

# Bipartite Graph Game

**Time Limit**

**Memory Limit**

1 second ([See Below](#))

512 MB

## Description

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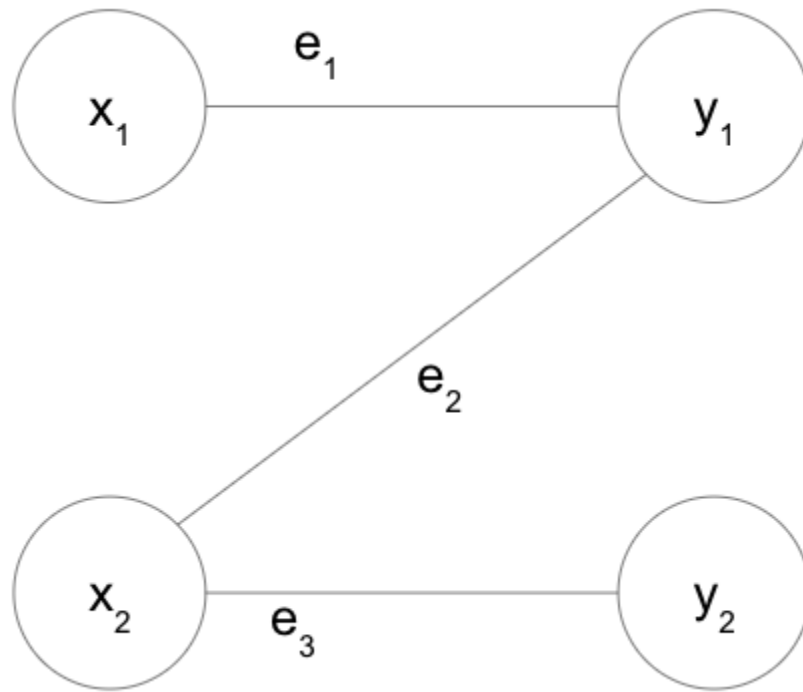
Bob likes to play a game using bipartite graphs. We define a bipartite graph  $H=(X+Y,E)$  as follows:

- An  $n$ -node set  $X=\{x_1,x_2,\dots,x_n\}$  and an  $m$ -node set  $Y=\{y_1,y_2,\dots,y_m\}$  are disjoint, and thus every edge in  $H$  connects one node in  $X$  with one node in  $Y$ .
- The edge set is represented by  $E=\{e_1,e_2,\dots,e_k\}$ .

Bob plays the bipartite graph game as follows:

- To each node  $x_i$  in  $X$ , a distinct integer weight  $v_i$  between 1 and  $n$  is assigned. That is,  $1 \leq v_i \leq n$  &  $v_i \in \mathbb{Z}$  for each  $i$  with  $1 \leq i \leq n$  and  $v_i \neq v_j$  when  $i \neq j$ .
- To each node  $y_j$  in  $Y$ , a distinct integer weight  $w_j$  between 1 and  $m$  is assigned. That is,  $1 \leq w_j \leq m$  &  $w_j \in \mathbb{Z}$  for each  $j$  with  $1 \leq j \leq m$  and  $w_i \neq w_j$  when  $i \neq j$ .
- Given this, the weight of an edge  $e=(x_i,y_j)$  is defined as  $v_i+w_j$ .
- The "score" of  $H$  is defined as the sum of the weights of all edges.

For instance, suppose  $X = \{x_1, x_2\}$ ,  $Y = \{y_1, y_2\}$ , and  $E = \{(x_1, y_1), (x_2, y_1), (x_2, y_2)\}$  as shown below.

