Research:

What about interpolation of feature points (x coord uniform) using catmullromspline (without 2D interpolation)? Try to spin coordinate start around itself (e.g. x/y2=x/y1\*sin?/cos?(a)) to align start end and points to be parallel to x axis and then do CatmullRomCurve. Compare the results