## 5. Association Rules Mining

## Apriori algorithm

"Apriori is an algorithm for frequent item set mining and association rule learning over transactional databases. It proceeds by identifying the frequent individual items in the database and extending them to larger and larger item sets as long as those item sets appear sufficiently often in the database. The frequent item sets determined by Apriori can be used to determine association rules which highlight general trends in the database: this has applications in domains such as market basket analysis." [1 [https://en.wikipedia.org/wiki/Apriori\_algorithm]]

#### Association rules

- Association rule: implication in the form  $X \Rightarrow Y$ , where X, Y is the subset of the set of items I
- Support: Percentag of occurrence of X U Y in a transaction database D
- Confidence: Ratio of the count of transactions in the set of transactions D that contain X and Y to the count of transactions in the set D that contain X.

## Apriori algorithm - Observation

- Subset of each frequent itemset occurres at least as often as the original itemset.
- No itemset occurres more often than any of its subests.

## Apriori - computation

- $L_k$ : Set of frequent itemsets of size k (with min support)
- $C_k$ : Set of candidate itemset of size k (potentially frequent itemsets)

$$\begin{split} L_{l} &= \{ \text{frequent items} \}; \\ & \textbf{for } (k=1; L_{k} ! = \varnothing; k++) \textbf{ do} \\ & C_{k+1} = \text{candidates generated from } L_{k}; \\ & \textbf{ for each } \text{ transaction } t \text{ in database do} \\ & \text{increment the count of all candidates in } \\ & C_{k+1} \text{ that are contained in } t \\ & L_{k+1} = \text{candidates in } C_{k+1} \text{ with min\_support} \\ & \textbf{return } \cup_{k} L_{k}; \end{split}$$

Apriori - candidates generation

**Input**:  $L_{i-1}$ : set of frequent itemsets of size i-1

**Output**:  $C_i$ : set of candidate itemsets of size i.

 $C_i = empty set;$ 

 $\mathbf{for} \ \mathrm{each} \ \underline{\mathrm{itemset}} \ J \ \mathrm{in} \ L_{i\text{--}1} \ \mathbf{do}$ 

for each itemset K in  $L_{i-1}$  s.t.  $K \le J$  do

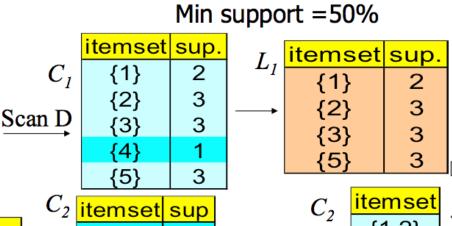
if i-2 of the elements in J and K are equal then if all subsets of  $\{K \cup J\}$  are in  $L_{i-1}$  then

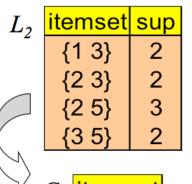
$$C_i = C_i \cup \{K \cup J\}$$

return  $C_i$ ;

Apriori - example

# The Apriori Algorithm — Example





Database D

134

TID Items

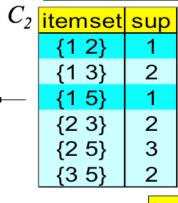
200 2 3 5

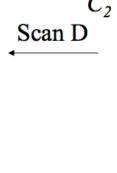
300 1 2 3 5

25

100

400





{1 2} {1 3} {1 5} {2 3} {2 5} {3 5}

$$C_3$$
 itemset  $\{2\ 3\ 5\}$ 

 $L_3$  itemset sup  $\{2\ 3\ 5\}$  2

Generation of association rules

for each frequent itemset I do

for each subset C of I do

if  $(\operatorname{support}(I) / \operatorname{support}(I - C) >= \operatorname{minconf})$  then output the rule  $(I - C) \Rightarrow C$ , with confidence =  $\operatorname{support}(I) / \operatorname{support}(I - C)$ and  $\operatorname{support} = \operatorname{support}(I)$ 

