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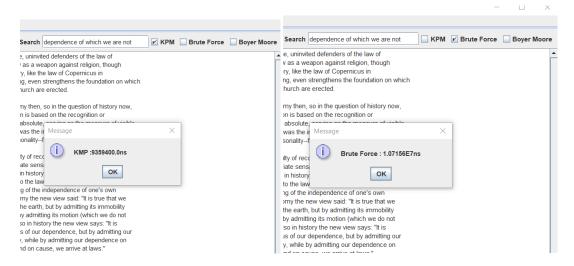
#### Comp261 Assignment 5

## **Question 1:**

Write a short summary of the performance you observed using the two search algorithms.

KMP algorithm preformed faster search than brute force algorithm. For example, below are some measures that compares both algorithms using war\_and\_peace.txt,

word search: dependence of which we are not



## **Question 2:**

- Report the binary tree of codes your algorithm generates
- -> 111010
- -> 111001
- -> 110
- ! -> 1110000111
- " -> 11111010
- '-> 111000010
- (-> 011000111000
- ) -> 1111101111111
- \* -> 11111011010010
- , -> 1111111

- --> 100101001
- . -> 1110001
- /-> 011000111001010111110
- 0 -> 111110110100001
- 1 -> 11111011010001
- 2 -> 111110110100000
- 3 -> 0110001110010111
- 4 -> 01100011100101010
- 5 -> 0110001110010100
- 6 -> 0110001110010110
- 7 -> 01100011100111110
- 8 -> 01100011100100
- 9 -> 01100011100111101
- : -> 111000001001
- ; -> 111110110101
- = -> 011000111001010111111
- ? -> 1001010100
- A -> 011000110
- B -> 1110000001
- C -> 01100010000
- D -> 11111011000
- E -> 01100010001
- F -> 11100000101
- G -> 111110111101
- H -> 1110000011
- I -> 100101011
- J -> 11111011010011
- K -> 111110111100
- L -> 1111101111110
- M -> 1001010101
- N -> 1110000000
- O -> 01100011101

- P -> 011000101
- Q -> 01100011100111111
- R -> 11111011011
- S -> 0110001111
- T -> 100101000
- U -> 01100011100110
- V -> 111000001000
- W -> 0110001001
- X -> 01100011100111100
- Y -> 111110111110
- $Z \rightarrow 011000111001110$
- à -> 0110001110010101110
- a -> 1000
- b -> 1111100
- c -> 101111
- $d \rightarrow 10110$
- ä -> 011000111001010111100
- e -> 000
- f -> 100110
- g -> 100100
- h -> 0011
- é -> 0110001110010101111010
- i -> 0100
- j -> 11111011001
- ê -> 011000111001010110
- k -> 0110000
- I -> 01101
- m -> 101110
- n -> 0101
- o -> 0111
- p -> 1111110
- q -> 11111011101

r -> 11110

s -> 0010

t -> 1010

u -> 111011

v -> 1001011

w -> 100111

x -> 1110000110

y -> 011001

z -> 11111011100

-> 0110001110010101111011

The final size of War and Peace after Huffman coding.

input length: 3258246 bytes

output length: 1848598 bytes

# **Question 3:**

war\_and\_peace.txt: Original length: 3258246 bytes

Output length: 1848598 bytes

Reduction in size: 43.26%

taisho.txt: Original length: 3649944 bytes

Output length: 1542656 bytes

Reduction in size: 57.73%

pi.txt: Original length: 1010003 bytes

Output length: 443632 bytes

Reduction in size: 56.08%

Which of these achieves the best compression, i.e. the best reduction in size?

The best compression achieve is taisho.txt

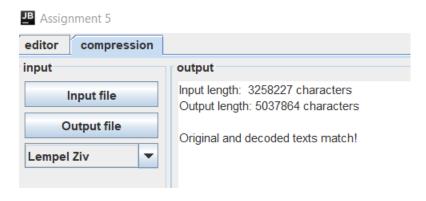
What makes some of the encodings better than others?

This is because of the size of the character where some are small than the others such as taisho.txt has small character set.

