$$\sum_{k=1}^{n} (-1)^k \binom{2n}{n-k}^2 \binom{2n}{n+k}$$