

# How to Form Bags in Batch Steganography

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Eli Dworetzky, Jessica Fridrich

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# Batch steganography

Alice / steganographer

- Spreads payload across multiple covers (or **bag** of images)
- Useful when payload cannot fit within one image

Warden / Eve

- Inspects the **entire** bag (pooled steganalysis)
- Applies a single-image detector (SID) to all images
  - E.g. SRNet, rich models, etc.
- “Pools” the SID outputs to decide if the **bag** is cover or stego

# Practical question: how to form the bag?

Alice has a **fixed payload** to communicate

- ① What kind of images should she use?
- ② How many images should she use?

# Alice uses source biasing

## Source biasing

- Alice samples covers from the cover source with a bias towards harder-to-steganalyze images
- Alice gains security when biasing optimally
- Warden tests for a deviation in cover source by considering the **joint** statistical impact of steganography and biasing

E. Dworetzky, E. Kaziakhmedov, J. Fridrich, “Improving Steganographic Security with Source Biasing”, 12th IH&MMSec. Workshop, Vigo, Spain, June 24-26, 2024.

- We will utilize the model proposed in this prior work
- Prior work studied **fixed rate** – we now have a **fixed payload**

## Alice's goal

Given a fixed payload, Alice wants to choose bag size  $n$  so that

$$P_D \leq \tilde{P}_D \text{ and } n \leq n_{\max}$$

- $\tilde{P}_D$  — maximal tolerable detectability by Warden's (pooled) detector
- $n_{\max}$  — bandwidth limit
- Alice's optimal source biasing strength is a function of  $n$

# Outline

- Formal setup of batch steganography / pooled steganalysis
- High level overview of the model
- Two benefits of source biasing: **Bias gain** and **bandwidth savings**
- Confirmation by experiments on ALASKA II dataset
  - Bias gain and bandwidth savings observed in practice

# Batch stego setup

## Alice

- Payload is  $\alpha C$  bits,  $\alpha > 0$ , where  $C$  is capacity of each cover
  - Ternary embedding:  $C = \log_2 3 \times \text{number of pixels}$
- $\lceil \alpha \rceil$  is the smallest number of images needed to fit the payload
- Independently samples a bag of  $n$  covers of fixed size from  $\mathcal{X}$ ,  $\mathbf{X} = (X_1, \dots, X_n)$ ,  $n \geq \alpha$
- Embeds  $\alpha_i C$  bits in  $X_i$ ,  $\sum_{i=1}^n \alpha_i = \alpha$ ,  $0 \leq \alpha_i \leq 1$
- Her spreading strategy determines the  $\alpha_i$

## Warden

- Has a SID  $d : \mathcal{X} \rightarrow \mathbb{R}$  and a pooler  $\pi : \mathbb{R}^n \rightarrow \mathbb{R}$
- Given a bag of  $n$  images  $\mathbf{Y} = (Y_1, \dots, Y_n)$ , Warden's detection statistic is  $\pi(d(Y_1), \dots, d(Y_n))$

## Detector-centric approach

We model the effect of embedding and model the source itself through soft outputs of the SID  $d$

- Permits formulating steganalysis and source biasing **jointly** through a single hypothesis test
  - Closed-form ROC of Warden's optimal pooler (LRT)
- Model parameters can be estimated in practice
- We observe a close match between model and experiments on real datasets



# Source model and biasing

Alice's cover source  $\mathcal{X}$  has only two types of images: Hard & Easy

When sampling from  $\mathcal{X}$  (no bias), for each  $i$

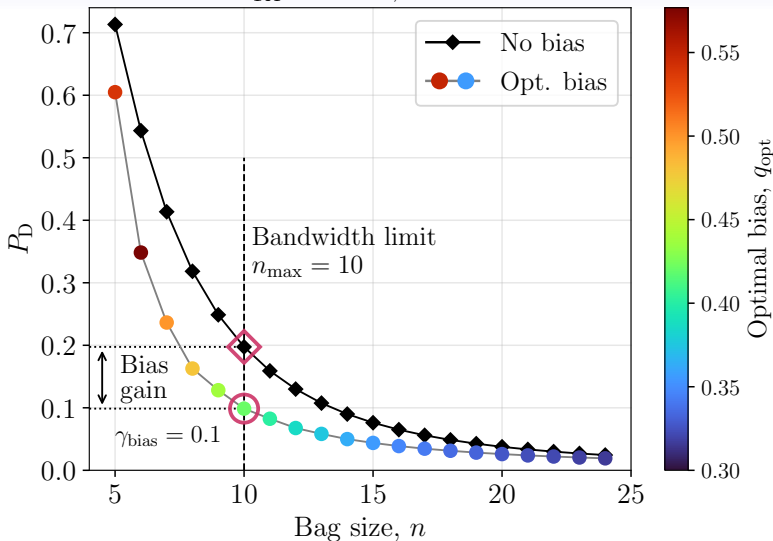
- $X_i$  is hard with probability  $p$
- $X_i$  is easy with probability  $1 - p$