**Question 4**: The Lempel-Ziv algorithm has a parameter: the size of the sliding window.

On a text of your choice Using war\_and\_peace.txt, the original size is 3258227 characters

For window size: 40000



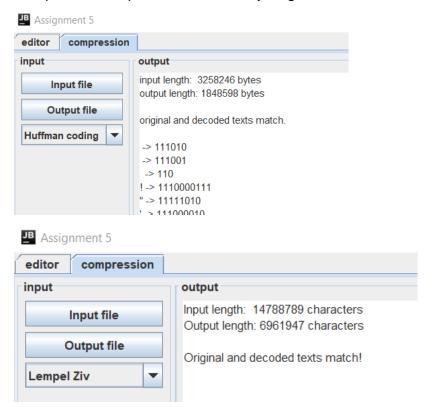
For window size: 50000



How does changing the window size affect the quality of the compression?

Based on the output, it shows when the window size increased then the output of the compression size will be decreased in the file. This is because a larger compression file size could happen due to the way of formatting the output. The increased in size of the file because text is stored using the braces, comma, delimiters, the length and offset numbers. A better option of storing the data by using the four bytes where 2bytes for offset, the 3<sup>rd</sup> byte for length and 4<sup>th</sup> byte is for character this is for handling chucks of data. In addition, according to the data, allocate the maximum number of bits and record them by using the per block for compression.

**Question 5**: What happens if you Huffman encode War and Peace before applying Lempel-Ziv compression to it? Do you get a smaller file size (in characters) overall?



Yes, based on the result above, using the war\_and\_peace.txt with original size is 3258246 characters in length for Huffman encoding which outputted in binary which is 14788789 characters. This mean it has reduced by half in size and then used it to do Lempel-Ziv compression, the final output which is 6961947 characters showed the size of length has been increased which is due to some additional character such as the braces, comma, delimiters, the length and offset numbers.

# Part4: Ngrams:

Finds the ngrams probabilities for characters in the whakatauki

Prefix: tak|a (which mean tak followed by "a") n:3 Probability: 0.0010559662. Note that the result is obtained after applying "back-off" (n (5-2))

# Finds the log probability for the test that is in English

Using n-gram table the log probability of those two new string is as follows:

