

Can Selective Predation Slow the Spread of CWD?

Modeling disease, predation, dispersal, and population dynamics
in Wisconsin

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Acknowledgement

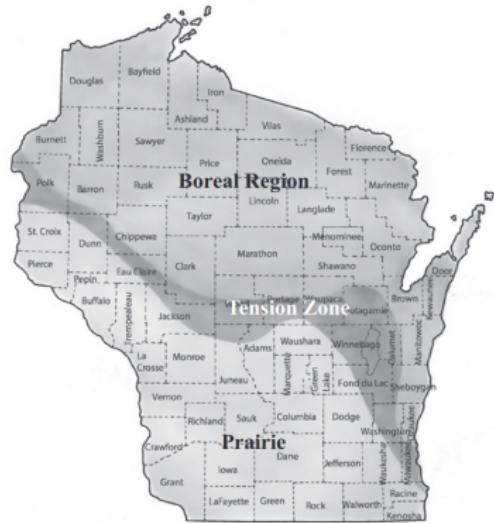
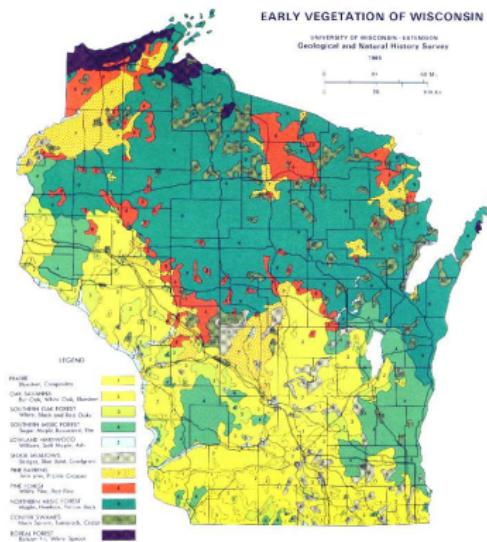


Prof. Tim Van Deelen

The setting: Wisconsin

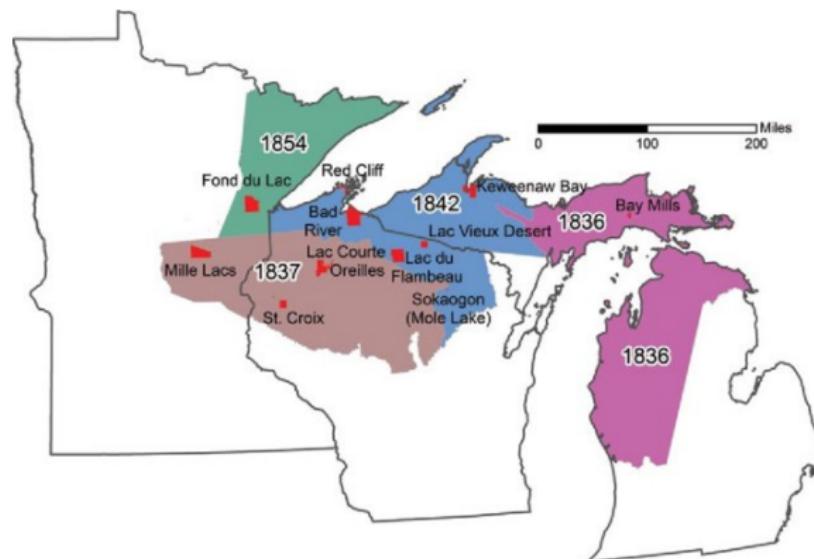


The setting: Wisconsin



- **Southwest:** Mainly agricultural / ex-prairie and oak savanna.
- **Northeast:** Conifer-hardwood forest / bogs / also agriculture

The setting: Wisconsin



Wildlife management and fishing rights largely retained by Ojibwe tribes in the North.

Three characters

- ① White-tailed deer
- ② Chronic wasting disease
- ③ Wolves

White-tailed deer in Wisconsin

Odocoileus virginianus

- (over)-abundant: 1.9-2.1 million ind.
- major ecological impacts
- ≈ 350,000 hunted annually (and falling)
- \$1.4 billion dollars / year to economy
- a big chunk of which funds research / mitigation of those ecological impacts

