$$\sum_{k=1}^{n-1} k! \binom{2k}{k}^2 (2k+1)(-1)^k x_{2k+1} = 0$$