Turn your face to the sun and the shadows fall behind you, translation

```
NB: _(Underscore) is used to represent white
                                                                                                                                                                                                                                                                                             _fa1|1
                                                                                                                                                                                                                                                                                                                            n:4 Prob: 0.7477876
space and \((or sign)\) is used to indicate next
                                                                                                                                                                                                                                                                                           fa11|_
                                                                                                                                                                                                                                                                                                                            n:4 Prob: 0.3068783
                                                                                                                                                                                                                                                                                           all_|b
                                                                                                                                                                                                                                                                                                                            n:4 Prob: 0.037077032
character
                                                                                                                                                                                                                                                                                          11_b | e
                                                                                                                                                                                                                                                                                                                            n:4 Prob: 0.8068182
                                                                                                                                                                                n:4 Prob: 0.10454246
                                                                                                                                         the |s
                                                                                                                                                                                                                                                                                          1_be|h
                                                                                                                                                                                                                                                                                                                            n:4 Prob: 0.003236246
Turn|_
                                                         Prob: 0.2857143
                                                                                                                                                                              n:4 Prob: 0.06284093
                                      n:4
                                                                                                                                         he s|u
                                                                                                                                                                                                                                                                                                                            n:4 Prob: 0.82894737
                                                                                                                                                                                                                                                                                           beh|i
                                                          Prob: 0.0056179776
                                                                                                                                         e_su|n
                                                                                                                                                                               n:4 Prob: 0.12790698
urn_|y
                                      n:4
                                                                                                                                                                                                                                                                                          behi|n
                                                                                                                                                                                                                                                                                                                            n:4 Prob: 0.9152047
                                                         Prob: 0.8333333
                                                                                                                                                                               n:4 Prob: 0.28695652
rn v o
                                      n:4
                                                                                                                                         sun|
                                                                                                                                                                                                                                                                                          ehin | d
                                                                                                                                                                                                                                                                                                                            n:4 Prob: 1
n_yo|u
                                      n:4 Prob: 1
                                                                                                                                         sun_|a
                                                                                                                                                                               n:4 Prob: 0.22222222
                                                                                                                                                                                                                                                                                                                            n:4 Prob: 0.72328764
                                                                                                                                                                                                                                                                                          hindl
                                      n:4 Prob: 0.18479016
                                                                                                                                         un_a|n
                                                                                                                                                                              n:4 Prob: 0.26086956
you|r
                                                                                                                                                                                                                                                                                          ind_|y
                                                                                                                                                                                                                                                                                                                            n:4 Prob: 0.009731731
                                                                                                                                                                                n:4 Prob: 0.7039877
your|_
                                      n:4 Prob: 0.7655334
                                                                                                                                         n_an|d
                                                                                                                                                                                                                                                                                          nd_y|o
                                                                                                                                                                                                                                                                                                                            n: 2 Prob: 0.7345133
                                                                                                                                                                                                                                                                                                                            n:4 Prob: 1
                                                                                                                                                                                                                                                                                          d_yo|u
our |f
                                      n:4 Prob: 0.06315789
                                                                                                                                        _and|_
                                                                                                                                                                               n:4 Prob: 0.890655
                                                                                                                                                                                                                                                                                                                            n:4 Prob: 0.062137723
                                                                                                                                                                                                                                                                                           _you|,
                                      n:4 Prob: 0.5263158
ur_f|a
                                                                                                                                         and_|s
                                                                                                                                                                                n:4 Prob: 0.092595376
                                                                                                                                                                                                                                                                                                                            n:4 Prob: 0.6847826
                                                                                                                                                                                                                                                                                          you, |
                                      n:4 Prob: 0.4293478
                                                                                                                                         nd_s|h
                                                                                                                                                                               n:4 Prob: 0.16666667
r fa|c
                                                                                                                                                                                                                                                                                          ou,_|t