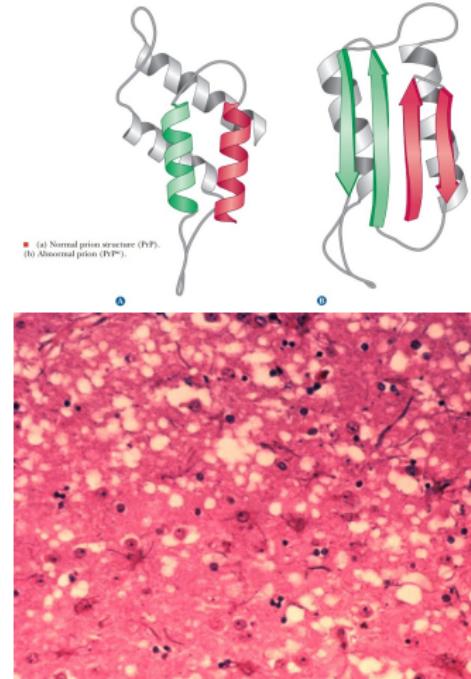


Todd Hubler - *The Isthmus*

Chronic Wasting Disease

Transmissible spongiform encephalopathy

- Turns brains into sponges
- Invariably fatal
- Caused by **prion**
 - misfolded protein found in nervous system
- Only affects cervids
 - only TSE in *wildlife*
- Major focus of concern / research among agencies



Chronic Wasting Disease

Clinical Signs

“Zombie Disease”

- Emaciation
- Lack of coordination
- Drooping head/ears
- Excessive drooling
- Excessive drinking
- Excessive urination



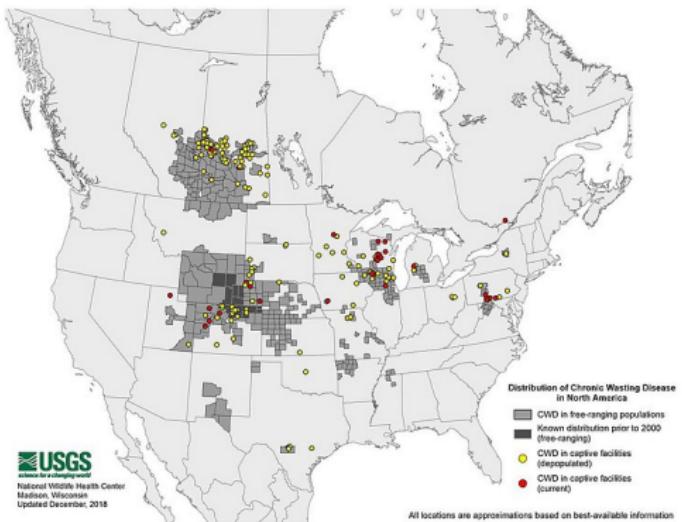
Incubation: (asymptomatic) period lasts on average 18 months

Transmission: urine, feces, blood. Direct contact. Long-term environmental persistence (even uptake by plants).

Chronic Wasting Disease

Global Expansion

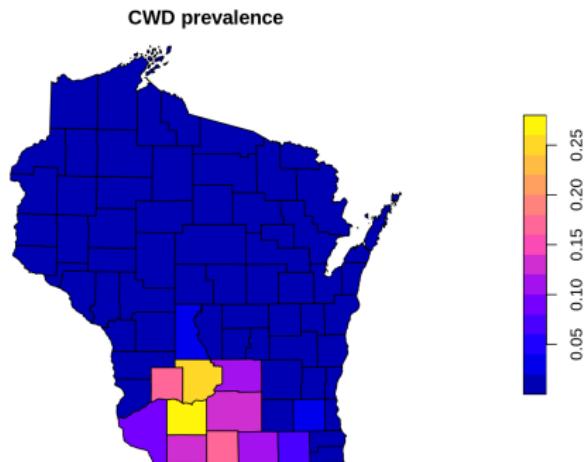
- 1967 - First detected (mule deer) in research facility Colorado.
- 1981 - First wild animal (elk) detected in Colorado
- 2002 - Found in wild WTD in Wisconsin
- 2011 - Found in wild WTD in Maryland
- 2017 - Appeared in 3 reindeer in Norway (!) - entire 2000 animal herd summarily executed



USGS
U.S. Geological Survey
National Wildlife Health Center
Madison, Wisconsin
Updated December, 2018

