

Marketing Analytics

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2024-04-30

```
# Encode 'churn' variable: If 'churn' equals 'Yes', encode as 1, else encode as 0
data$churn<-ifelse(data$churn=='Yes',1,0)
# Categorical Variable Conversion
data$marital <- as.factor(data$marital)
data$ed <- as.factor(data$ed)
data$retire <- as.factor(data$retire)
data$gender <- as.factor(data$gender)
data$voice <- as.factor(data$voice)
data$internet <- as.factor(data$internet)
data$forward <- as.factor(data$forward)
data$custcat <- as.factor(data$custcat)
```

```
# Creating survival object
surv_obj <- Surv(time = data$tenure, event = data$churn)

# Defining a function to fit accelerated failure time (AFT) model
fit_aft_model <- function(dist) {
  # Fitting AFT model using survreg function
  model <- survreg(
    surv_obj ~ age + marital + address + income + ed + retire + gender + voice + internet + forward + c
    data = data,
    dist = dist
  )
  return(model)
}
```

```
#Get Available Distributions:
distributions <- names(survreg.distributions)
```

```
#Fit AFT Models with All Available Distributions
models <- lapply(distributions, fit_aft_model)
```

```
new_data <- data.frame(
  age = mean(data$age),
  marital = as.factor(names(which.max(table(data$marital)))),
  address = mean(data$address),
  income = mean(data$income),
  ed = as.factor(names(which.max(table(data$ed)))),
  retire = as.factor(names(which.max(table(data$retire)))),
  gender = as.factor(names(which.max(table(data$gender)))),
  voice = as.factor(names(which.max(table(data$voice)))),
```

```

internet = as.factor(names(which.max(table(data$internet)))),
forward = as.factor(names(which.max(table(data$forward)))),
custcat = as.factor(names(which.max(table(data$custcat)))),
tenure = median(data$tenure)
)

# Define a function to generate survival curves
survival_curves <- function(models, dist) {
  probs <- seq(0.1, 0.9, length = 9)
  all_data <- data.frame()

  # Iterate through models and add survival data to the dataframe
  for (i in seq_along(models)) {
    # Predict survival probabilities using the fitted model
    pred_surv <- predict(models[[i]], type = "quantile", p = 1 - probs, newdata = new_data)
    data <- data.frame(Time = pred_surv, Probabilities = probs, Distribution = dist[i])
    all_data <- rbind(all_data, data)
  }
  return(all_data)
}

survival_curve<-survival_curves(models, distributions)
survival_curve

```

##	Time	Probabilities	Distribution
## 1	98.51839	0.1	extreme
## 2	91.41844	0.2	extreme
## 3	85.66433	0.3	extreme
## 4	80.25139	0.4	extreme
## 5	74.71866	0.5	extreme
## 6	68.66806	0.6	extreme
## 7	61.54718	0.7	extreme
## 8	52.24948	0.8	extreme
## 9	37.37294	0.9	extreme
## 10	107.61308	0.1	logistic
## 11	94.97419	0.2	logistic
## 12	86.57356	0.3	logistic
## 13	79.68730	0.4	logistic
## 14	73.36785	0.5	logistic
## 15	67.04841	0.6	logistic
## 16	60.16215	0.7	logistic
## 17	51.76152	0.8	logistic
## 18	39.12263	0.9	logistic
## 19	109.32823	0.1	gaussian
## 20	97.29046	0.2	gaussian
## 21	88.61039	0.3	gaussian
## 22	81.19358	0.4	gaussian
## 23	74.26127	0.5	gaussian
## 24	67.32897	0.6	gaussian
## 25	59.91216	0.7	gaussian
## 26	51.23208	0.8	gaussian
## 27	39.19432	0.9	gaussian
## 28	371.86412	0.1	weibull

