

Rubric Assignment 2

Q.1

$$GaAs: V_{bi} = 1.20V, \quad n_i = 1.8 \times 10^6 \text{ cm}^{-3}$$

$$x_p = 0.2W = 0.2(x_n + x_p)$$

$$\text{or} \quad \frac{x_p}{x_n} = 0.25$$

Also

$$N_d x_n = N_a x_p$$

$$\Rightarrow \frac{x_p}{x_n} = \frac{N_d}{N_a} = 0.25$$

Now

$$V_{bi} = V_t \ln \left(\frac{N_a N_d}{n_i^2} \right)$$

$$1.20 = 0.0259 \ln \left(\frac{0.25 N_a^2}{n_i^2} \right)$$

Then

$$\frac{0.25 N_a^2}{n_i^2} = \exp \left(\frac{1.20}{0.0259} \right)$$

$$\text{or} \quad N_a = 2n_i \exp \left[\frac{1.20}{2(0.0259)} \right]$$

(2)

d

$$N_a = 4.14 \times 10^{16} \text{ cm}^{-3} \quad 2 \text{ Marks}$$

e

$$N_d = 0.25 N_a = 1.04 \times 10^{16} \text{ cm}^{-3} \quad 2 \text{ Marks}$$

f

$$\chi_n = \left[\frac{2eV_{bi}}{e} \left(\frac{N_a}{N_d} \right) \left(\frac{1}{N_a + N_d} \right) \right]^{1/2}$$

$$= \left[\frac{2 \times (13.1) (8.85 \times 10^{-14}) (1.20)}{1.6 \times 10^{-19}} \times \left(\frac{4}{1} \right) \frac{1}{4.14 \times 10^{16} + 1.04 \times 10^{16}} \right]^{1/2}$$

$$\chi_n = 0.366 \text{ } \mu\text{m} \quad 2 \text{ Marks}$$

g

$$\chi_p = 0.25 \chi_n = 0.0916 \text{ } \mu\text{m} \quad 2 \text{ Marks}$$

h

$$E_{\max} = \frac{e N_d \chi_n}{e} = \frac{e N_a \chi_p}{e}$$

$$= \frac{(1.6 \times 10^{-19}) (1.04 \times 10^{16}) (0.366 \times 10^{-4})}{(13.1) (8.85 \times 10^{-14})}$$

$$E_{\max} = 5.25 \times 10^4 \text{ V/cm} \quad 2 \text{ Marks}$$

(3)

Q.2

a. By Poisson's eqn we know that

$$\frac{dE}{dx} = \frac{\rho}{\epsilon_s} \rightarrow 1 \text{ Marks}$$

Here

$$\frac{dE}{dx} = \frac{-4.2 \times 10^4 \text{ V/cm} - 0}{0 - 2 \times 10^{-4} \text{ cm}} = +ve \text{ quantity}$$

$$\Rightarrow \frac{\rho}{\epsilon_s} = +ve \rightarrow 1 \text{ Marks}$$

Hence the Semiconductor is n-type Since the depleted charged ions are +ve. 2 Marks

b. Schottky barrier diode (n-type)

$$N_d = 2.5 \times 10^{15} \text{ cm}^{-3}$$

$$\phi_B = 0.55 \text{ V}$$

$$V_{bi} = \phi_B - \phi_n \rightarrow 1 \text{ Marks}$$

$$\phi_n = V_t \ln \left(\frac{N_c}{N_d} \right) = 0.0259 \ln \left(\frac{2.8 \times 10^{19}}{2.5 \times 10^{15}} \right)$$

$$\phi_n = 0.24 \text{ V} \rightarrow 1 \text{ Marks}$$

a. i. $V_{bi} = \phi_B - \phi_n$

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$$V_{bi} = 0.55 - 0.24$$

$$\boxed{V_{bi} = 0.31V} \rightarrow 1 \text{ Marks}$$

(ii) $N_d = 3 \times 10^{16} \text{ cm}^{-3}$

$$\phi_n = 0.0259 \ln \left(\frac{2.8 \times 10^{19}}{3 \times 10^{16}} \right)$$

$$\phi_n = 0.17V \rightarrow 1 \text{ Marks}$$

$$V_{bi} = 0.55 - 0.17$$

$$\boxed{V_{bi} = 0.38V} \rightarrow 1 \text{ Marks}$$

Change in $V_{bi} = 0.07V \rightarrow 1 \text{ Marks}$
So by increasing N_d , V_{bi} increases.