Alice's bias

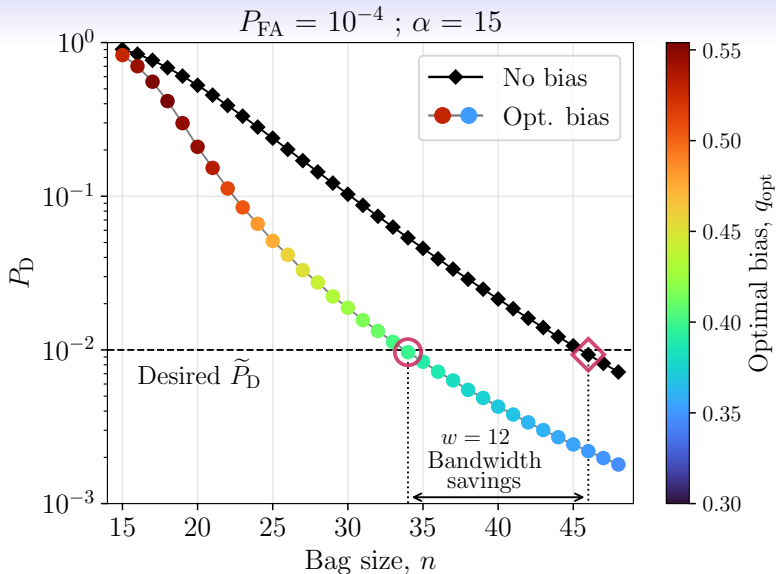
- Selects hard images with probability  $q \geq p$

## Insight from the model: bias gain

$$P_{FA} = 10^{-2} ; \alpha = 5$$



## Insight: bandwidth savings



## Biasing and spreading in practice

Given bag  $(X_1, \dots, X_n)$

- Alice estimates the difficulty of each image by seeing how her own detector  $d^{(A)}$  reacts to embedding

Biasing:

- Done by inverse transform sampling modified with a parametric model with parameter  $q$
- $q = 1$  corresponds to unbiased sampling,  $q > 1$  biased

Greedy spreader:

- Orders images by difficulty
- Starting with the most difficult, she embeds fully with HILL one by one
- $\alpha$  images will be embedded,  $n - \alpha$  will be empty

# Experiments on ALASKA II

ALASKA II (75k grayscale images) divided into four subsets

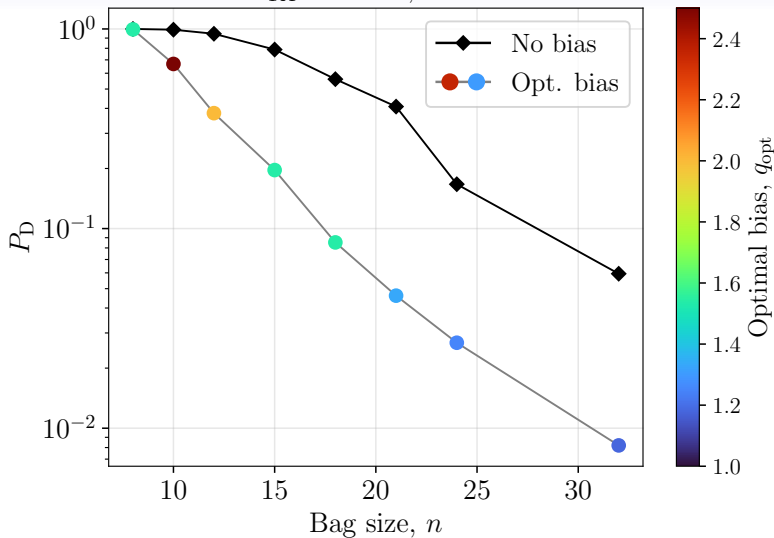
- 23k used for training Alice's detector
- 23k used for training Warden's detector and 10k for pooler
- 19k used for evaluation
- Both detectors SRNets, JIN pre-trained, refined on HILL with uniform payloads on  $[0, \log_2 3]$

Warden's Pooler

- Trained as random forest on  $2n + 2$  dim. feature extracted from bag  $(X_1, \dots, X_n)$

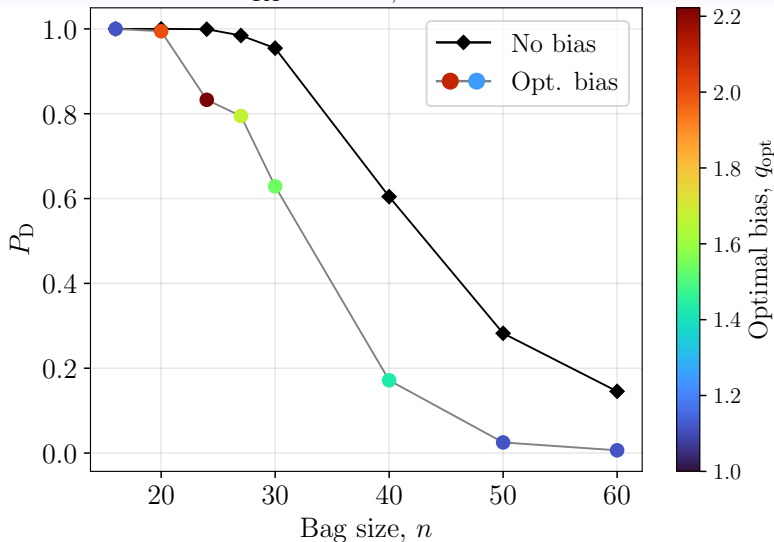
# Experiments on ALASKA II

$$P_{FA} = 10^{-3} ; \alpha = 8$$



## Experiments on ALASKA II

$$P_{FA} = 10^{-3}; \alpha = 16$$



# Conclusions

Selecting covers with an optimal bias, Alice benefits in terms of

- Lower detection probability  $P_D$  at the same bag size  $n$
- Smaller bag size  $n$  at the same  $P_D$

What kind of images should Alice use?

- Difficult cover images...but not a suspiciously high ratio of them

How many images should Alice use? Depending on her preferences

- As many as she can within her bandwidth constraint
- Just enough to achieve a desired detectability if bandwidth is costly
- ...or somewhere in between