Chronic Wasting Disease: In Wisconsin

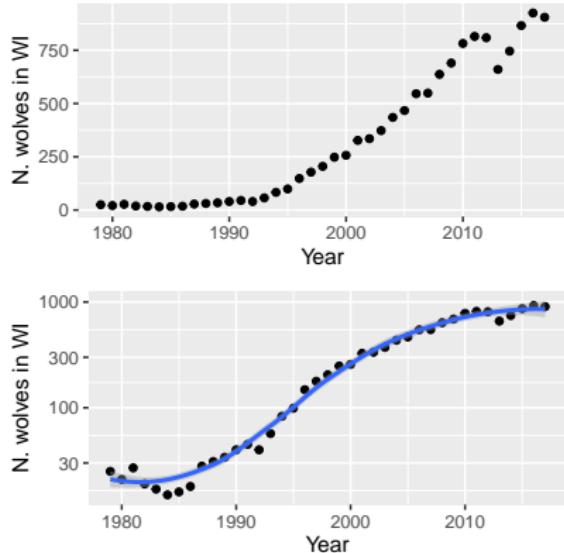
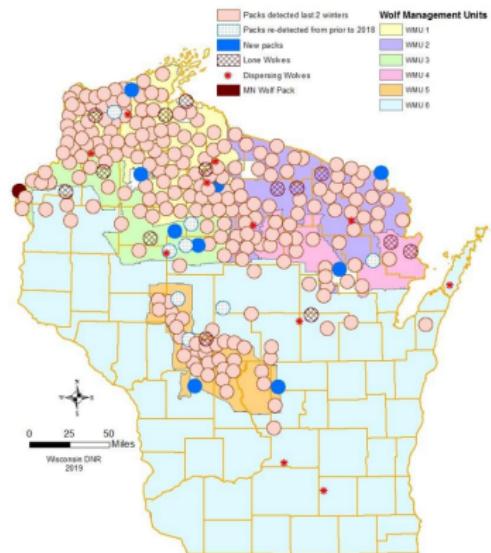
Concentrated in southern counties, up to 25% prevalence.



Good data: In affected counties, all hunted carcasses need to be tested. In non-affected counties, a sample of carcasses is tested.

Wolves in Wisconsin

Exterminated early 1900's. Re-colonized from Minnesota post-ESA.



Currently, approx. 1000 ind. mainly in North. Expansion slowing. **Good Data.**

The question

Wolves selectively predate on old, young, weak or **infirm(?)** individuals . . . though there is no direct evidence w.r.t. CWD (or - actually - other diseases).

Given that CWD is concentrated in the SW - and expanding - and wolves are concentrated in NE - and maybe still expanding? - What happens when they meet?

Specifically, how do wolf presence and selective predation influence:

- **CWD prevalence**
- **CWD spread**
- **Deer abundance**

Approaches to look at this question

Lots of **Mathematical Modeling!!** Mainly, continuous-time, non-spatial SEIR-type ODE's.

Journal of Wildlife Diseases, 47(1), 2011, pp. 79-93
© Wildlife Disease Association 2011

THE ROLE OF PREDATION IN DISEASE CONTROL: A COMPARISON OF SELECTIVE AND NONSELECTIVE REMOVAL ON PRION DISEASE DYNAMICS IN DEER

Margaret A. Wild,^{1,5} N. Thompson Hobbs,² Mark S. Graham,^{1,4} and Michael W. Miller³

$$\frac{dS}{dt} = a(S+I) \left(1 - \frac{S+I}{K_a} \right) - S(\gamma E + m) \\ - (1-p)\delta(S+I),$$

$$\frac{dI}{dt} = \gamma SE - I(m+\mu) - p(1-c)\delta(S+I),$$

$$\frac{dE}{dt} = \varepsilon I - \tau E,$$

Very influential, but no data (and no spatial structure)

Wolves contribute to disease control in a multi-host system

E. Tanner^①, A. White¹, P. Acevedo^②, A. Balseiro^{③,4}, J. Marcos⁵ & C. Gortázar²

$$\frac{dP_1}{dt} = \beta_{12}P_2\frac{G}{N} + \omega\beta_{13}P_3F - mP_1 - d_pP_1 - \beta_{13}P_3\frac{G}{N} - \omega\beta_{12}P_2F - \alpha_pP_3W \quad (1a)$$

$$\frac{dP_2}{dt} = \beta_{12}P_1\frac{G}{N} + \omega\beta_{23}P_3F - mP_2 - d_pP_2 - \beta_{23}P_3\frac{G}{N} - \omega\beta_{12}P_1F - \alpha_pP_2W \quad (1b)$$

$$\frac{dP_3}{dt} = \beta_{23}P_2\frac{G}{N} + \omega\beta_{13}P_1F - mP_3 - \alpha_E P_3 - d_pP_3 - \alpha_W P_3W \quad (1c)$$