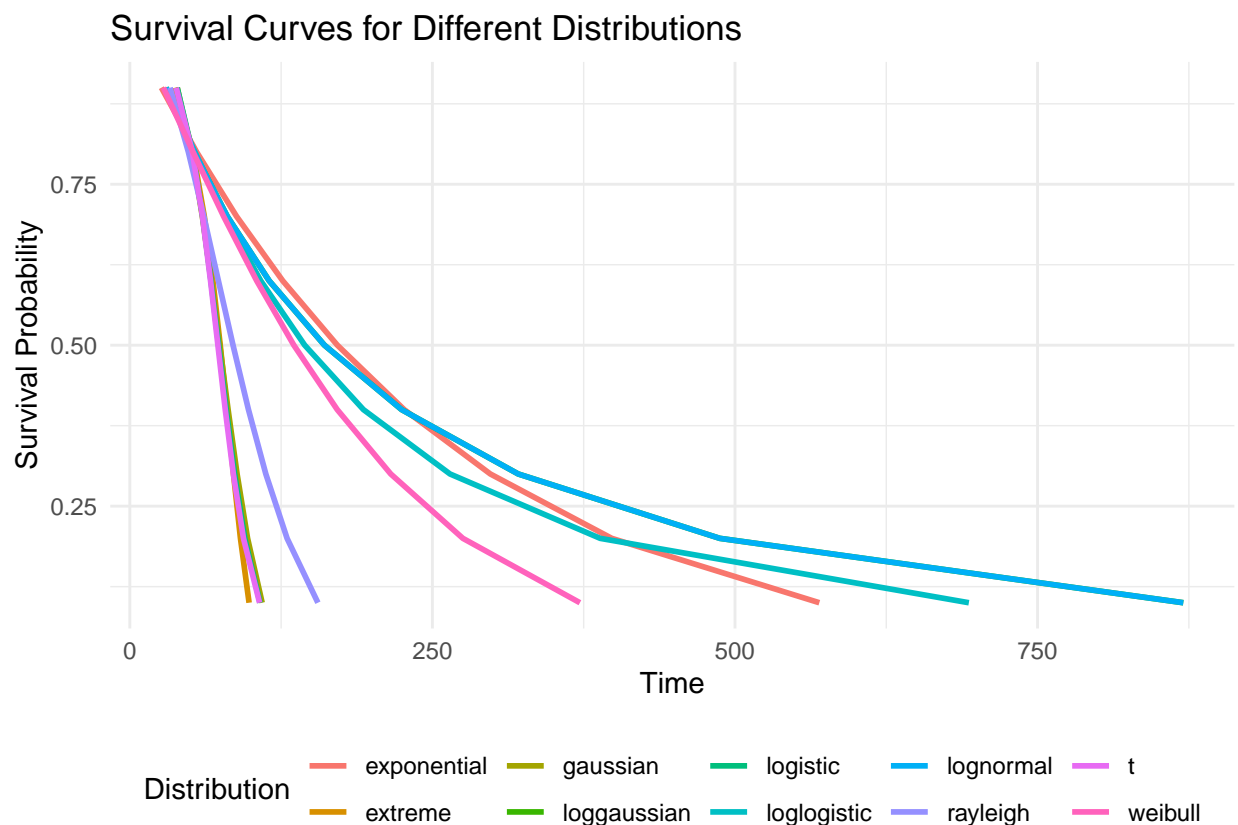
## 29	275.17842	0.2	weibull
## 30	215.59207	0.3	weibull
## 31	171.37008	0.4	weibull
## 32	135.52854	0.5	weibull
## 33	104.85481	0.6	weibull
## 34	77.52341	0.7	weibull
## 35	52.26176	0.8	weibull
## 36	27.80875	0.9	weibull
## 37	569.68079	0.1	exponential
## 38	398.18978	0.2	exponential
## 39	297.87398	0.3	exponential
## 40	226.69878	0.4	exponential
## 41	171.49101	0.5	exponential
## 42	126.38297	0.6	exponential
## 43	88.24467	0.7	exponential
## 44	55.20777	0.8	exponential
## 45	26.06716	0.9	exponential
## 46	155.39566	0.1	rayleigh
## 47	129.91765	0.2	rayleigh
## 48	112.36715	0.3	rayleigh
## 49	98.02744	0.4	rayleigh
## 50	85.25969	0.5	rayleigh
## 51	73.19263	0.6	rayleigh
## 52	61.15998	0.7	rayleigh
## 53	48.37525	0.8	rayleigh
## 54	33.24069	0.9	rayleigh
## 55	870.39770	0.1	loggaussian
## 56	487.47787	0.2	loggaussian
## 57	320.93435	0.3	loggaussian
## 58	224.54225	0.4	loggaussian
## 59	160.80994	0.5	loggaussian
## 60	115.16690	0.6	loggaussian
## 61	80.57671	0.7	loggaussian
## 62	53.04822	0.8	loggaussian
## 63	29.71037	0.9	loggaussian
## 64	870.39770	0.1	lognormal
## 65	487.47787	0.2	lognormal
## 66	320.93435	0.3	lognormal
## 67	224.54225	0.4	lognormal
## 68	160.80994	0.5	lognormal
## 69	115.16690	0.6	lognormal
## 70	80.57671	0.7	lognormal
## 71	53.04822	0.8	lognormal
## 72	29.71037	0.9	lognormal
## 73	693.22288	0.1	loglogistic
## 74	388.63569	0.2	loglogistic
## 75	264.54065	0.3	loglogistic
## 76	192.99940	0.4	loglogistic
## 77	144.50765	0.5	loglogistic
## 78	108.19962	0.6	loglogistic
## 79	78.93857	0.7	loglogistic
## 80	53.73274	0.8	loglogistic
## 81	30.12373	0.9	loglogistic
## 82	107.18571	0.1	t

```
## 83 93.89165      0.2      t
## 84 85.53428      0.3      t
## 85 78.84671      0.4      t
## 86 72.76980      0.5      t
## 87 66.69289      0.6      t
## 88 60.00533      0.7      t
## 89 51.64795      0.8      t
## 90 38.35389      0.9      t
```

```
plt <- ggplot(data = survival_curve, aes(x = Time, y = Probabilities, color = Distribution)) +
  geom_line(size = 1) +
  theme_minimal() +
  labs(x = "Time", y = "Survival Probability", title = "Survival Curves for Different Distributions") +
  theme(legend.position = "bottom") +
  geom_abline(intercept = 0, slope = 0)
```

```
## Warning: Using 'size' aesthetic for lines was deprecated in ggplot2 3.4.0.
## i Please use 'linewidth' instead.
## This warning is displayed once every 8 hours.
## Call 'lifecycle::last_lifecycle_warnings()' to see where this warning was
## generated.
```

```
print(plt)
```



From the results it is obvious that the best survival curve is the lognormal one.

