

Corrections on GR #2

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Problem 1: and V

¶ merged upon $C_{t_{alt}}$, so I will just correct these pieces and finish solving to the end.

$$V = \sqrt{\frac{2nW}{\rho S C_L}} = \sqrt{\frac{2(1)(724,223)}{3 \times 10^{-6}(6280)(.462)}} = 12,900 \frac{ft}{s}$$

$$q = \frac{1}{2} \rho V^2 = \frac{1}{2} (3 \times 10^{-6}) (12,900 \frac{ft}{s})^2 = 249.615$$

$$D = C_D q S$$

$$C_D = .05 + .078 (.462)^2 = .0666$$

$$D = .0666 (249.6) (6280) = \boxed{104,394.7 \text{ lbs}} \text{ drag}$$

Max powered Range:

$$E = \frac{1}{C_t} \frac{C_L}{C_D} \ln \left(\frac{W_1}{W_2} \right)$$

$$C_{t_{alt}} = C_{t_{SL}} \left(\frac{q_{ALT}}{q_{SL}} \right) = \frac{.0005}{sec} \left(\frac{1075 \frac{ft}{s}}{1116.4 \frac{ft}{s}} \right) = \frac{0.000481}{sec}$$

$$E = \frac{1}{.000481_s} \cdot \frac{.462}{.0666} \ln \left(\frac{724,223}{624,223} \right) = 2143.0 sec$$

$$d = vt \quad d = \frac{12,900 \frac{ft}{s} (2143.0 sec)}{5} \cdot \frac{1 \text{ mile}}{6076 \text{ ft}} = \boxed{4,549.8 \text{ miles}} \text{ Range}$$

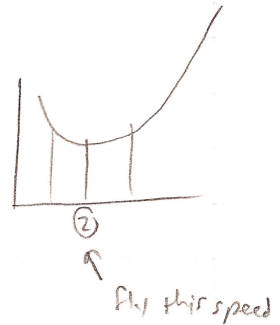
$$M = \frac{12,900 \frac{ft}{s}}{1075 \frac{ft}{s}} = \boxed{12}$$

Problem 2) A) Given: $\overset{\text{glider}}{S} = 303 \text{ ft}^2$ $\rho = .002377 \frac{\text{slug}}{\text{ft}^3}$
 $W = 225 \text{ lbs} + 145 \text{ lbs Wilbur} = 370 \text{ lbs}$
 $C_D = \underbrace{0.07}_{C_{D_0}} + \underbrace{0.08}_{k} C_L^2$

Find: V for max range

Assume: std. atmos., flying at sea level

Sketch:



Estimate: $< 100 \text{ mph}$

Solution: $C_{D_0} = k C_L^2$
 $C_L = \sqrt{\frac{C_{D_0}}{k}}$

$$C_L = \sqrt{\frac{.07}{.08}} = 0.9354$$

$$V = \sqrt{\frac{2 n W}{\rho S C_L}} = \sqrt{\frac{2 (370 \text{ lbs})}{.002377 (303) (.9354)}} = \boxed{33.14 \frac{\text{ft}}{\text{s}}} @ \text{ max. range}$$

check: $\frac{33.14 \text{ ft}}{\text{s}} \cdot \frac{\text{mile}}{5280 \text{ ft}} \cdot \frac{3600 \text{ s}}{\text{hr}} = 22.6 \text{ mph} \checkmark$

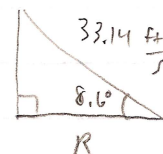
B) Given: $h = 100 \text{ ft}$
 Find: range

$$D = C_D \rho S = .14 (1.305) (303) = 55.36 \text{ lbs drag}$$

$$q = \frac{1}{2} \rho V^2 = \frac{1}{2} (.002377) (33.14)^2 = 1.305$$

$$C_D = .07 + .08 (.9354)^2 = .1400$$

$$\gamma = \sin^{-1} \left(\frac{D}{W} \right) = \sin^{-1} \left(\frac{55.36 \text{ lbs}}{370 \text{ lbs}} \right) = 8.6^\circ$$



$$\sin 8.6^\circ = \frac{h}{33.14}$$

$$h = 4.96 \text{ ft/s down}$$

$$\frac{100 \text{ ft}}{4.96 \text{ ft/s}} = 20.16 \text{ seconds}$$

$$1 \cos 8.6 = \frac{R}{32.14}$$

$$R = 32.77 \text{ ft/s} \cdot 20.16 \text{ s} = \boxed{660.6 \text{ ft}}$$

$$c) \quad 3 C_{D_0} = k C_L^2$$

$$C_L = \sqrt{\frac{3 C_{D_0}}{k}} = \sqrt{\frac{3 (.07)}{(.08)}} = 1.62$$

$$V = \sqrt{\frac{2 (370)}{(.002377) (303) (1.62)}} = \boxed{25.18 \text{ ft/s}}$$

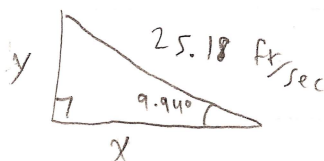
$$d) \quad q = \frac{1}{2} \rho V^2 = \frac{1}{2} (.002377) (25.18)^2 = .7535$$

$$C_D = .07 + .08 (1.62)^2 = .28$$

$$D = .28 (.7535) (303) = \boxed{63.9 \text{ lbf drag}}$$

$$\gamma = \sin^{-1} \left(\frac{D}{W} \right) = \sin^{-1} \left(\frac{63.9}{370} \right) = \boxed{9.94^\circ}$$

Bonus) arrival:



$$\sin (9.94) (25.18) = 4.346 \text{ ft/s down}$$

$$\frac{100 \text{ ft}}{4.346 \text{ ft/s}} = 23.01 \text{ sec} - 20.16 \text{ sec} = \boxed{2.85 \text{ sec longer}}$$