$$\frac{dY_1}{dt} = mP_1 - mY_1 - d_pY_1 - \beta_{12}Y_2\frac{G}{N} - \omega\beta_{13}Y_3F - cT_1 - \alpha_{14}Y_4W \quad (1d)$$

$$\frac{dY_2}{dt} = \beta_{12}Y_1\frac{G}{N} + \omega\beta_{23}Y_3F + mP_2 - mY_2 - d_pY_2 - \beta_{23}Y_3\frac{G}{N} - \omega\beta_{12}Y_1F - cT_2 - \alpha_{14}Y_4W \quad (1e)$$

$$\frac{dY_3}{dt} = \beta_{23}Y_2\frac{G}{N} + \omega\beta_{13}Y_1F + mP_3 - mY_3 - d_pY_3 - \beta_{12}Y_1\frac{G}{N} - \omega\beta_{23}Y_2F - cT_3 - \alpha_{14}Y_4W \quad (1f)$$

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$$\frac{dA_2}{dt} = \beta_{12}A_1\frac{G}{N} + \omega\beta_{23}A_3F + mY_2 - d_pA_2 - \beta_{23}A_3\frac{G}{N} - \omega\beta_{12}A_1F - cA_2 - \alpha_{14}A_4W \quad (1h)$$

$$\frac{dA_3}{dt} = \beta_{23}A_2\frac{G}{N} + \omega\beta_{13}A_1F + mY_3 - d_pA_3 - \beta_{12}A_1\frac{G}{N} - \omega\beta_{23}A_2F - cA_3 - \alpha_{14}A_4W \quad (1i)$$

$$W = W(t) \quad (1j)$$

Lots of compartments - and some data (but no spatial structure)

Modeling goals

- Capturing dynamics of:
 - disease,
 - predation,
 - population
 - dispersal
- Biologically meaningful parameters
 - independently estimated / estimable?
- Provide spatially and temporally explicit predictions
- Balances realism with tractability

Basic model structure:

Discrete time / discrete space

- **Annual** - matches data collection and deer biology (birth / seasonal mortality / dispersal?)
- **County-level metapopulation** - matches data reporting and collection

Two classes: Susceptible and Infected

$$S_{i,t+1} = S_{i,t} - \text{infected} + \text{recruited} - \text{died} + \text{immigrated} - \text{emigrated}$$
$$I_{i,t+1} = I_{i,t} + \text{infected} - \text{died} + \text{immigrated} - \text{emigrated}$$

Complete model

	Susceptible ($S_{i,t+1}$)	Infected ($I_{i,t+1}$)
disease	$-\gamma \frac{S_{i,t} I_{i,t}}{\text{area}}$	$\gamma \frac{S_{i,t} I_{i,t}}{\text{area}}$
predation	$-\left(\frac{S_{i,t}}{S_{i,t} + I_{i,t}}\right) \left(\frac{1}{1+\alpha}\right) W_{max}$	$-\left(\frac{I_{i,t}}{S_{i,t} + I_{i,t}}\right) \left(\frac{\alpha}{1+\alpha}\right) W_{max}$
other mortality	$-\mu_s S_{i,t}$	$-\mu_I I_{i,t}$
recruitment	$\rho S_{i,t} (1 - S_{i,t}/K_i)$	
immigration	$\sum_j M_{S,ij}$	$\sum_j M_{I,ij}$
emigration	$-\sum_j E_{S,ji}$	$-\sum_j E_{I,ji}$



Recruitment

Approximate number of new (non-infected) individuals entering population annually:

$$\rho S_{i,t} (1 - S_{i,t}/K_i)$$

Assumptions:

- ① Logistic, density dependent growth with carrying capacity: K
- ② Intrinsic adult recruitment rate, ρ , uniform across range

Mortality

Non-Wolf:

Annual mortality rate: μ_S and μ_I :

- Equal (!?)
- Constant across range (?)

Mortality

Wolf:

Assume: **Wolves gonna kill what wolves gonna kill** - (almost entirely deer).

- e.g. 10 wolves, each kills 20 deer / year = 200 deer/year/county killed
- Apportioning of S and I killed is proportional to the *availability* ($\frac{I}{S+I}$) and the *preference* ($\frac{\alpha}{1+\alpha}$).

$$\bullet P(I \text{ killed}) \propto P(I) \times P(\text{killed} | I) = \left(\frac{I}{S+I} \right) \left(\frac{\alpha}{1+\alpha} \right) N_w K_{\text{rate}}$$

$$\bullet P(S \text{ killed}) \propto P(S) \times P(\text{killed} | S) = \left(\frac{S}{S+I} \right) \left(\frac{1}{1+\alpha} \right) N_w K_{\text{rate}}$$

where α is the odds of selecting infected over non-infected deer,
i.e. the Predation Selection Coefficient (presumably > 1).

