Term	Description	Term	Description	
Indices		Time se	Time series	
i	Generation technology	$d_{r,t}$	Demand, region r , time	
r , r'	Region		step t (GWh)	
t	Time step	$w_{r,t}$	Wind capacity factor, re-	
\mathbf{Sets}			gion r , time $t \in [0, 1]$	
${\mathcal I}$	Technologies: baseload (b) ,	$s_{r,t}$	Solar capacity factor, re-	
	peaking (p) , wind (w) , solar		gion r , time $t \in [0, 1]$	
	(s), unmet demand (u)	Decisio	on variables	
${\cal D}$	Decision variables	$cap_{i,r}^{gen}$	Generation capacity, tech-	
Parameters		- 7-	nology i , region r (GW)	
C_i^{gen}	Install cost, technology i	$\operatorname{cap}^{\operatorname{tr}}_{r,r'}$	Transmission capacity, re-	
	(£m/GWyr)	,	gion r to r' (GW)	
$C_{r,r'}^{\mathrm{tr}}$	Install cost, transmission,	$gen_{i,r,t}$	Generation, technology i ,	
,	region r to r' (£m/GWyr)		region r , time t (GWh)	
F_i^{gen}	Generation cost, technology	$\operatorname{tr}_{r,r',t}$	Transmission, region r to	
	i (£m/GWh)		region r' , time t (GWh)	

Table 1: Nomenclature.

Documentation

1. Overview

There are two base models:

- The 1_region model has one region in which supply must match demand.
- The 6_region model has six regions. Supply must match demand across the
 model as a whole, but electricity may be transmitted across the regions according to a transmission topology, taken from the IEEE 6-bus test system.

For each of the two base models, there are a number of customisable inputs/settings that change the model's behaviour.

- The run mode. Each model can be run in either plan or operate mode. In plan mode, generation and transmission capacities are determined by minimising the sum of installation and generation costs. The models are then generation & transmission expansion planning models. In operate mode, the installed capacities are user-defined, and only the generation and transmission levels are determined by minimising the generation cost subject to a fixed model configuration.
- Each technology's install and generation cost.
- The (demand, wind and solar) time series inputs.
- The baseload_integer constraint. If False, baseload may be built to any nonnegative capacity (i.e. a continuous variable). If True, baseload may be built in blocks of 3GW. This constraint applies only in plan mode.
- The baseload_ramping constraint. If False, baseload generation can change arbitrarily quickly between time steps. If True, baseload generation levels can ramp up or down at most 20% of its installed capacity in an hour.
- The allow_unmet constraint. If False, all demand must be met. If True, some unmet demand is allowed at high cost, if this leads to a lower total system cost. In operate mode, unmet demand is always allowed to keep solutions feasible, since the capacities are fixed.

	Installation cost	Generation cost	Carbon emissions		
Technology	(£m/GWyr)	(£m/GWh)	$(t CO_2/GWh)$		
Generation technologies					
Baseload	$C_b^{\rm gen} = 300$	$F_b^{\rm gen} = 0.005$	$e_b = 200$		
Peaking	$C_p^{\text{gen}} = 100$	$F_p^{\text{gen}} = 0.035$	$e_m = 400$		
Wind	$C_w^{\text{gen}} = 100$	$F_w^{\mathrm{gen}} = 0$	$e_w = 0$		
Solar	$C_s^{\text{gen}} = 30$	$F_s^{\text{gen}} = 0$	$e_s = 0$		
Unmet demand	$C_u^{\text{gen}} = 0$	$F_u^{\text{gen}} = 6$	$e_u = 0$		
Transmission technologies					
Regions 1 to 5	$C_{1,5}^{\mathrm{tr}} = 150$	-	-		
Other links	$C_{r,r'}^{\mathrm{tr}} = 100$	-	-		

Table 2: Costs and carbon emissions of generation and transmission technologies. Transmission costs consist only of installation costs. Installation costs are annualised so as to reflect cost per year of plant lifetime.