                                                                                                                                                                                                                                                                                                                            n:4 Prob: 0.014851485
  _fac|e
                                      n:4 Prob: 0.8169827
                                                                                                                                         d sh|a
                                                                                                                                                                                n:4 Prob: 0.09608541
                                                                                                                                                                                                                                                                                          u,_t|r
                                                                                                                                                                                                                                                                                                                            n: 2 Prob: 0.033236995
face |_
                                      n:4 Prob: 0.44354838
                                                                                                                                         _sha|d
                                                                                                                                                                               n:4 Prob: 0.092819616
                                                                                                                                                                                                                                                                                          ,_tr|a
                                                                                                                                                                                                                                                                                                                            n:4 Prob: 0.12173913
                                      n:4 Prob: 0.099585064
                                                                                                                                                                                n:4 Prob: 0.4716981
                                                                                                                                         shad|o
ace_|t
                                                                                                                                                                                                                                                                                           _tra|n
                                                                                                                                                                                                                                                                                                                            n:4 Prob: 0.3671875
ce_t|o
                                      n:4 Prob: 0.35490605
                                                                                                                                         hado|w
                                                                                                                                                                                n:4 Prob: 1
                                                                                                                                                                                                                                                                                                                            n:4 Prob: 0.70212764
                                                                                                                                                                                                                                                                                          tran|s
                                                                                                                                                                                                                                                                                                                            n:4 Prob: 0.065656565
                                      n:4 Prob: 0.7316547
                                                                                                                                         adow|s
                                                                                                                                                                                n:4 Prob: 0.42
                                                                                                                                                                                                                                                                                         rans | 1
e_to|_
                                                                                                                                                                                                                                                                                                                            n:4 Prob: 0.7692308
                                      n:4 Prob: 0.19636564
                                                                                                                                         dows |_
                                                                                                                                                                                n:4 Prob: 0.51111114
                                                                                                                                                                                                                                                                                          ansl|a
_to_|t
                                                                                                                                                                                                                                                                                          nslalt
                                                                                                                                                                                                                                                                                                                            n:4 Prob: 0.8333333
                                      n:4 Prob: 0.8855353
                                                                                                                                                                                n:4 Prob: 0.031496063
to_t|h
                                                                                                                                         ows_|f
                                                                                                                                                                                                                                                                                           slatli
                                                                                                                                                                                                                                                                                                                            n:4 Prob: 0.3846154
                                      n:4 Prob: 0.87489265
                                                                                                                                                                                n: 2 Prob: 0.29657292
o th | e
                                                                                                                                         ws f | a
                                                                                                                                                                                                                                                                                                                            n:4 Prob: 0.7481203
                                                                                                                                                                                                                                                                                          lati | o
                                      n:4 Prob: 0.08106648
                                                                                                                                         s_fa|1
                                                                                                                                                                                n:4 Prob: 0.03259259
the|
                                                                                                                                                                                                                                                                                          atio|n
                                                                                                                                                                                                                                                                                                                            n:4 Prob: 0.99680513
                                   \log_{10}(0.2857143) + \log_{10}(0.0056179776) + \log_{10}(0.8333333) + \log_{10}(1) + \log_{10}(0.18479016) + \log_{10}(0.7655334) \\ = -3.72302629772 \dots \\ -3.7230262972 \dots \\ -3.72302972 \dots \\ -3.72302 \dots \\ -3.72
                                                                      -3.72302629772 + \log_{10}(0.06315789) + \log_{10}(0.5263158) + \log_{10}(0.4293478) + \log_{10}(0.8169827) \\ = -5.65633017533 \dots \\ -3.72302629772 + \log_{10}(0.06315789) + \log_{10}(0.5263158) + \log_{10}(0.4293478) + \log_{10}(0.8169827) \\ = -5.65633017533 \dots \\ -3.72302629772 + \log_{10}(0.06315789) + \log_{10}(0.5263158) + \log_{10}(0.4293478) + \log_{10}(0.8169827) \\ = -5.65633017533 \dots \\ -3.72302699772 + \log_{10}(0.06315789) + \log_{10}(0.5263158) + \log_{10}(0.8493478) + \log_{10}(0.8169827) \\ = -5.65633017533 \dots \\ -3.7230269972 + \log_{10}(0.8493478) + \log_{10}(0.849
```

```
-3.72302629772 + \log_{10}(0.06315789) + \log_{10}(0.5263158) + \log_{10}(0.4293478) + \log_{10}(0.8169827) = -5.65633017533 \dots \\ -5.65633017533 + \log_{10}(0.44354838) + \log_{10}(0.099585064) + \log_{10}(0.35490605) + \log_{10}(0.7316547) + \log_{10}(0.19636564) = -8.30370990427 \dots \\ -8.30370990427 + \log_{10}(0.8855353) + \log_{10}(0.87489265) + \log_{10}(0.08106648) + \log_{10}(0.10454246) + \log_{10}(0.06284093) = -11.6881726233 \dots \\ -11.6881726233 + \log_{10}(0.12790698) + \log_{10}(0.26695652) + \log_{10}(0.22222222) + \log_{10}(0.26086956) + \log_{10}(0.7039877) = -14.5126863226 \dots \\ -14.5126863226 + \log_{10}(0.890655) * \log_{10}(0.092595376) + \log_{10}(0.16666667) + \log_{10}(0.09608541) = -16.2562093865 \dots \\ -16.2562093865 + \log_{10}(0.092819616) + \log_{10}(0.4716981) + \log_{10}(0.142) + \log_{10}(0.51111114) = -18.2831408550 \dots \\ -18.2831408550 + \log_{10}(0.031496063) + \log_{10}(0.29657292) + \log_{10}(0.03259259) + \log_{10}(0.7477876) + \log_{10}(0.3068783) = -22.4388897789 \dots \\ -22.4388897789 + \log_{10}(0.037077032) + \log_{10}(0.8068182) + \log_{10}(0.03236246) + \log_{10}(0.82894737) = -26.5344406461 \dots \\ -26.5344406461 + \log_{10}(0.9152047) + \log_{10}(0.12173913) + \log_{10}(0.72328764) + \log_{10}(0.014851485) = -32.0587436685 + \log_{10}(0.033236995) + \log_{10}(0.12173913) + \log_{10}(0.3671875) + \log_{10}(0.70212764) = -35.0403877648 \dots \\ -35.0403877648 + \log_{10}(0.065656565) + \log_{10}(0.7692308) + \log_{10}(0.8333333) + \log_{10}(0.3846154) + \log_{10}(0.74781203) + \log_{10}(0.99680513) = -36.9586258323 \dots \\ -35.0403877648 + \log_{10}(0.0656565656) + \log_{10}(0.7692308) + \log_{10}(0.8333333) + \log_{10}(0.3846154) + \log_{10}(0.7481203) + \log_{10}(0.99680513) = -36.9586258323 \dots \\ -35.0403877648 + \log_{10}(0.065656565) + \log_{10}(0.7692308) + \log_{10}(0.8333333) + \log_{10}(0.3846154) + \log_{10}(0.7481203) + \log_{10}(0.99680513) = -36.9586258323 \dots \\ -36.9586
```

