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Q.1. Consider a particle moving in a one-dimensional finite square well defined by

$$V_x = \begin{cases} -V_0 & |x| < a \\ 0 & |x| > a \end{cases}$$

Solve the time-independent Schrodinger equation for the system and obtain the bound state energy eigenfunctions. Discuss how the energy levels can be obtained graphically.

[5 marks]

Q.2. The normalized wave function is given as

$$\psi(x) = \frac{\sqrt{31}}{2a^{\frac{3}{2}}}(a^3x^{\frac{3}{2}} - x^{\frac{5}{2}})$$

and is present in 1D potential well given as

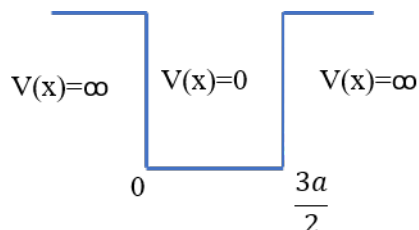


Figure 1:

Find the ground state energy using the expectation value $\langle E \rangle$.

[5 marks]

Q.3. Using the uncertainty principle, estimate the ground state energy of the helium atom.

[5 marks]

Q.4. Derive the reciprocal lattice of fcc and bcc crystal.

[5 marks]

Q.5. An α -particle having energy 10MeV approaches a square potential barrier of height 30MeV. Determine the width of the barrier if the transmission coefficient is 2×10^{-3} . Given: mass of an α particle = 6.68×10^{-27} kg, $\hbar = 1.054 \times 10^{-34}$ Js [5 marks]

Q.6. Two potential barriers are shown in Figure 2, namely A and B, and they have the height $\frac{V_0}{2}$ and $3V_0$. Find the ratio of $\frac{T_A}{T_B}$ (tunneling probability) given $E = \frac{V_0}{100}$. [5 marks]

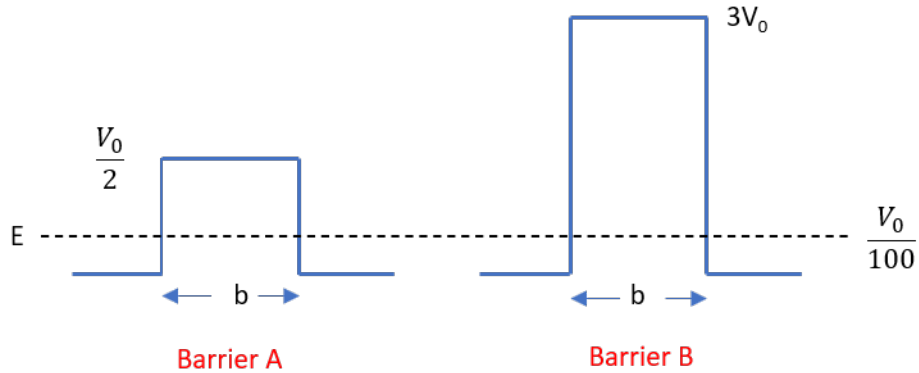


Figure 2:

Best wishes