To improve model selection, we can consider additional statistical measures like the Akaike Information Criterion (AIC) and the Bayesian Information Criterion (BIC). Lower AIC and BIC values indicate better model performance.

```
# Create an empty dataframe to store decision data
decision_data <- data.frame()
for (i in seq_along(models)) {
  # Extract log likelihood, AIC, and BIC values for each model
  loglikelihood <- models[[i]]$loglik
  aic <- AIC(models[[i]])
  bic <- BIC(models[[i]])
  data_aic_bic <- data.frame(Loglikelihood = loglikelihood, AIC = aic, BIC = bic, Distribution = distri)
  # Append data to decision_data dataframe
  decision_data <- rbind(decision_data, data_aic_bic)
}

min_bic <- min(decision_data$BIC)
min_aic <- min(decision_data$AIC)

decision_data
```

##	Loglikelihood	AIC	BIC	Distribution
## 1	-1747.194	3181.130	3269.470	extreme
## 2	-1572.565	3181.130	3269.470	extreme
## 3	-1734.223	3149.168	3237.507	logistic
## 4	-1556.584	3149.168	3237.507	logistic
## 5	-1714.485	3133.226	3221.565	gaussian
## 6	-1548.613	3133.226	3221.565	gaussian
## 7	-1606.431	2962.382	3050.721	weibull
## 8	-1463.191	2962.382	3050.721	weibull
## 9	-1606.980	2971.078	3054.510	exponential
## 10	-1468.539	2971.078	3054.510	exponential
## 11	-1739.723	3091.719	3175.151	rayleigh
## 12	-1528.859	3091.719	3175.151	rayleigh
## 13	-1602.518	2951.151	3039.491	loggaussian
## 14	-1457.576	2951.151	3039.491	loggaussian
## 15	-1602.518	2951.151	3039.491	lognormal
## 16	-1457.576	2951.151	3039.491	lognormal
## 17	-1605.208	2953.691	3042.030	loglogistic
## 18	-1458.845	2953.691	3042.030	loglogistic
## 19	-1748.062	3165.973	3254.312	t
## 20	-1564.986	3165.973	3254.312	t

In our analysis, we observe that the model with a lognormal distribution yields the minimum AIC (2951.151) and BIC (3039.491). Therefore, based on these criteria, we again select the model with a lognormal distribution as our final choice.

#Feature Significance Then which features are influential for the model. Initially, we'll incorporate all available features into the model and evaluate their significance. (Alpha = 0.1)

```
# Fitting a model with all features and examining their significance
feature_testing_model <- survreg(surv_obj ~ age + marital + address + income + ed + retire + gender + v
summary_results <- summary(feature_testing_model)
summary_results
```

```
##
## Call:
## survreg(formula = surv_obj ~ age + marital + address + income +
##         ed + retire + gender + voice + internet + forward + custcat,
##         data = data, dist = "lognormal")
##
##               Value Std. Error      z      p
## (Intercept)      2.338870   0.281279  8.32 < 2e-16
## age              0.032795   0.007247  4.53 6.0e-06
## maritalUnmarried -0.459424   0.114720 -4.00 6.2e-05
## address          0.042153   0.008882  4.75 2.1e-06
## income           0.001387   0.000918  1.51  0.131
## edDid not complete high school 0.379168   0.200877  1.89  0.059
## edHigh school degree 0.315976   0.162495  1.94  0.052
## edPost-undergraduate degree -0.019815   0.222366 -0.09  0.929
## edSome college    0.285140   0.164846  1.73  0.084
## retireYes         0.031781   0.444440  0.07  0.943
## genderMale        0.051108   0.114237  0.45  0.655
## voiceYes          -0.424370   0.168551 -2.52  0.012
## internetYes       -0.758597   0.142814 -5.31 1.1e-07
## forwardYes        -0.196353   0.179535 -1.09  0.274
## custcatE-service   1.059925   0.170244  6.23 4.8e-10
## custcatPlus service 0.923373   0.214843  4.30 1.7e-05
## custcatTotal service 1.182016   0.249736  4.73 2.2e-06
## Log(scale)        0.275904   0.045997  6.00 2.0e-09
##
## Scale= 1.32
##
## Log Normal distribution
## Loglik(model)= -1457.6   Loglik(intercept only)= -1602.5
## Chisq= 289.88 on 16 degrees of freedom, p= 3.2e-52
## Number of Newton-Raphson Iterations: 5
## n= 1000
```

```
# Checking features with p-values less than 0.1
significant_features <- summary_results$table[, 4] < 0.10
significant_features
```

```
##               (Intercept)               age
##               TRUE               TRUE
##      maritalUnmarried               address
##               TRUE               TRUE
##      income edDid not complete high school
##               FALSE               TRUE
##      edHigh school degree edPost-undergraduate degree
##               TRUE               FALSE
##      edSome college               retireYes
##               TRUE               FALSE
##      genderMale               voiceYes
##               FALSE               TRUE
##      internetYes               forwardYes
##               TRUE               FALSE
##      custcatE-service               custcatPlus service
##               TRUE               TRUE
##      custcatTotal service               Log(scale)
```

```
## TRUE TRUE
```

