achievable.



Given a tree, compute the largest score of a good node-subset that Alice and Bob can achieve.

## Input

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The first line of the input will contain  $T$ , the number of test cases.

The first line of each test case will contain  $n$ , the number of nodes. The second line will contain  $n$  integers separated by whitespace, describing the values assigned to nodes ( $v[1], \dots, v[n]$ ). The third line will contain  $n$  integers separated by whitespace, describing the parent of each node ( $p[1], \dots, p[n]$ ).

## Output

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Output the answer for each test case in each line.

## Limit

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- $1 \leq T \leq 10$
- $2 \leq n \leq 100,000$
- $-10^9 \leq v[i] \leq 10^9$  ( $i = 1, 2, \dots, n$ )
- $0 \leq p[i] \leq n$  ( $i = 1, 2, \dots, n$ )
- For each test case:
  - Among  $i = 1, 2, \dots, n$ ,  $p[i] = 0$  holds for exactly one  $i$ .
  - For all  $i$ ,  $p[i] \neq i$ .

## Sample Input 1 Copy

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```
5
6
30 15 10 20 15 18
```

```
0 1 1 3 3 3
6
1 120 100 10 20 30
0 1 1 3 3 3
6
100 8 5 -20 -30 15
0 1 1 3 3 3
5
-1 -2 -3 -4 -5
2 3 4 5 0
2
-2022 2022
0 1
```

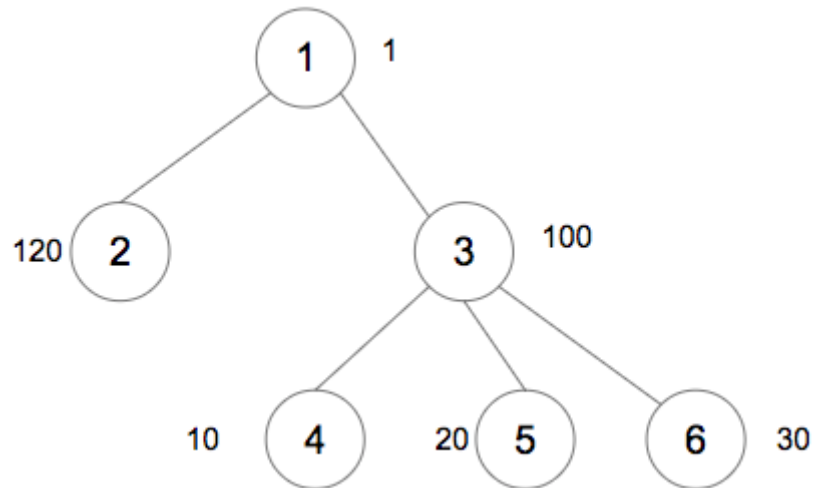
## Sample Output 1 Copy

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```
83
220
115
-6
2022
```

Case 1: Discussed in the problem statement.

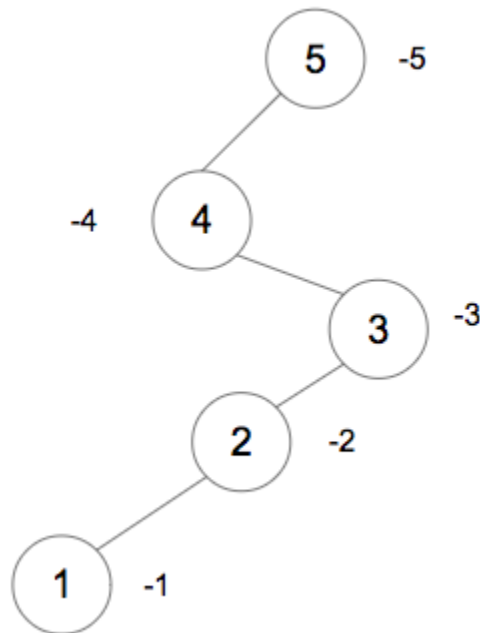
Case 2: It's the same tree as in Case 1, but the values assigned to nodes are different.



In this case,  $S = \{2, 3\}$  maximizes the score.

Case 3: No explanation.

Case 4: The tree is shown below.  $S = \{4, 2\}$  maximizes the score.



Case 5: No explanation.

## Time Limit

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- Java 8: 3 seconds
- Python 3: 6 seconds

- PyPy3: 6 seconds
- Java 8 (OpenJDK): 3 seconds
- Java 11: 3 seconds
- Kotlin (JVM): 3 seconds
- Java 15: 3 seconds