$$\lim_{n \to \infty} \sum_{k=1}^{n} (-1)^{k} k! (2k-1)!! \sin\left(\frac{\pi}{2k}\right)$$