As some features had p values > 1, hence we need to exclude them from the model.

```
# Building the final model with selected features
```

```
final_model <- survreg(surv_obj ~ age + marital + address + ed + voice + internet + custcat, data = data,
```

```
summary_final <- summary(final_model)
```

```
summary_final
```

```
##
```

```
## Call:
```

```
## survreg(formula = surv_obj ~ age + marital + address + ed + voice +
```

```
## internet + custcat, data = data, dist = "lognormal")
```

```
## Value Std. Error z p
```

```
## (Intercept) 2.30040 0.26658 8.63 < 2e-16
```

```
## age 0.03672 0.00642 5.72 1.1e-08
```

```
## maritalUnmarried -0.45111 0.11455 -3.94 8.2e-05
```

```
## address 0.04228 0.00884 4.78 1.7e-06
```

```
## edDid not complete high school 0.32318 0.19886 1.63 0.10
```

```
## edHigh school degree 0.28346 0.16202 1.75 0.08
```

```
## edPost-undergraduate degree -0.00704 0.22287 -0.03 0.97
```

```
## edSome college 0.26066 0.16435 1.59 0.11
```

```
## voiceYes -0.43112 0.16788 -2.57 0.01
```

```
## internetYes -0.76976 0.14268 -5.40 6.8e-08
```

```
## custcatE-service 1.06378 0.17072 6.23 4.6e-10
```

```
## custcatPlus service 0.80252 0.16934 4.74 2.1e-06
```

```
## custcatTotal service 1.05892 0.21074 5.02 5.0e-07
```

```
## Log(scale) 0.28004 0.04601 6.09 1.1e-09
```

```
##
```

```
## Scale= 1.32
```

```
##
```

```
## Log Normal distribution
```

```
## Loglik(model)= -1459.7 Loglik(intercept only)= -1602.5
```

```
## Chisq= 285.71 on 12 degrees of freedom, p= 4.7e-54
```

```
## Number of Newton-Raphson Iterations: 5
```

```
## n= 1000
```

```
exp_coefs <- exp(coef(final_model))
```

```
exp_coefs
```

```
## (Intercept) age
```

```
## 9.9781819 1.0374031
```

```
## maritalUnmarried address
```

```
## 0.6369217 1.0431842
```

```
## edDid not complete high school edHigh school degree
```

```
## 1.3815083 1.3277135
```

```
## edPost-undergraduate degree edSome college
```

```
## 0.9929849 1.2977840
```

```
## voiceYes internetYes
```

```
## 0.6497821 0.4631241
```

```
## custcatE-service custcatPlus service
```

```
## 2.8972934 2.2311654
```

```
## custcatTotal service
```

```
## 2.8832641
```