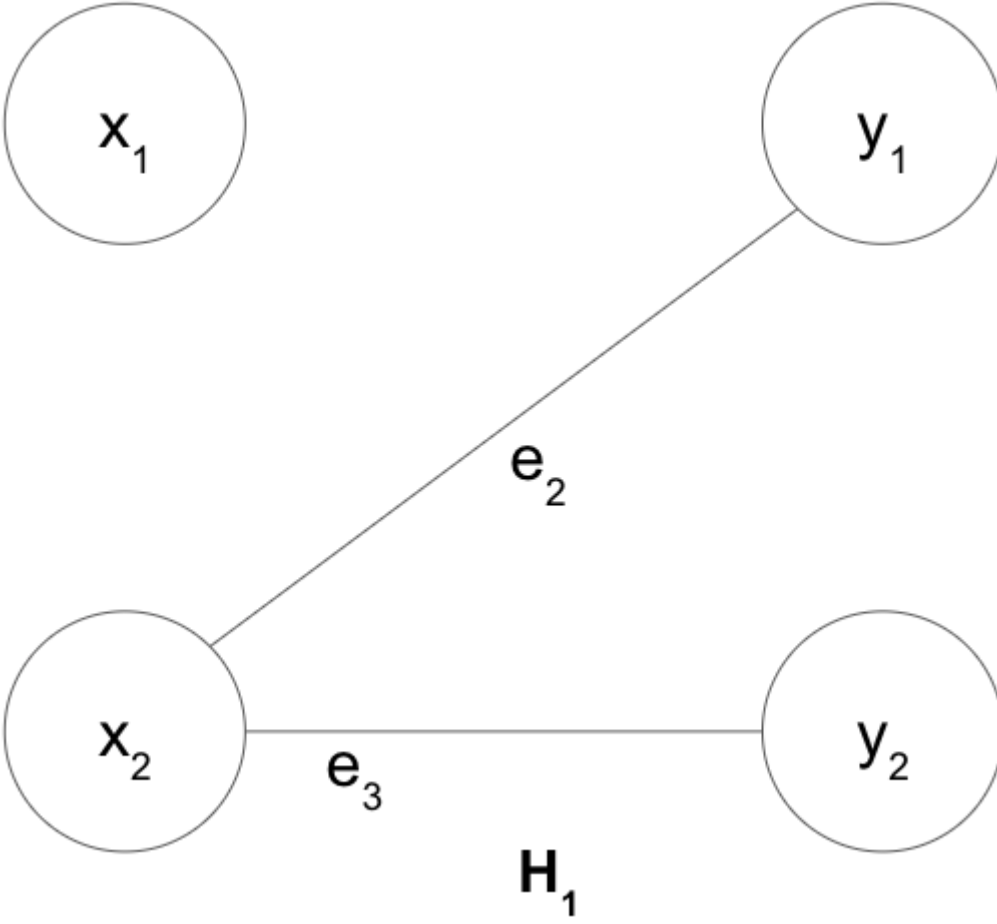


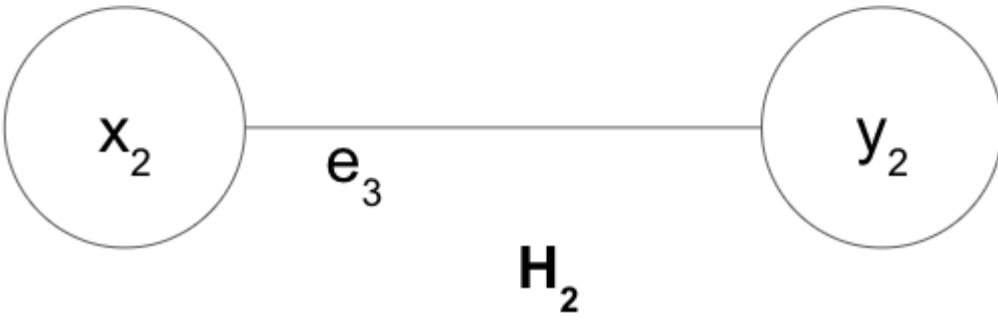
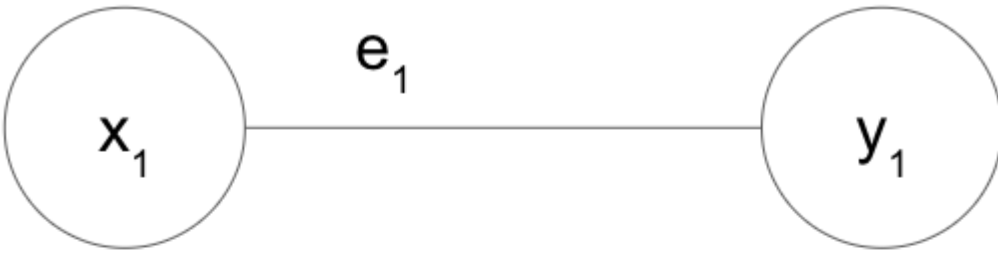
There are  $2! \times 2! = 4$  ways to assign weights to the nodes as above.

