$$\lim_{n\to\infty} \frac{1}{n^3} \sum_{k=0}^{n-1} (-1)^k \binom{n}{k}^2 k!(n-2k)$$