logPob (string) =  $\sum_{j} logProb(jth \ letter)$ Therefore LogProb(English

The log probabilities for English version is -36.9586258323

Finds the log probability for the test that is in Te Reo

# For the Te Reo version:

# Hurihia to aroaro ki te ra tukuna to atarangi kia taka ki muri i a koe

Hu r ur i ri h ih i hi a ia _ a_ t	n:2 Prob: 0.69863015 n:2 Prob: 0.076125 n:0 Prob: 0.04988357 n:2 Prob: 1 n:2 Prob: 3.1535793E-4 n:2 Prob: 0.047173083 n:2 Prob: 0.059052452		
_t o	n:2 Prob: 0.23747851		
to  _	n:2 Prob: 0.6661312		
o_ a	n:2 Prob: 0.06780819		
_a r	n:2 Prob: 0.050021842		
ar o	n:2 Prob: 0.020478783		
ro a	n:2 Prob: 0.054253183		
oa r	n:2 Prob: 0.087936044	tu   k	n:2 Prob: 8.1135903E-4
ar o	n:2 Prob: 0.020478783		
ro _	n:2 Prob: 0.001786113	uk u	n:2 Prob: 0.016260162
o_ k	n:2 Prob: 0.01033349 n:2 Prob: 0.24792452		0 D 1 01/////
_k i ki _	n:2 Prob: 0.24792452 n:2 Prob: 0.06934307	ku n	n:2 Prob: 0.16666667
i_ t	n:2 Prob: 0.07883818	,,,,, l.o.	n:2 Prob: 0.024658175
_t e	n:2 Prob: 0.017018987	un a	II.2 Prob. 0.024036173
te _	n:2 Prob: 0.11733703	na _	n:2 Prob: 0.16777408
e_ r	n:2 Prob: 0.03199047		
_r a	n:2 Prob: 0.095168374	a_ t	n:2 Prob: 0.059052452
ra _	n:2 Prob: 0.008780488		2 D 1 0 22747051
a_ t	n:2 Prob: 0.059052452	_t o	n:2 Prob: 0.23747851
_t u	n:2 Prob: 0.009592043		

```
n:2 Prob: 0.6661312
to |_
           n:2 Prob: 0.06780819
o_|a
           n:2 Prob: 0.07809927
_a|t
           n:2 Prob: 0.048302542
at|a
           n:2 Prob: 0.057535816
ta|r
           n:2 Prob: 0.025470842
ar | a
ra|n
           n:2 Prob: 0.1909756
           n:2 Prob: 0.029984267
an | g
           n:2 Prob: 0.011726437
ng|i
           n:1 Prob: 0.00207
gi|_
i |k
           n:2 Prob: 0.0062240665
           n:2 Prob: 0.24792452
k|i
                                      i_|m
                                                  n:2 Prob: 0.010373444
ki|a
           n:1 Prob: 0.01743764
                                                  n:2 Prob: 0.083333336
                                      m|u
ia|
           n:2 Prob: 0.047173083
                                                  n:2 Prob: 0.036121674
                                      mu|r
           n:2 Prob: 0.059052452
a_|t
                                                  n:2 Prob: 0.076125
                                      ur|i
           n:2 Prob: 0.022622
_t|a
                                      ri|_
                                                  n:2 Prob: 4.5300112E-4
           n:2 Prob: 0.10853868
ta | k
                                                  n:2 Prob: 0.15145229
                                      i |a
           n:2 Prob: 0.014849551
ak|a
                                      _a|_
                                                  n:2 Prob: 0.14838526
           n:2 Prob: 0.2808399
ka|
                                      a_|k
                                                  n:2 Prob: 0.006006768
           n:2 Prob: 0.006006768
a_|k
                                                  n:2 Prob: 3.773585E-4
                                      k|o
k|i
           n:2 Prob: 0.24792452
                                                  n:1 Prob: 0.0026217978
                                      ko|e
           n:2 Prob: 0.06934307
ki|_
```