• The installed capacities of generation and technology technologies. These are model inputs only in operate mode, and are model outputs (hence not user-defined) in plan mode.

The install and generation costs are specified in models/{MODEL_NAME}/techs.yaml. The installed capacities are specified in models/{MODEL_NAME}/model.yaml. All other settings & inputs are specified when conducting model runs (see main.py).

2. Technologies

In each model, three generation technologies are allowed: baseload, peaking, wind and solar. Baseload and peaking are conventional technologies whose generation levels can be controlled. Wind and solar have no generation cost but generation levels that are capped by the time-varying wind and solar capacity factors respectively. Unmet demand is considered, for modelling purposes, a fourth technology with no install cost but a high generation cost. The default characteristics of the the generation technologies is provided in Table 2.

In the 6_region model, the costs of the same technologies in different regions (e.g. baseload in regions 1 and 3) are perturbed slightly to remove solution nonuniqueness between regions – so baseload in region 1 is (very slightly) different than baseload in region 3. Details can be found in models/6_region/techs.yaml.

3. Time series inputs

Time series inputs consist of hourly demand levels, wind capacity factors and solar capacity factor in different European countries over the period 1980-2017. Long-term anthropogenic demand trends such as GDP growth and efficiency improvements are removed so that the time series can be viewed as being drawn from the same underlying demand distribution. Details on the construction of the time series can be found in (Bloomfield et al, 2019).

4. 1-region model

The 1_region model considers a single node and a choice of the three generation technologies. It takes three input time series: hourly demand levels, wind capacity factors and solar capacity factor in the United Kingdom. In plan mode, the model leads to a generation expansion planning problem where the optimal generation capacities

and hourly generation levels for each technology are model outputs. This problem is either a continuous linear program or a mixed-integer linear program, depending on whether the baseload_integer constraint is activated.

4.1. Planning mode

Model inputs:

$$\{C_i^{\text{gen}}, F_i^{\text{gen}}, d_{1,t}, w_{1,t} : i \in \mathcal{I}; t = 1 \dots T\}.$$
 (1)

Model outputs:

$$\{\operatorname{cap}_{i,1}^{\operatorname{gen}}, \operatorname{gen}_{i,1,t}, : i \in \mathcal{I}; t = 1 \dots T\}.$$
 (2)

The model outputs are determined as the decision variables that solve the following optimisation problem:

$$\min \left[\frac{T}{8760} \left(\underbrace{\sum_{i \in \mathcal{I}} C_i^{\text{gen}} \text{cap}_{i,1}^{\text{gen}}}_{\text{installation cost,}} \right) + \underbrace{\sum_{i \in \mathcal{I}} \sum_{t=1}^{T} F_i^{\text{gen}} \text{gen}_{i,1,t}}_{\text{generation capacity}} \right]$$
(3)

subject to

$$\sum_{i \in \mathcal{I}} \operatorname{gen}_{i,1,t} = d_{1,t} \quad \forall t$$
 (4)

$$gen_{b,1,t} \le cap_{b,1}^{gen} \quad \forall t$$
 (5)

$$gen_{p,1,t} \le cap_{p,1}^{gen} \quad \forall t \tag{6}$$

$$gen_{w,1,t} \le cap_{w,1}^{gen} w_{1,t} \quad \forall t$$
 (7)

$$gen_{s,1,t} \le cap_{s,1}^{gen} s_{1,t} \quad \forall t$$
 (8)

$$\operatorname{cap}_{b,1}^{\operatorname{gen}} \in 3\mathbb{Z} \tag{9}$$

$$|\text{gen}_{b,1,t} - \text{gen}_{b,1,t+1}| \le 0.2 \text{cap}_{b,1}^{\text{gen}} \quad \forall t$$
 (10)

$$gen_{u,1,t} = 0 \quad \forall t \tag{11}$$

$$\operatorname{cap}_{i,1}^{\operatorname{gen}}, \operatorname{gen}_{i,1,t} \ge 0 \quad \forall i, t. \tag{12}$$

