

3 Build an interpreter

The following grammar in the BackusNaur form(BNF) describes a Turing Machine and its input tape. It is stored in a txt file that you can download from bCourses. The Input $\langle TM \rangle$ is composed by a $\langle machine \rangle$ and an $\langle input_list \rangle$. The $\langle machine \rangle$ may expand into a

$\langle initial_state \rangle$, a $\langle final_state_list \rangle$ and a $\langle transition_list \rangle$. The $\langle transition_list \rangle$ may contain a list of $\langle transition \rangle$ s. The $\langle transition \rangle$ consists of a current state, an input, an output, a movement and a next state. The $\langle input_list \rangle$ contains all of inputs.

```
<TM>:='{ <machine> },{' <input_list> }'  
<machine> := '{<initial_state> },{'<final_state_list> },{'<transition_list> }'  
<initial_state>:= 'q0'  
<final_state_list> := <final_state> ',' <final_state_list> | <final_state>  
<final_state> := identifier  
<transition_list>:= <transition> ',' <transition_list> | <transition>  
<transition> := '{ <state> ',' <input> ',' <output> ',' <move> ',' <state> }'  
<state> := identifier  
<output> := identifier  
<move> := 'R'|'L'
```

Write a program in your computer to read the input($\langle TM \rangle$) as above and come up with your output.

Here are examples for you to test your code. Example 1 is a unary-add-one TM with a input tape bb111bb. It is also stored in the txt file that you can download from bCourses.

```
{{q0},{qf},{q0,b,b,R,q0},{q0,1,1,R,q1},{q1,1,1,R,q1},{q1,b,1,R,qf}},{b,b,1,1,1,b,b}
```

Your program should read the txt file, execute the TM and output the following string:

```
{b,b,1,1,1,1,b},{qf}
```

Here is example 2 for you to test your code. It is a unary-minus-one TM with a input tape bb111bb.

```
{{q0},{qf},{q0,b,b,R,q0},{q0,1,1,R,q1},{q1,1,1,R,q1},{q1,b,b,L,q2},{q2,1,b,R,qf}},{b,b,1,1,1,b,b}
```

Your program should read the txt file, execute the TM and output the following string:

```
{b,b,1,1,b,b,b},{qf}
```

Here is example 3 for you to test your code. You take a binary number bb111bb as input and add 1.

```
{{q0},{qf},{q0,b,b,R,q0},{q0,1,1,R,q1},{q0,0,0,R,q1},{q1,1,1,R,q1},{q1,0,0,R,q1},{q1,b,b,L,q2},{q2,1,0,L,q2},{q2,0,1,R,qf},{q2,b,1,R,qf}},{b,b,1,1,1,b,b}
```

Your program should read the txt file, execute the TM and output the following string:

```
{b,1,0,0,0,b,b},{qf}
```

The turing machine accepts the number which only contains 1, and any number contains 0 will be considered unacceptable. If the number only contains 1, the final state will be qa, otherwise it will be qu.

$\{\{q_0\},\{q_a, q_u\},\{\{q_0, b, b, R, q_0\},\{q_0, 1, 1, R, q_1\},\{q_0, 0, 0, R, q_u\},\{q_1, 1, 1, R, q_1\},\{q_1, b, b, L, q_a\},\{q_1, 0, 0, R, q_u\}\},\{b, b, 1, 1, 1, b, b\}$

Your program should read the txt file, execute the TM and output the following string:

$\{b, b, 1, 1, 1, b, b\},\{q_a\}$