# logPob (string) = $\sum_{j} logProb(jth \ letter)$ Therefore, LogProb(whakatauki) =

```
 \log_{10}(0.69863015) + \log_{10}(0.076125) + \log_{10}(0.04988357) + \log_{10}(1) + \log_{10}(0.1535793E-4) \\ = -6.07746408712 ... \\ -6.07746408712 + \log_{10}(0.047173083) + \log_{10}(0.059052452) + \log_{10}(0.23747851) + \log_{10}(0.05661312) \\ = -9.43334780048 + \log_{10}(0.06780819) + \log_{10}(0.059052452) + \log_{10}(0.020478783) + \log_{10}(0.054253183) \\ = -14.8571766013 ... \\ -14.8571766013 + \log_{10}(0.087936044) + \log_{10}(0.020478783) + \log_{10}(0.001786113) + \log_{10}(0.01033349) \\ = -22.3355495782 + \log_{10}(0.24792452) + \log_{10}(0.06934307) + \log_{10}(0.07883818) + \log_{10}(0.017018987) \\ = -26.9725567355 + \log_{10}(0.11733703) + \log_{10}(0.09934307) + \log_{10}(0.09818374) + \log_{10}(0.008780488) \\ = -32.4760897206 + \log_{10}(0.059052452) + \log_{10}(0.09952043) + \log_{10}(0.16777408) + \log_{10}(0.016260162) \\ = -40.6026027262 + \log_{10}(0.16666667) + \log_{10}(0.024688175) + \log_{10}(0.07809927) + \log_{10}(0.059052452) \\ = -44.9928302361 + \log_{10}(0.23747851) + \log_{10}(0.06661312) + \log_{10}(0.06780819) + \log_{10}(0.07809927) + \log_{10}(0.048302542) \\ = -49.3857470320 ... \\ -49.3857470320 + \log_{10}(0.057535816) + \log_{10}(0.052470842) + \log_{10}(0.099756) + \log_{10}(0.01743764) \\ = -63.6468763009 + \log_{10}(0.047173083) + \log_{10}(0.059052452) + \log_{10}(0.022622) + \log_{10}(0.01743764) \\ = -63.6468763009 + \log_{10}(0.047173083) + \log_{10}(0.059052452) + \log_{10}(0.022622) + \log_{10}(0.01743764) \\ = -63.8118285715 + \log_{10}(0.04849551) + \log_{10}(0.02808399) + \log_{10}(0.076125) \\ = -80.8016561258 + \log_{10}(0.24792452) + \log_{10}(0.1545229) + \log_{10}(0.14838526) + \log_{10}(0.0606768) + \log_{10}(0.3773585E-4) + \log_{10}(0.076125) \\ = -94.019860536 ... \\ -80.8016561258 + \log_{10}(0.45300112E-4) + \log_{10}(0.1545229) + \log_{10}(0.006006768) + \log_{10}(0.006006768) + \log_{10}(0.006217788) \\ = -94.019860536 ... \\ -80.8016561258 + \log_{10}(0.45300112E-4) + \log_{10}(0.1545229) + \log_{10}(0.006006768) + \log_{10}(0.006006768) + \log_{10}(0.006217788) \\ = -94.019860536 ... \\ -80.8016561258 + \log_{10}(0.45300112E-4) + \log_{10}(0.1545259) + \log_{10}(0.006006768) + \log_{10}(0.006006768) + \log_{10}(0.0062617788) \\ = -94.0198660536 ... \\ -80.8016561258 + \log_{1
```

the log probabilities for Te Reo version is -94.0198960536

#### **Question 6:**

Explain (1 paragraph) why the two log probabilities are so different.