Tools

- pandas Python Data Analysis Library
  - Great for data munging and preparation, but less so for data analysis and modeling.
  - Helps fill this gap, enabling you to carry out your entire data analysis workflow in Python without having to switch to a more domain specific language like R.
  - A fast and efficient DataFrame object for data manipulation with integrated indexing;
  - Tools for reading and writing data between in-memory data structures and different formats: CSV and text files, Microsoft Excel, SQL databases, and the fast HDF5 format;
    - http://pandas.pydata.org/ [http://pandas.pydata.org/]

#### Virtualenv

```
# https://virtualenv.pypa.io/en/stable/userguide/
# create env
virtualenv ddw-tutorial-5
# virtualenv --system-site-packages ddw-tutorial-5
# activate
source ddw-tutorial-5/bin/activate
# operations ...
pip install ...
# deactivate and remove
deactivate
rm -r ./ddw-tutorial-5
```

#### Installation

```
pip install pandas
```

## **Basic Operations**

```
# Reading csv to a data frame
import pandas as pd

df = pd.read_csv('bank-data.csv')

# print head(tail) of the data frame
print(df.head()) # df.tail()

# select column
print(df[['age', 'car']])

# select by index
print(df.iloc[3:6,5:9])

# delete column
del df["id"]
print(df.head())

# discretize continous values to categorical values
df["income"] = pd.cut(df["income"],10)
print(df.head())
```

#### Output

```
# print head(tail) of the data frame
         id age
                                        income married
                     sex
                              region
                                                       children
                                                                  car save_act
0
   ID12101
             48
                 FEMALE
                         INNER_CITY
                                       17546.0
                                                    NO
                                                               1
3
                                                                   NO
                                                                            NO
                                      30085.1
                                                                  YES
                   MALE
                                TOWN
                                                   YES
                                                                            NO
   ID12102
              40
   ID12103
             51 FEMALE
                          INNER_CITY
                                      16575.4
                                                   YES
                                                                  YES
                                                                            YES
3
   ID12104
              23
                  FEMALE
                                TOWN
                                       20375.4
                                                                   NO
                                                                            NO
4
                               RURAL
   TD12105
             57
                 FFMALE
                                      50576.3
                                                   YFS
                                                                   NO
                                                                           YFS
  current_act mortgage
                         pep
Θ
           NΩ
                     ÑΩ
                         YES
           YES
1
                    YES
                          NO
           YES
                     NO
                          NO
4
           N0
                     NO
                          NO
  select column
0
      48
           N0
       40
          YES
       51
          YES
: 3
       23
           N0
[600 rows x 2 columns]
# select by index
  married children car save_act
3
       YES
                      NO
                               NO
                   0
       YES
                      NO.
                              YES
5
                      NO
       YES
                              YES
# delete column
                     region
                             income married children car save act \
```

```
FEMALE INNER CITY
                                17546.0
                                               NO
0
     48
                                                                NO
                                                                          N0
                          TOWN
           MALE
                                30085.1
                                                               YES
                  INNER_CITY
     51
         FFMALE
                                16575.4
                                              YFS
                                                           0
                                                               YES
                                                                         YES
          FEMALE
                         TOWN
                                20375.4
                                              YES
                                                                NO
                                                                          NO
3
                                                           3
                        RURAL
         FEMALE
                                50576.3
                                                                NO
                                                                         YES
   current_act mortgage NO NO
                            pep
YES
0
            YES
            YES
                       NO
                             NO
3
            YES
                       NO
                             NO
             NO
                       NO
                             NO
# discretize continous values to categorical values
             sex
                       region
                                                  income married children
                                                                               car
                  INNER_CITY
TOWN
         FEMALE
                                (16637.388, 22448.977]
     40
           MALE
                                (28260.566, 34072.155]
                                                               YFS
                                                                            3
                                                                                YFS
                  INNER_CITY
TOWN
         FEMALE
                                (10825.799, 16637.388]
(16637.388, 22448.977]
                                                                            0
     51
                                                               YES
                                                                                YES
     23
         FEMALE
                                                               YES
                                                                                 N0
                                                                            3
4
     57
         FEMALE
                        RURAL
                                (45695.333, 51506.922]
                                                               YES
                                                                             0
                                                                                 NO
   save_act current_act mortgage
                                     pep
0
                       N0
                                      YES
         NΩ
                      YES
                                YFS
                                       NO
        YES
                      YES
                                 NO
                                       NO
                                       N0
         NO
                      YES
                                 N0
                       NO
                                 NO
                                       N0
```