This is the key, unobservable parameter of interest!

Disease dynamics

Number of infected . . .

(by county by year)

$$-\gamma \frac{S \times I}{\text{area}}$$

- γ is infection rate per encounter
- Total number of infections is higher if areas are smaller (densities are higher).
- Lots of mechanism and structure swept under rug here!

Dispersal

Necessary for disease to spread! (or not spread)

Immigration

$$M_i = \kappa_m \sum_j S_j \exp\left(-\frac{d_{ij}}{\lambda}\right)^\beta$$

Emigration

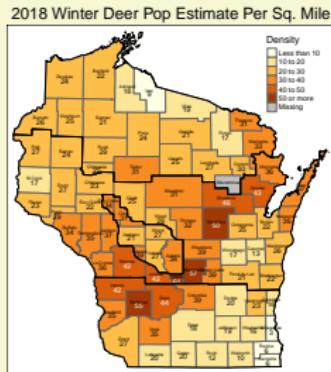
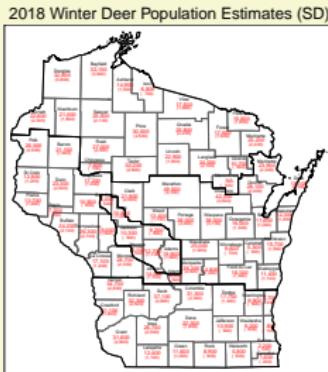
$$E_j = \kappa_e S_i \sum_i \exp\left(-\frac{d_{ij}}{\lambda}\right)^\beta$$

- **Exponential** ($\beta = 1$) or **Gaussian** ($\beta = 2$) dispersal kernel with mean λ
- κ - normalization, so that probability of emigrating from site j sums to 1
- Assumes homogenous dispersal in all directions, dependent only on distance.
- *Estimable (and refinable) from movement data!?*

Data

Deer Abundance

Wisconsin DNR winter population survey:
<https://dnr.wi.gov/topic/hunt/maps.html>



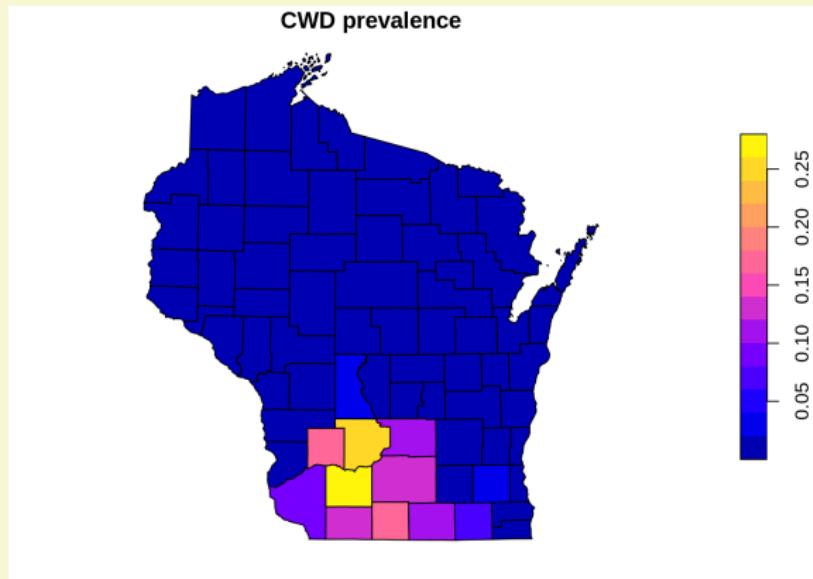
Fall population estimates - total harvest, by county.

Working assumption: Carrying Capacity $K_i = 2N_i$.