It is because the ngrams table that was built is based on English text, the chance of finding next character after the given prefix is higher in English compared to in Te Reo text. In addition, finding the following character/next character after the given prefix in Te Reo text will result in small probability because it is less likely to be the next character in English version which means the Te Reo log probability differ quite a lot compared to the English.

#### **Question 7:**

using this whakatauki: Titiro whakamuri kia haere whakamua

(a) War\_and\_peace.txt

```
Ti|t
         n:2
              Prob: 0.052287582
         n:2 Prob: 0.06509021
n:2 Prob: 0.015421722
n:2 Prob: 0.01270971
it|i
ti|r
ir|o
         n:2 Prob: 0.001786113
ro|_
o_|w
         n:2 Prob: 0.050514538
w|h
         n:2 Prob: 2.8677125E-5
         n:2 Prob: 0.17335945
wh|a
         n:2 Prob: 0.0024766407
n:2 Prob: 0.014849551
ha|k
ak|a
         n:2 Prob: 0.002624672
ka|m
===
am|u
         n:2 Prob: 0.014922098
         n:2 Prob: 0.036121674
mu|r
        n:2 Prob: 0.076125
n:2 Prob: 4.5300112E-4
n:2 Prob: 0.0062240665
ur|i
ri|
i_|k
k|i
         n:2 Prob: 0.24792452
ki|a
         n:1 Prob: 0.01743764
         n:2 Prob: 0.047173083
ia|_
         n:2 Prob: 0.045262266
a_|h
_h|a
         n:2 Prob: 0.24563798
         n:2 Prob: 0.0020638674
ha|e
ae|r
         n:2 Prob: 0.005988024
         n:2 Prob: 0.18708989
er|e
re|_
         n:2 Prob: 0.2677065
         n:2 Prob: 0.08050567
e_|w
w|h
         n:2 Prob: 0.2607324
         n:2 Prob: 0.17335945
wh|a
         n:2 Prob: 0.0024766407
halk
ak|a
         n:2 Prob: 0.014849551
====
ka|m
         n:2 Prob: 0.002624672
am|u
         n:2
               Prob: 0.014922098
         n:1 Prob: 0.020305352
mu|a
```

```
\begin{aligned} \log_{10}(0.052287582) + \log_{10}(0.06509021) + \log_{10}(0.015421722) + \log_{10}(0.01270971) + \log_{10}(0.001786113) + \log_{10}(0.050514538) &= -10.2204919405 \dots \\ -10.2204919405 + \log_{10}(2.8677125E-5) + \log_{10}(0.17335945) + \log_{10}(0.0024766407) + \log_{10}(0.014849551) + \log_{10}(0.002624672) &= -22.5393574445 \dots \\ -22.5393574445 + \log_{10}(0.014922098) + \log_{10}(0.036121674) + \log_{10}(0.076125) + \log_{10}(4.5300112E-4) + \log_{10}(0.0062240665) &= -32.4760588823 \dots \\ -32.4760588823 + \log_{10}(0.24792452) + \log_{10}(0.01743764) + \log_{10}(0.047173083) + \log_{10}(0.045262266) + \log_{10}(0.24563798) &= -38.1205256234 \dots \\ -38.1205256234 + \log_{10}(0.020638674) + \log_{10}(0.005988024) + \log_{10}(0.18708989) + \log_{10}(0.2677065) + \log_{10}(0.08050567) &= -45.4230245954 \dots \\ -45.4230245954 + \log_{10}(0.2607324) + \log_{10}(0.17335945) + \log_{10}(0.0024766407) + \log_{10}(0.014849551) &= -51.2023057447 \dots \\ -51.2023057447 + \log_{10}(0.002624672) + \log_{10}(0.014922098) + \log_{10}(0.020305352) &= -57.3017902961 \dots \end{aligned}
```

the log probabilities for whakatauki for war\_and\_peace.txt (n) is -57.3017902961 bits and then convert to bit-string =1/2 <sup>n</sup> = 1/2 <sup>-57.3017902961</sup> = **1.77646920891E+17** 