.For each additional year of a customer's age, there's a 3% increase in hazard. .Unmarried individuals have roughly a 36% lower hazard compared to married ones. .Education levels are compared to the "College Degree" target group: .Individuals who did not complete high school have a 38% higher hazard. .Individuals with a high school education have a 32% higher hazard. .Individuals with a post-Undergrad degree have approximately a 1% lower hazard. .Individuals who did some college have a 29% higher hazard. .Having "Voice yes" results in approximately a 35% lower hazard compared to the "Voice No" group. .Having "Internet yes" leads to roughly a 55% lower hazard compared to the "Internet No" group. .Customer categories are compared to the "Basic service" target group: ."E-service" customers have a 189% higher hazard. ."Plus Service" customers have a 123% higher hazard. ."Total Service" customers have a 188% higher hazard.

```
new_data <- data.frame(
  age = mean(data$age),
  marital = as.factor(names(which.max(table(data$marital)))),
  address = mean(data$address),
  income = mean(data$income),
  ed = as.factor(names(which.max(table(data$ed)))),
  retire = as.factor(names(which.max(table(data$retire)))),
  gender = as.factor(names(which.max(table(data$gender)))),
  voice = as.factor(names(which.max(table(data$voice)))),
  internet = as.factor(names(which.max(table(data$internet)))),
  forward = as.factor(names(which.max(table(data$forward)))),
  custcat = as.factor(names(which.max(table(data$custcat)))),
  tenure = median(data$tenure) # Median tenure value for prediction
)

# Making predictions using the final model
predictions <- predict(final_model, type = "response", newdata = data)

# Creating a dataframe with predictions
predictions_data <- data.frame(predictions)

# Adjusting predictions for CLV calculation
sequence <- seq(1, length(colnames(predictions_data)), 1)
MM <- 1300 # Monthly margin assumption
r <- 0.1 # Discount rate assumption
for (num in sequence) {
  predictions_data[, num] <- predictions_data[, num] / (1 + r / 12) ^ (sequence[num] - 1)
}

# Calculating CLV
predictions_data$CLV <- MM * rowSums(predictions_data)

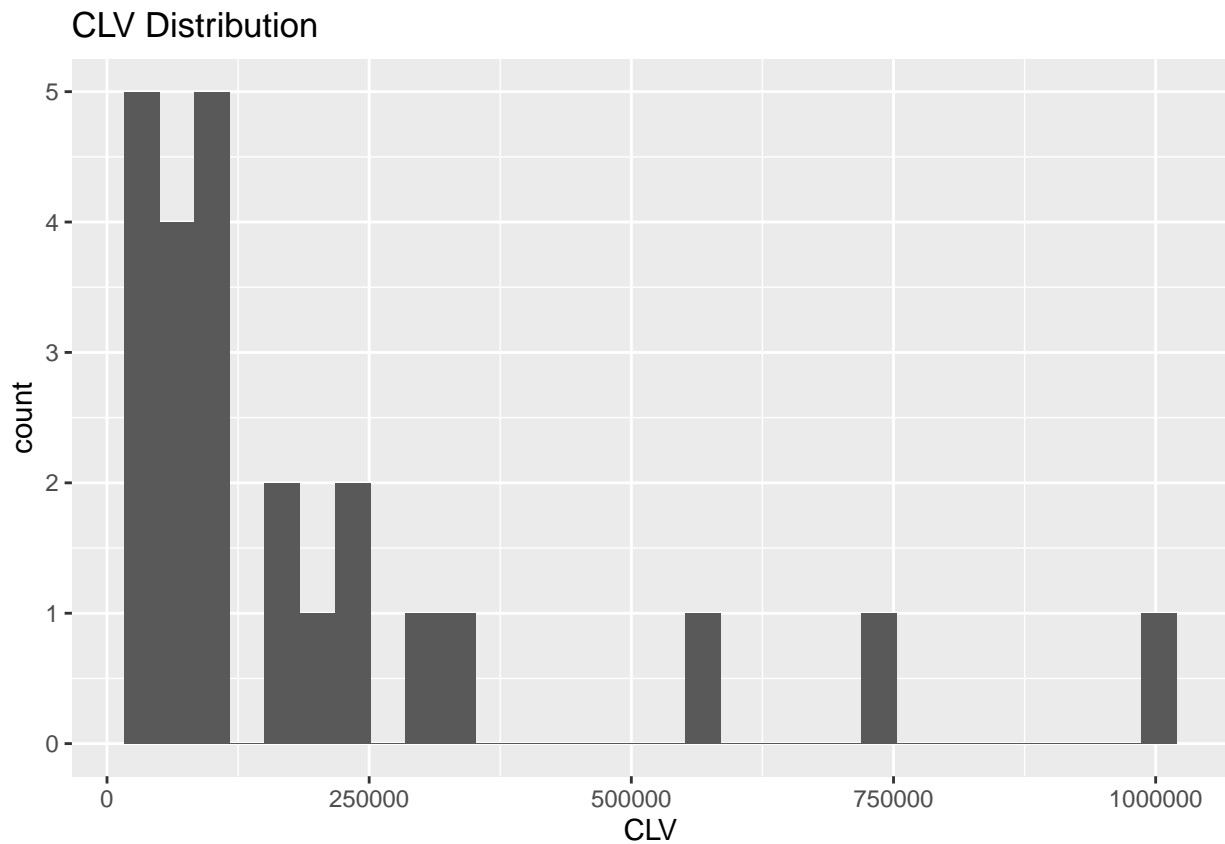
# Summary statistics of CLV
summary(predictions_data$CLV)

##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##    6531   55138  117200  246071  266528 3843252

# Plotting CLV distribution
examine_data <- head(predictions_data, 24)
ggplot(examine_data, aes(x = CLV)) +
  labs(title = "CLV Distribution") +
  geom_histogram()
```



```
## 'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.
```



```
##CLV Comparison: Female and Male customers
```