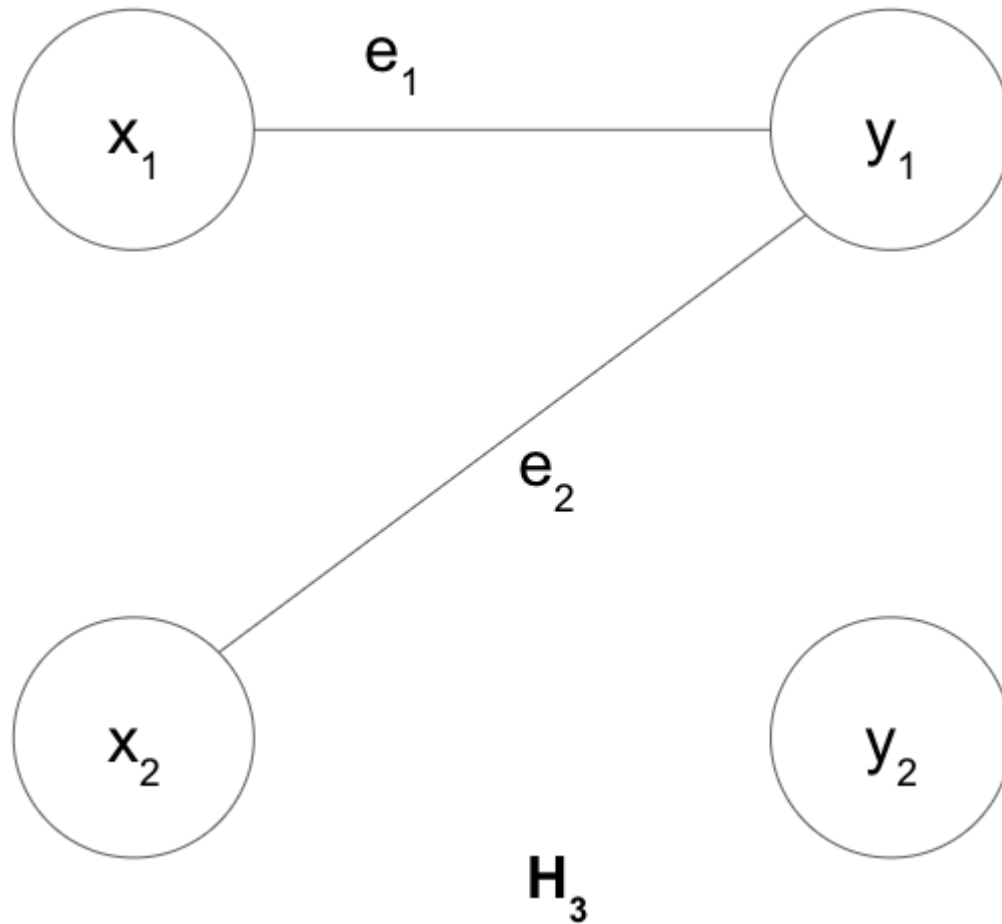
- If  $v_1 = 1, v_2 = 2$  and  $w_1 = 1, w_2 = 2$ :  $e_1 = v_1 + w_1 = 2, e_2 = v_2 + w_1 = 3, e_3 = v_2 + w_2 = 4$ , and thus the score of  $H$  is 9.
- If  $v_1 = 1, v_2 = 2$  and  $w_1 = 2, w_2 = 1$ :  $e_1 = v_1 + w_1 = 3, e_2 = v_2 + w_1 = 4, e_3 = v_2 + w_2 = 3$ , and thus the score of  $H$  is 10.
- If  $v_1 = 2, v_2 = 1$  and  $w_1 = 1, w_2 = 2$ :  $e_1 = v_1 + w_1 = 3, e_2 = v_2 + w_1 = 2, e_3 = v_2 + w_2 = 3$ , and thus the score of  $H$  is 8.
- If  $v_1 = 2, v_2 = 1$  and  $w_1 = 2, w_2 = 1$ :  $e_1 = v_1 + w_1 = 4, e_2 = v_2 + w_1 = 3, e_3 = v_2 + w_2 = 2$ , and thus the score of  $H$  is 9.

Let  $S(H)$  be the largest score of  $H$  we can obtain by assigning the weights. Bob is getting bored from computing  $S(H)$  as he is too good at it.

Alice, noticing this, proposed a new game. Let  $H_i$  be the graph you obtain by removing the  $i$ -th edge from  $H$  (see below).







$S(H_i)$  is then the highest score achievable for  $H_i$ , analogously. In the example above,  $H_1$  is obtained by removing  $(x_1, y_1)$  in  $H$ , and  $S(H_1) = 7$  (to achieve this, Bob should assign  $v_1 = 1, v_2 = 2$ ). In the same example,  $H_2$  is obtained by removing  $(x_2, y_1)$  in  $H$ , and  $S(H_2) = 6$  regardless of the weights  $(v_1, v_2, w_1, w_2)$ . Lastly,  $S(H_3) = 7$ , and thus the maximum of  $S(H_1), S(H_2), S(H_3)$  is 7.

Per Alice's suggestion, Bob wants to compute  $S(H)$  as well as the maximum of  $S(H_1), S(H_2), \dots, S(H_k)$ . Let's help Bob.

## Input

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The first line of the input will contain  $T$ , the number of test cases.

The first line of each test case will contain  $n, m, k$ , separated by whitespace. The next  $k$  lines will contain two integers (a node in  $X$  and a node in  $Y$ ) in each line, describing an edge. If an edge connects  $x_i$  and  $y_j$ , then the input will be given as " $i\ j$ ".

## Output

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Output each test case's answer (two integers) in each line. The first integer must be  $S(H)$  and the second the maximum of  $S(H_1), \dots, S(H_k)$ .

## Limit

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- $1 \leq T \leq 10$
- $1 \leq n, m \leq 10,000$
- $1 \leq k \leq 100,000$

## Sample Input 1 Copy

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```
3
1 5 2
1 5
1 4
2 2 3
1 1
2 1
2 2
3 2 4
1 1
2 1
2 2
```

3 2

## Sample Output 1 Copy

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11 6

10 7

15 13

Case 1: One way is to assign  $v_1 = 1$ ,  $w_4 = 4$ ,  $w_5 = 5$  to obtain  $S(H) = 11$ .  $S(H_1) = S(H_2) = 6$  in this example.

Case 2: Discussed in the problem statement.

Case 3: No explanation.

## Time Limit

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- Java 8: 6 seconds
- Python 3: 3 seconds
- PyPy3: 3 seconds
- Java 8 (OpenJDK): 6 seconds
- Java 11: 6 seconds
- Kotlin (JVM): 6 seconds
- Java 15: 6 seconds