The $\frac{T}{8760}$ factor ensures the installation and generation costs are scaled correctly in model runs of different simulation lengths. (4) is the demand balance requirement. (5)-(8) ensure generation does not exceed installed capacity (for baseload and peaking) or installed capacity times the capacity factor (for wind and solar). (9) is the integer constraint (active only if baseload_integer=True) for baseload capacity, which may only be installed in units of 3GW. (10) is the ramping constraint (active only if baseload_ramping=True) for baseload generation, which can ramp up or down at maximally 20%/hr. (11) (active only if allow_unmet=False) removes the possibility of unmet demand. (12) enforces the nonnegativity of capacity and generation levels.

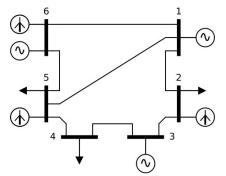
4.2. Operation mode

 $Model\ inputs:$

$$\{C_i^{\text{gen}}, F_i^{\text{gen}}, d_{1,t}, w_{1,t}, \text{ cap}_{i,1}^{\text{gen}}, : i \in \mathcal{I}; t = 1 \dots T\}.$$
 (13)

Model outputs:

$$\{ gen_{i,1,t}, : i \in \mathcal{I}; t = 1...T \}.$$
 (14)



Bus	Demand/candidate generation
1	baseload, peaking
2	demand, wind, solar (DE)
3	baseload, peaking
4	demand (FR)
5	demand, wind, solar (UK)
6	baseload, peaking, wind, solar (ES)

Figure 1: 6-bus model configuration. Demand must be met at buses 2, 5 and 6. Conventional generation (baseload or peaking) may be installed at buses 1, 3 and 6. Wind and solar generation may be installed at buses 2, 5 and 6. Buses 2, 4, 5 and 6 use (demand, wind or solar) time series data from Germany (DE), France (FR), the United Kingdom (UK) and Spain (ES) respectively.

The model outputs are determined as the decision variables that solve the following optimisation problem:

$$\min \sum_{i \in \mathcal{I}} \sum_{t=1}^{T} F_i^{\text{gen}} \text{gen}_{i,1,t}$$
(15)

subject to

$$\sum_{i \in \mathcal{I}} \operatorname{gen}_{i,1,t} = d_{1,t} \quad \forall t$$
 (16)

$$gen_{b,1,t} \le cap_{b,1}^{gen} \quad \forall t$$
 (17)

$$\operatorname{gen}_{p,1,t} \le \operatorname{cap}_{p,1}^{\operatorname{gen}} \quad \forall t \tag{18}$$

$$\operatorname{gen}_{w,1,t} \le \operatorname{cap}_{w,1}^{\operatorname{gen}} w_{1,t} \quad \forall t$$
 (19)

$$gen_{s,1,t} \le cap_{s,1}^{gen} s_{1,t} \quad \forall t$$
 (20)

$$|\text{gen}_{b,1,t} - \text{gen}_{b,1,t+1}| \le 0.2 \text{cap}_{b,1}^{\text{gen}} \quad \forall t$$
 (21)

$$gen_{u,1,t} = 0 \quad \forall t \tag{22}$$

$$gen_{i,1,t} \ge 0 \quad \forall i, t. \tag{23}$$

where each constraint has the same meaning as in the planning model.

5. 6-region model

The 6_region model is a more complicated multi-region model. The system's topology is based on the *IEEE 6-bus system*. The available technologies at each bus are based on a renewables-ready version of the 6-bus system introduced by Kamalinia & Shahidehpour (2010). Figure 1 provides a diagram of the model configuration.

The model takes 6 input time series: hourly demand levels and wind capacity factors in three European countries each. In plan mode, the model leads to a generation & transmission expansion planning problem where the optimal generation & transmission capacities and hourly generation & transmission levels for each technology are determined. This problem is either a continuous linear program or a mixed-integer linear program depending on whether the baseload_integer constraint is activated. In operate mode, the generation & transmission capacities are fixed and only the hourly generation & transmission levels are determined. The mathematical details for the model are provided below.