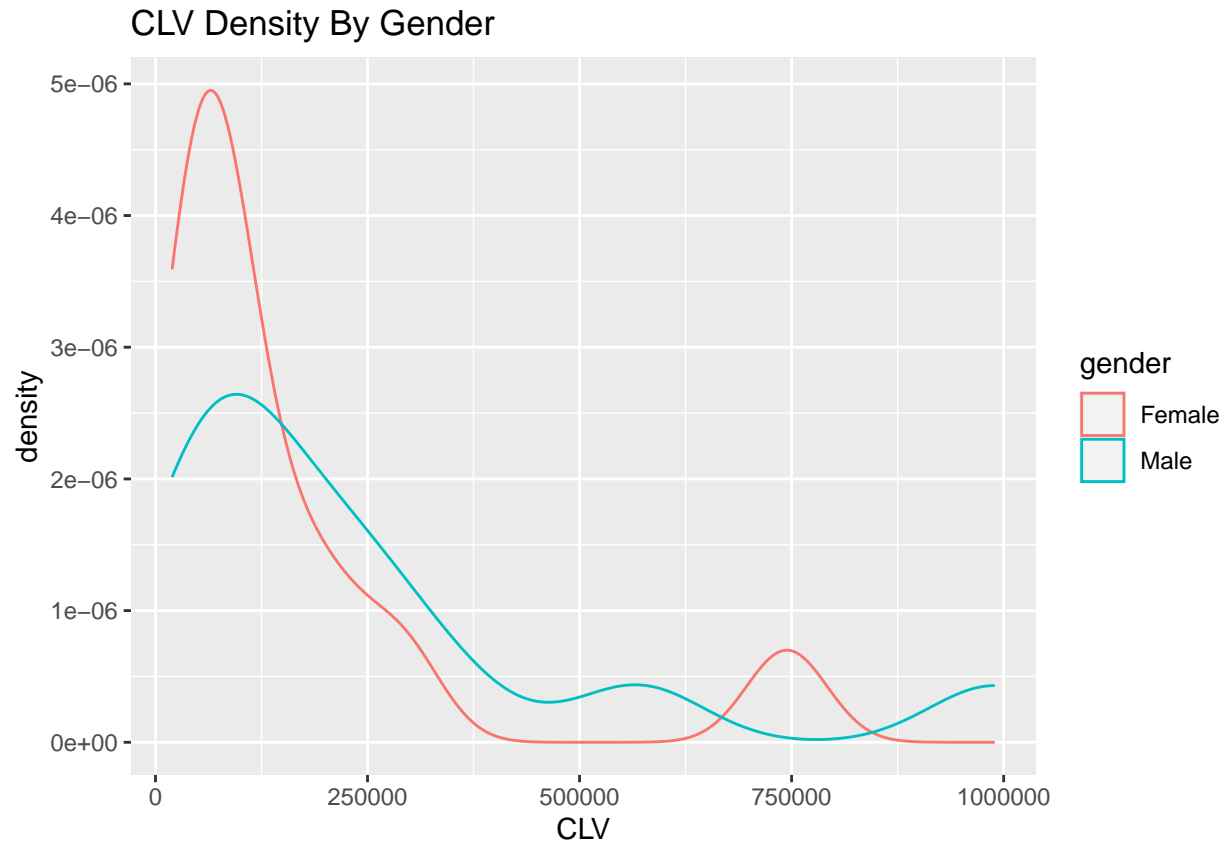
```
# Adding CLV to telco dataframe
data$CLV <- predictions_data$CLV

# Subset of data for examination
examine_data <- head(data, 24)
examine_data
```

##	ID	region	tenure	age	marital	address	income	ed
## 1	1	Zone 2	13	44	Married	9	64	College degree
## 2	2	Zone 3	11	33	Married	7	136	Post-undergraduate degree
## 3	3	Zone 3	68	52	Married	24	116	Did not complete high school
## 4	4	Zone 2	33	33	Unmarried	12	33	High school degree
## 5	5	Zone 2	23	30	Married	9	30	Did not complete high school
## 6	6	Zone 2	41	39	Unmarried	17	78	High school degree
## 7	7	Zone 3	45	22	Married	2	19	High school degree
## 8	8	Zone 2	38	35	Unmarried	5	76	High school degree
## 9	9	Zone 3	45	59	Married	7	166	College degree
## 10	10	Zone 1	68	41	Married	21	72	Did not complete high school
## 11	11	Zone 2	5	33	Unmarried	10	125	College degree
## 12	12	Zone 3	7	35	Unmarried	14	80	High school degree
## 13	13	Zone 1	41	38	Married	8	37	High school degree
## 14	14	Zone 2	57	54	Married	30	115	College degree

```
## 15 15 Zone 2      9 46 Unmarried      3      25 Did not complete high school
## 16 16 Zone 1     29 38  Married      12      75 Post-undergraduate degree
## 17 17 Zone 3     60 57 Unmarried     38     162 High school degree
## 18 18 Zone 3     34 48 Unmarried      3      49 High school degree
## 19 19 Zone 2      1 24 Unmarried      3      20 Did not complete high school
## 20 20 Zone 1     26 29  Married      3      77 College degree
## 21 21 Zone 3      6 30 Unmarried      7      16 Some college
## 22 22 Zone 1     68 52  Married     17     120 Did not complete high school
## 23 23 Zone 3     53 33 Unmarried     10     101 Post-undergraduate degree
## 24 24 Zone 3     55 48  Married     19      67 Did not complete high school
##      retire gender voice internet forward      custcat churn      CLV
## 1      No  Male      No      No      Yes Basic service      1 95484.99
## 2      No  Male     Yes      No      Yes Total service      1 108989.61
## 3      No Female      No      No      No Plus service      0 744415.47
## 4      No Female      No      No      No Basic service      1 61204.82
## 5      No  Male      No      No      Yes Plus service      0 176017.12
## 6      No Female      No      No      No Plus service      0 210284.60
## 7      No Female      No      Yes     No E-service      1 56410.08
## 8      No  Male     Yes     Yes     Yes Total service      0 42511.20
## 9      No  Male      No      No      Yes Plus service      0 339592.36
## 10     No  Male      No      No      No E-service      0 568552.13
## 11     No Female      No      Yes     No Basic service      1 19618.09
## 12     No Female     Yes     No      Yes Plus service      0 103920.72
## 13     No Female      No      No      No Basic service      0 97497.46
## 14     No Female     Yes     Yes     Yes Total service      1 290630.13
## 15     No Female      No      No      No Basic service      0 70162.30
## 16     No  Male      No      Yes     No E-service      0 115868.49
## 17     No  Male      No      No      Yes Plus service      0 989563.61
## 18     No Female      No      No      Yes Plus service      0 161912.93
## 19     No  Male      No      No      No Basic service      0 31279.38
## 20     No  Male     Yes     Yes     Yes Total service      1 37060.03
## 21     No Female      No      Yes     No E-service      1 58200.40
## 22     No  Male      No      No      Yes Basic service      0 248174.27
## 23     No Female     Yes     Yes     Yes Total service      0 36496.52
## 24     No  Male      No      No      No Basic service      0 233178.54
```

```
# Comparing CLVs by gender
ggplot(examine_data, aes(x = CLV, color = gender)) +
  labs(title = "CLV Density By Gender") +
  geom_density()
```