Data

CWD prevalence

Wisconsin DNR CWD monitoring efforts (by county)

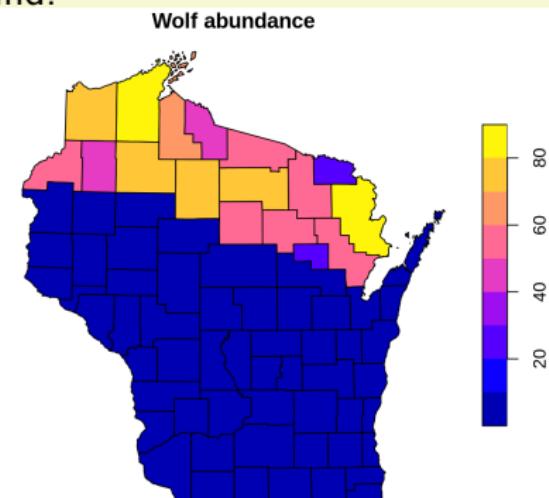
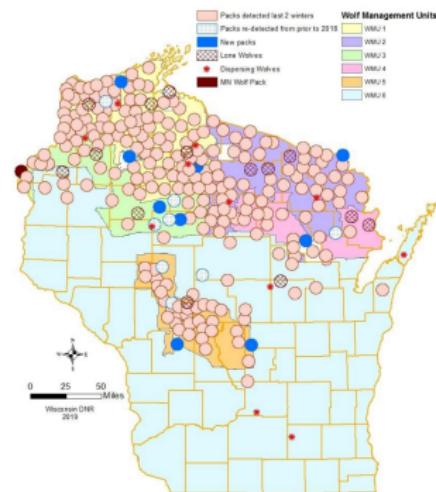


<https://dnr.wi.gov/wmcwd/Summary/YearCounty/2019>

Data

Wolves

Latest estimate from DNR: 950 ind.



County data not readily available ... so I allocated 1000 wolves across the counties north of this line.

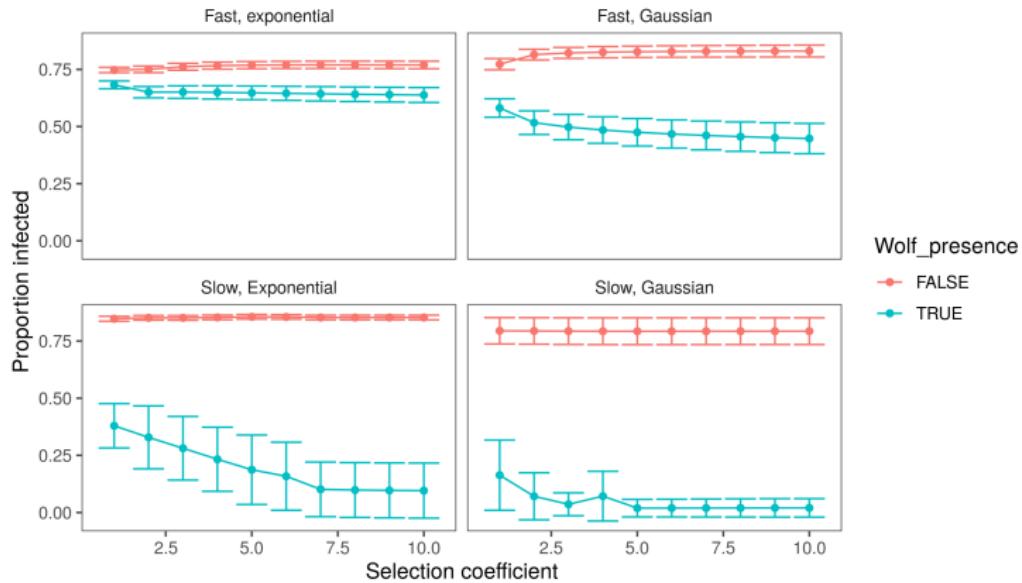
Model

Shiny App.

A brand new skill! Facilitates exploring parameters and visualizing results.

(enjoy demo)

A Result: Selective Predation Decreases CWD Prevalence!



In ALL parameterizations, wolves depress CWD. Note - dispersal scale (10 and 80 km) AND shape both important.

`rho = 0.5, gamma = .02, mu_S = 0.06, mu_I = 0.06, W_max = 60,
lambda = 10 or 80`

Next steps

Model structure

- Add **Male / Female** sex classes!
- Separate **Infected / Asymptomatic** from **Infected / Symptomatic**
- Assess assumptions: Density dependence? | Disease transmission?

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Data

- Obtain better **wolf distribution** and **predation** data
- Use **Harvest** for mortality!
- Use **GPS data** for dispersal portion
- Fit to historical data!?
 - Infer γ by matching to observed CWD spread?

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Larger strategy

- Thoroughly analyze / explore parameter space
- Find PhD student to do the work!?
- Get funding!

Thanks!