The 6_region model leads to solution nonuniqueness. For example, excess demand in region 2 has no preference between being met from regions 1 or 3. For this reason, the model should only be used for model-wide summary statistics (e.g. the total baseload capacity). If outputs at regional level are desired, regions must de differentiated by having different technologies in each (e.g. by changing the technology prices at regional level).

5.1. Planning mode

Model inputs:

$$\{C_i^{\text{gen}}, F_i^{\text{gen}}, d_{r,t}, w_{r,t} : i \in \mathcal{I}; r \in \mathcal{R}; t = 1 \dots T\}.$$
 (24)

Model outputs:

$$\{\operatorname{cap}_{i,r}^{\operatorname{gen}}, \operatorname{cap}_{r,r'}^{\operatorname{tr}}, \operatorname{gen}_{i,r,t}, \operatorname{tr}_{r,r',t} : i \in \mathcal{I}; r, r' \in \mathcal{R}; t = 1 \dots T\}.$$
 (25)

The model outputs are determined as the decision variables that solve the following optimisation problem:

$$\min \sum_{r \in \mathcal{R}} \left[\frac{T}{8760} \left(\sum_{i \in \mathcal{I}} C_i^{\text{gen}} \operatorname{cap}_{i,r}^{\text{gen}} + \frac{1}{2} \sum_{r' \in \mathcal{R}} C_{r,r'}^{\text{tr}} \operatorname{cap}_{r,r'}^{\text{tr}} \right) + \sum_{i \in \mathcal{I}} \sum_{t=1}^{T} F_i^{\text{gen}} \operatorname{gen}_{i,r,t} \right]$$
(26)
$$\underset{\text{generation capacity}}{\operatorname{installation cost}} \underbrace{ \underset{\text{installation cost,}}{\operatorname{transmission capacity}}$$

subject to

$$\operatorname{cap}_{b,r}^{\text{gen}}\big|_{r\neq 1,3,6} = \operatorname{cap}_{p,r}^{\text{gen}}\big|_{r\neq 1,3,6} = \operatorname{cap}_{w,r}^{\text{gen}}\big|_{r\neq 2,5,6} = 0$$
(27)

$$\operatorname{cap}_{r,r'}^{\operatorname{tr}}\big|_{\{r,r'\}\neq\{1,2\},\{1,5\},\{1,6\},\{2,3\},\{3,4\},\{4,5\},\{5,6\}} = 0 \tag{28}$$

$$\sum_{i \in \mathcal{I}} \operatorname{gen}_{i,r,t} + \sum_{r'=1}^{6} \operatorname{tr}_{r',r,t} = d_{r,t} \quad \forall \, r,t$$
 (29)

$$\operatorname{tr}_{r,r',t} + \operatorname{tr}_{r,'r,t} = 0 \quad \forall \, r, r', t \tag{30}$$

$$\operatorname{gen}_{b,r,t} \le \operatorname{cap}_{b,r}^{\operatorname{gen}} \quad \forall \, r,t$$
 (31)

$$\operatorname{gen}_{p,r,t} \le \operatorname{cap}_{p,r}^{\operatorname{gen}} \quad \forall \, r,t$$
 (32)

$$gen_{w,r,t} \le cap_{w,r}^{gen} w_{r,t} \quad \forall \, r,t \tag{33}$$

$$|\operatorname{tr}_{r,r',t}| \le \operatorname{cap}_{r,r'}^{\operatorname{tr}} \quad \forall \, r, r', t \tag{34}$$

$$\operatorname{cap}_{h\,r}^{\mathrm{gen}} \in 3\mathbb{Z} \quad \forall \, r \tag{35}$$

$$|\operatorname{gen}_{b,r,t} - \operatorname{gen}_{b,r,t+1}| \le 0.2 \operatorname{cap}_{b,r}^{\operatorname{gen}} \quad \forall \, r,t$$
(36)

$$gen_{u,r,t} = 0 \quad \forall \, r,t \tag{37}$$

$$\operatorname{cap}_{i,r}^{\operatorname{gen}}, \operatorname{cap}_{r,r'}^{\operatorname{tr}}, \operatorname{gen}_{i,r,t} \ge 0 \quad \forall i, r, t.$$
 (38)