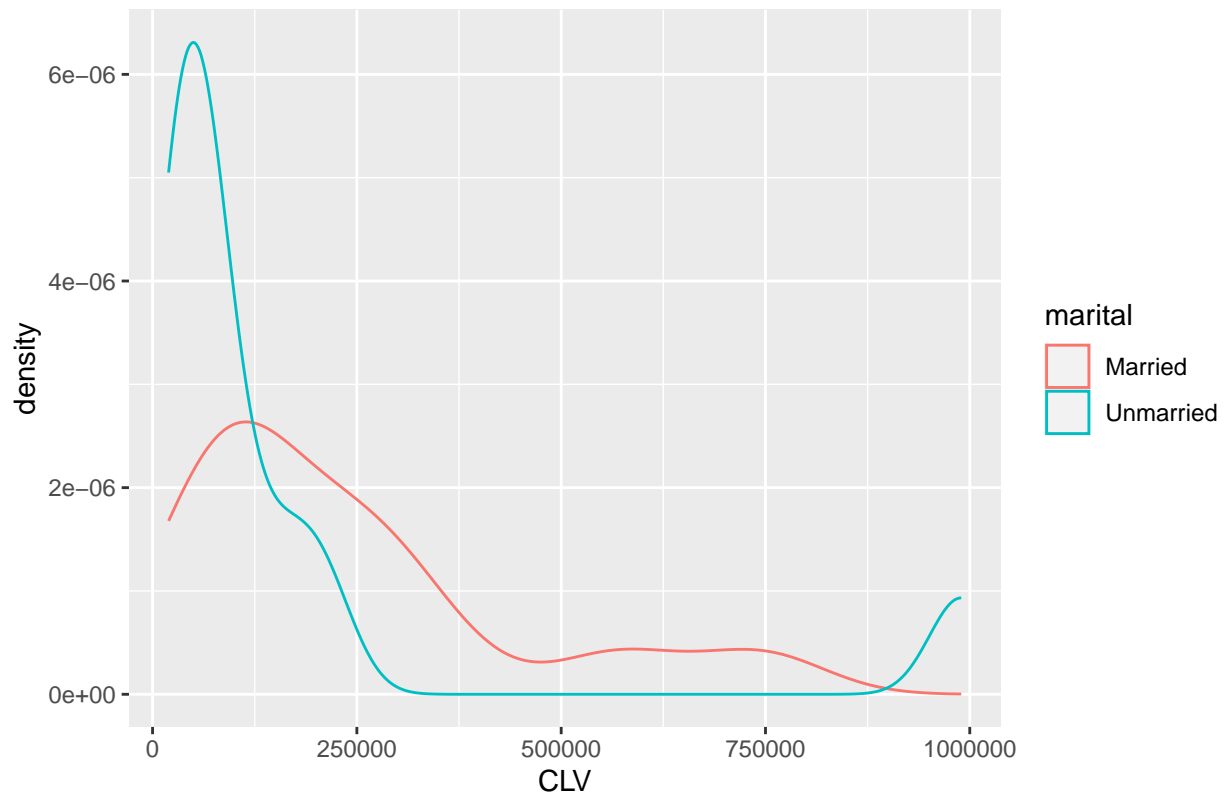


From this graph we can see variations in CLV between males and females focused on the first 24 months for simplification. It's apparent that males tend to exhibit lower initial spending compared to females, but as time progresses, males make more consistent and higher-value purchases. Interestingly, both genders typically make a single substantial purchase at the outset, followed by consistent smaller purchases over time.

##CLV Comparison: Married and Unmarried customers

```
ggplot(examine_data, aes(x = CLV, color = marital)) +  
  labs(title = "Customer Lifetime Value Density by Marital Status") +  
  geom_density()
```