(5)

Q3
a, The depletion width W & maximum electric field E_m can be computed as follows

$$V_{bi} = V_T \ln \left(\frac{N_a N_d}{n_i^2} \right) = 0.0259 \ln \frac{(10^{17})(2 \times 10^{16})}{(1.5 \times 10^{10})^2}$$

$$\boxed{V_{bi} = 0.777 \text{ V}} \rightarrow 1 \text{ Marks}$$

$$W = \sqrt{\frac{2\epsilon}{q} \frac{N_a + N_d}{N_a N_d} (V_{bi} - V_a)}$$

$$= \sqrt{\frac{2 \times 11.8 \times 0.85 \times 10^{-14}}{1.6 \times 10^{-19}} \frac{1.2 \times 10^{17}}{2 \times 10^{33}} \times 0.12 \text{ cm}}$$

$$= 0.0974 \text{ cm}$$

$$E_m = \frac{2(V_{bi} - V_a)}{W} = \frac{2 \times 0.12 \text{ V}}{0.097 \times 10^{-4} \text{ cm}} = \boxed{25 \text{ kV/cm}} \quad 1 \text{ Marks}$$

b, The equilibrium minority carrier densities are given by

$$p_{n0} = \frac{n_i^2}{N_d} = \frac{(1.5 \times 10^{10})^2}{2 \times 10^{16}} = 1.125 \times 10^4 \text{ cm}^{-3}$$

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$$\eta_{p0} = \frac{\eta_i^2}{N_A} = \frac{(1.5 \times 10^{10})^2}{1 \times 10^{17}} = 2.25 \times 10^3 \text{ cm}^{-3}$$

The minority carrier densities at x_p & x_n are given by

$$\eta(x_p) = \eta_{p0} (e^{V_a/V_T} - 1) = 1.8 \times 10^{14} \text{ cm}^{-3} \quad 1 \text{ Mark}$$

$$p(x_n) = p_{n0} (e^{V_a/V_T} - 1) = 8.9 \times 10^{14} \text{ cm}^{-3} \quad 1 \text{ Mark}$$

∴ The diffusion coefficients are given by

$$D_p = \mu_p kT/q = 0.0259 \times 500 = 12.9 \text{ cm}^2/\text{s}$$

$$D_n = \mu_n kT/q = 0.0259 \times 1500 = 38.7 \text{ cm}^2/\text{s}$$

The minority carrier diffusion lengths in the neutral regions are

$$L_p = \sqrt{D_p \tau_p} = 80.3 \text{ } \mu\text{m}$$

$$L_n = \sqrt{D_n \tau_n} = 88 \text{ } \mu\text{m}$$

The minority carrier densities at x_n & x_p are given by

$$J_p(x_n) = \frac{q D_p p_{n0}}{L_p} (e^{V_a/V_T} - 1) = 0.235 \text{ A/cm}^2 \quad 1 \text{ Mark}$$

$$J_n(x_p) = \frac{q D_n n_{p0}}{L_n} (e^{V_a/V_T} - 1) = 0.13 \text{ A/cm}^2 \quad 1 \text{ Mark}$$

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d, The diode current I is given by

$$I = A [J_p(x_n) + J_n(x_p)]$$

$$= 10^3 \text{ cm}^2 (0.235 + 0.13) \text{ A/cm}^2$$

$$I = 0.365 \text{ mA} \quad 1 \text{ Marks}$$

e, In the neutral p or n region, more than 5Lm or 5Lp away from the depletion region, the entire current density is due to drift of the majority carriers $\hat{J} \approx J_n = q \mu_n E_{\text{neutral}}^n n_{n0}$ in the neutral n region, 5Lp away from the depletion region giving

$$E_{\text{neutral}}^n = \frac{J}{q \mu_n n_{n0}} = \frac{0.365 \left[\frac{\text{A}}{\text{cm}^2} \right]}{1.6 \times 10^{-19} [\text{C}] \times 1500 \left[\frac{\text{cm}^2}{\text{V-s}} \right] \times 2 \times 10^{16} \left[\frac{1}{\text{cm}^3} \right]}$$

$$= 0.076 \text{ V/cm} \quad 1 \text{ Marks}$$

Similarly

$$E_{\text{neutral}}^p = \frac{J}{q \mu_p p_{p0}} = 0.045 \text{ V/cm} \quad 1 \text{ Marks}$$

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f, The reverse Saturation Current I_s is given by

$$I_s = A \left(\frac{q D_p p_{n0}}{L_p} + \frac{q D_n n_{p0}}{L_n} \right)$$

$$I_s = 4.5 \times 10^{-15} \text{ A} \quad 1 \text{ Marks}$$