(b) the text at http://www.gutenberg.org/files/44897/44897.txt?

```
Tit|i
       n:3
             Prob: 0.25
iti|r
       n:3
             Prob: 0.017605634
tir|o
       n:3
             Prob: 0.41935483
       n:3
             Prob: 0.5135135
iro|
ro_w
       n:2
             Prob: 0.039887376
o w|h
       n:3
             Prob: 0.31764707
wh a
       n:3
             Prob: 0.25353926
wha|k
       n:3
            Prob:0.39318886
hak a
       n:3 Prob:0.88505745
aka|m
       n:3 Prob:0.045016076
kam|u
       n:3
             Prob:0.14285715
amu|r
       n:3
             Prob:0.18125
mur|i
       n:3
             Prob:0.6551724
uri|
       n:3
             Prob:0.23287672
ri_|k
       n:3
             Prob:0.03311258
i k|i
       n:3
             Prob:0.3617021
ki|a
       n:3
             Prob:0.110738255
kia|_
       n:3
             Prob: 0.45454547
ia_|h
       n:3
             Prob:0.06635071
a_h|a
       n:3
             Prob:0.50877196
ha|e
       n:3
             Prob:0.15370706
hae|r
       n:3
             Prob: 0.90654206
=====
aer e
             Prob:0.1903501
       n:3
             Prob:0.47826087
ere|_
       n:3
re_|w
       n:3
             Prob:0.03451582
e_w|h
       n:3
             Prob:0.26107225
_wh|a
             Prob:0.25353926
====
             Prob:0.39318886
wha|k
       n:3
hak|a
       n:3
             Prob:0.88505745
aka|m
       n:3
             Prob:0.045016076
kam|u
       n:3
             Prob:0.14285715
amu|a
             Prob:0.33333334
       n:3
```

```
 \log_{10}(0.25) + \log_{10}(0.017605634) + \log_{10}(0.41935483) + \log_{10}(0.5135135) + \log_{10}(0.039887376) + \log_{10}(0.31764707) = -4.92049448645 \dots 
 -4.92049448645 + \log_{10}(0.25353926) + \log_{10}(0.39318886) + \log_{10}(0.88505745) + \log_{10}(0.045016076) + \log_{10}(0.14285715) = -8.16660698413 \dots 
 -8.16660698413 + \log_{10}(0.18125) + \log_{10}(0.6551724) + \log_{10}(0.23287672) + \log_{10}(0.03311258) + \log_{10}(0.3617021) = -11.6465032486 \dots 
 -11.6465032486 + \log_{10}(0.110738255) + \log_{10}(0.45454547) + \log_{10}(0.06635071) + \log_{10}(0.50877196) + \log_{10}(0.15370706) + \log_{10}(0.90654206) = -15.2721777223 \dots 
 -15.2721777223 + \log_{10}(0.1903501) + \log_{10}(0.47826087) + \log_{10}(0.03451582) + \log_{10}(0.26107225) + \log_{10}(0.25353926) = -18.9541356375 \dots 
 -18.9541356375 + \log_{10}(0.39318886) + \log_{10}(0.88505745) + \log_{10}(0.045016076) + \log_{10}(0.14285715) + \log_{10}(0.333333334) = -22.0814145996 \dots
```

the log probabilities for whakatauki for given text (n) is -22.0814145996 bits and then convert to bit-string = 1/2  $^{n}$  = 1/2  $^{-22.0814145996}$  = **4437804.24420** 

# **Question 8:**

please refer to Question8.java