Customer Lifetime Value Density by Marital Status



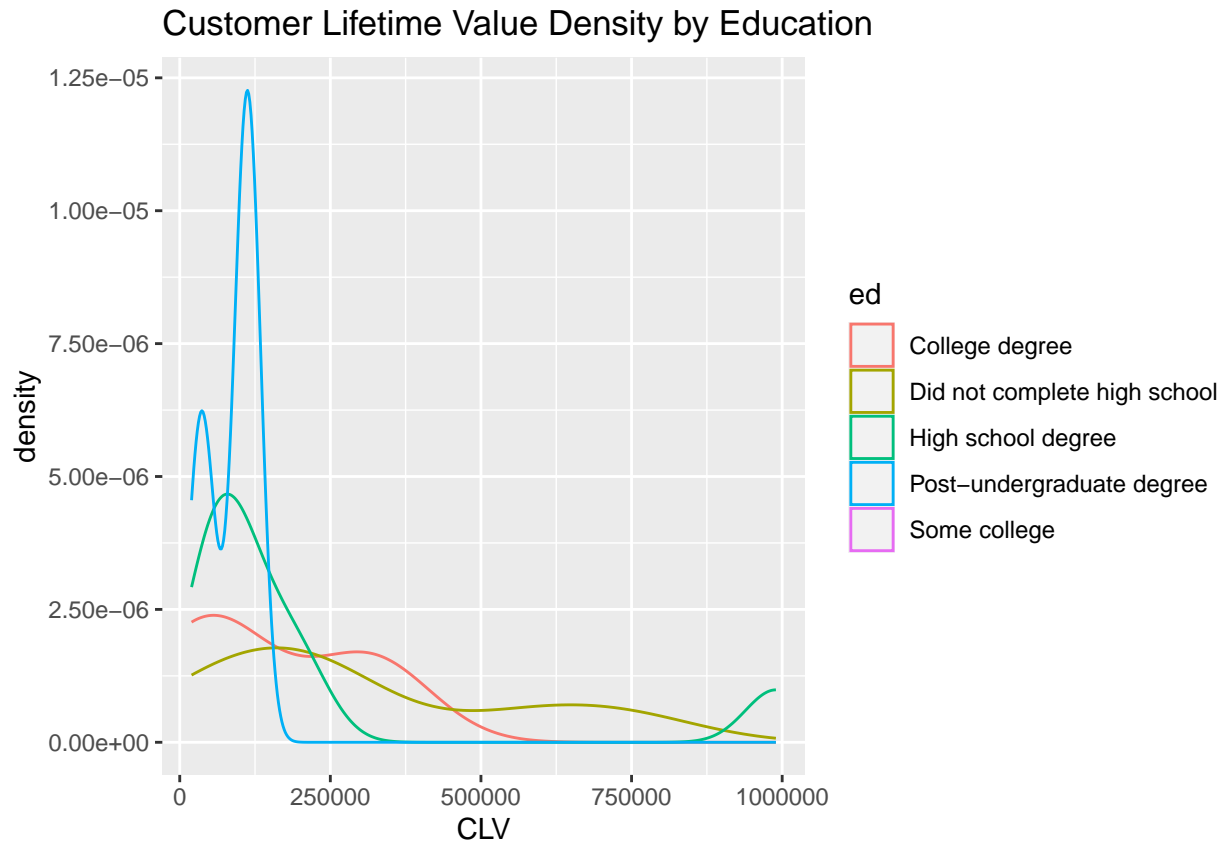
From this comparison of CLV s ov married and unmarried customers we can see that singles typically start with significant purchases but then show inconsistency over time. Married individuals, however, make smaller but consistent purchases after an initial large one. At the end of the graph we can also see that unmarried individuals can start soing purchases after long time not showing any activity.

##CLV Comparison: Education

```
ggplot(examine_data, aes(x = CLV, color = ed)) +
  labs(title = "Customer Lifetime Value Density by Education") +
  geom_density()
```

Warning: Groups with fewer than two data points have been dropped.

Warning in max(ids, na.rm = TRUE): no non-missing arguments to max; returning
-Inf



This graph shows analysis of customers' education levels. Those without high school diplomas tend to make consistent purchases over time. Customers with post-undergraduate degrees initially make high-value purchases but then decrease fastly. This could be because they opt for premium products early on. Customers with only college degree show inconsistent purchasing behavior, likely due to experimenting with different products. High school graduates behave similarly to those with post-undergraduate degrees but start with lower-priced purchases. Overall, both groups demonstrate consistency in their purchasing patterns.

Final conclusions

Based on the findings, the most valuable clients for long-term business success appear to be married individuals. They demonstrate consistent purchasing behavior over time, which is a positive indicator for the business. Next in line are male customers, who also exhibit a consistent purchasing pattern. Regarding education, those who did not complete high school tend to make frequent purchases. Additionally, customers with post-undergraduate degrees make high-value purchases, contributing significantly to the business. Overall, considering consistency and high-value purchases, married males emerge as the most valuable clients.

Retention rate

```
# Estimate churn rate for yearly prediction (considering 12 months)
churn_rate <- mean(predictions <= 12)

# Calculate total number of customers
total_customers <- nrow(data)
```

```
# Determine the count of at-risk customers
at_risk_customers <- total_customers * churn_rate

# Compute the average Customer Lifetime Value (CLV)
average_clv <- mean(data$CLV)

# Calculate the retention budget
retention_budget <- at_risk_customers * average_clv
retention_budget
```

```
## [1] 3937142
```

What else would I suggest for retention?

To improve retention, it's crucial to segment at-risk customers and assess their value to the company. By that we will understand is that customer worthy for spending resources or not (focus resources on retaining high-value customers). For valuable at-risk customers, we can implement targeted promotions and discounts. Another effective strategy is to maintain regular communication with customers through surveys or events to enhance loyalty and ensure continued engagement.