## Apriori algorithm implementation

```
from collections import Counter
def frequentItems(transactions, support):
     counter = Counter()
     for trans in transactions:
         counter.update(frozenset([t]) for t in trans)
     return set(item for item in counter if counter[item]/len(transactions) >= support), counter
def generateCandidates(L, k):
     candidates = set()
     for a in L:
         for b in L:
             union = a \mid b
             if len(union) == k and a != b:
                 candidates.add(union)
     return candidates
def filterCandidates(transactions, itemsets, support):
     counter = Counter()
     for trans in transactions:

subsets = [itemset for itemset in itemsets if itemset.issubset(trans)]
         counter.update(subsets)
     return set(item for item in counter if counter[item]/len(transactions) >= support), counter
def apriori(transactions, support):
     result = list()
resultc = Counter()
     candidates, counter = frequentItems(transactions, support)
     result += candidates
     resultc += counter
     while candidates:
         candidates = generateCandidates(candidates, k)
         candidates,counter = filterCandidates(transactions, candidates, support)
         result += candidates
         resultc += counter
         k += 1
     resultc = {item:(resultc[item]/len(transactions)) for item in resultc}
     return result, resultc
```

## Example

```
dataset = [
    ['bread', 'milk'],
    ['bread', 'diaper', 'beer', 'cola'],
    ['milk', 'diaper', 'beer', 'cola'],
    ['bread', 'milk', 'diaper', 'beer'],
    ['bread', 'milk', 'diaper', 'cola'],
]

frequentItemsets, supports = apriori(dataset, 0.1)
for f in frequentItemsets:
    print("{} - {}".format(f, supports[f]))

frozenset({'cola'}) - 0.4
frozenset({'beer'}) - 0.6
frozenset({'bread'}) - 0.8
frozenset({'bread'}) - 0.8
frozenset({'diaper'} - 0.8
frozenset({'diaper'} - 0.6
frozenset({'diaper', 'milk'} - 0.6
frozenset({'diaper', 'milk'} - 0.6
frozenset({'diaper', 'milk'} - 0.6
frozenset({'diaper', 'milk'} - 0.6
frozenset({'bread', 'milk'} - 0.6
frozenset({'bread', 'milk'} - 0.6
frozenset({'bread', 'diaper'} - 0.6
frozenset({'bread', 'diaper', - 0.6
frozenset({'diaper', - 0.01a'} - 0.4
frozenset({'diaper', 'cola'} - 0.4
fr
```

```
frozenset({'bread', 'diaper', 'milk'}) - 0.4
frozenset({'diaper', 'milk', 'cola'}) - 0.4
frozenset({'bread', 'diaper', 'beer'}) - 0.4
frozenset({'diaper', 'beer', 'milk'}) - 0.4
```

### Tasks

#### Implementation

- Complete the implementation about the generation of association rules
- Allow setting of minimum confidence value for each rule
  - the output can be printed to the console
    - provide information about antecedent, consequent, support and confidence of the rule
    - e.g. {a=1,b=2} -> {c=3}, support=0.5, confidence=0.3
    - optionally allow sorting by support, confidence, or rule length
- Implement other metric of your choice [1 [https://en.wikipedia.org/wiki/Association\_rule\_learning]]
  - $lift(X o Y) = rac{support(X \cup Y)}{support(X) imes support(Y)}$
  - $ullet conviction(X 
    ightarrow Y) = rac{1-support(Y)}{1-confidence(X 
    ightarrow Y)}$

#### Data Analysis

- Perform association rules mining on the example dataset containing bank data.
  - bank-data.zip
- Experiment with different settings of metrics (confidence, optionally lift and conviction). Which settings and metric works best for your use case.
- Try another dataset from UCI repository
  - e.g. subset of datasets in CSV http://repository.seasr.org/Datasets/UCI/csv/ [http://repository.seasr.org/Datasets/UCI/csv/]

#### Code Example

/mnt/www/courses/MI-DDW.16/data/pages/tutorials/05/start.txt  $\cdot$  Poslední úprava: 2017/04/23 08:19 autor: kuchajar naturalní verbiene ver