The $\frac{T}{8760}$ factor ensures the installation and generation costs are scaled correctly in model runs of different simulation lengths. (27)-(28) stipulate the locations of generation technologies and the model's transmission topology. (29) and (30) are the demand and power flow balance requirements. (31)-(33) ensure generation does not exceed installed capacity (for baseload and peaking) or installed capacity times the wind capacity factor (for wind). (34) ensures transmission does not exceed transmission capacity. (35) is the integer constraint (active only if baseload_integer=True) for baseload capacity, which may only be installed in units of 3GW. (36) is the ramping constraint (active only if baseload_ramping=True) for baseload generation, which can ramp up or down at maximally 20%/hr. (11) (active only if allow_unmet=False) removes the possibility of unmet demand. (38) enforces the nonnegativity of capacity and generation levels.

5.2. Operation mode

Model inputs:

$$\{C_i^{\text{gen}}, F_i^{\text{gen}}, d_{r,t}, w_{r,t}, \text{cap}_{i,r}^{\text{gen}}, \text{cap}_{r,r'}^{\text{tr}}, : i \in \mathcal{I}; r, r' \in \mathcal{R}; t = 1 \dots T\}.$$
 (39)

Model outputs:

$$\{\operatorname{gen}_{i,r,t}, \operatorname{tr}_{r,r',t} : i \in \mathcal{I}; r, r' \in \mathcal{R}; t = 1 \dots T\}.$$

$$(40)$$

The model outputs are determined as the decision variables that solve the following optimisation problem:

$$\min \sum_{r \in \mathcal{R}} \sum_{i \in \mathcal{I}} \sum_{t=1}^{T} F_i^{\text{gen}} \text{gen}_{i,r,t}$$
generation cost
$$(41)$$

subject to

$$\sum_{i \in \mathcal{I}} \operatorname{gen}_{i,r,t} + \sum_{r'=1}^{6} \operatorname{tr}_{r',r,t} = d_{r,t} \quad \forall \, r,t$$
(42)

$$\operatorname{tr}_{r,r',t} + \operatorname{tr}_{r,r,t} = 0 \quad \forall r, r', t$$

$$\operatorname{gen}_{b,r,t} \leq \operatorname{cap}_{b,r}^{\operatorname{gen}} \quad \forall r, t$$

$$(43)$$

$$gen_{b,r,t} \le cap_{b,r}^{gen} \quad \forall \, r,t \tag{44}$$

$$\operatorname{gen}_{p,r,t} \le \operatorname{cap}_{p,r}^{\operatorname{gen}} \quad \forall \, r,t$$
 (45)

$$gen_{w,r,t} \le cap_{w,r}^{gen} w_{r,t} \quad \forall \, r,t \tag{46}$$

$$|\operatorname{tr}_{r,r',t}| \le \operatorname{cap}_{r,r'}^{\operatorname{tr}} \quad \forall \, r,r',t$$
 (47)

$$|\operatorname{gen}_{b,r,t} - \operatorname{gen}_{b,r,t+1}| \le 0.2 \operatorname{cap}_{b,r}^{\operatorname{gen}} \quad \forall \, r,t$$

$$\tag{48}$$

$$gen_{u,r,t} = 0 \quad \forall \, r, t \tag{49}$$

$$gen_{i,r,t} \ge 0 \quad \forall i, r, t. \tag{50}$$

where each constraint has the same meaning as for the planning model.

6. References

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S Kamalinia, M Shahidehpour (2010). Generation expansion planning in windthermal power systems. IET Generation, Transmission & Distribution, 4-8, 940-951. doi:10.1049/iet-gtd.2009.0695.