

Discussion 6 Problems (Not Graded)

Read SmallC Formal Operational Semantics:

<https://github.com/anwarmamat/cm330spring18-public/blob/master/p3b/semantics.pdf>

Use the rules to show:

$$\frac{\bullet; 1 \rightarrow 1 \quad \bullet; 2 \rightarrow 2 \quad 3 \text{ is } 1 + 2}{\bullet; 1 + 2 \rightarrow 3} \quad \frac{\bullet; 3 \rightarrow 3 \quad 9 \text{ is } 3 * 3}{\bullet; (1 + 2) * 3 \rightarrow 9}$$

$$\frac{}{\bullet[x \mapsto \text{true}](x) = \text{true}}$$
$$\frac{}{\bullet[x \mapsto \text{true}]; x \rightarrow \text{true}} \quad \frac{}{\bullet[x \mapsto \text{true}]; \text{true} \rightarrow \text{true}}$$
$$\frac{}{\bullet[x \mapsto \text{true}]; x == \text{true} \rightarrow \text{true}} \quad \frac{}{\text{false is } \neg \text{true}}$$
$$\frac{}{\bullet[x \mapsto \text{true}]; !(x == \text{true}) \rightarrow \text{false}}$$

$$\frac{}{(x) \text{ not defined}} \quad \frac{}{\bullet[x \mapsto 0](x) = 0} \quad \frac{}{\bullet[x \mapsto 0]; 2 \rightarrow 2}$$
$$\frac{}{\text{int } x \rightarrow \bullet[x \mapsto 0]} \quad \frac{}{\bullet[x \mapsto 0]; x = 2 \rightarrow \bullet[x \mapsto 2]}$$
$$\bullet; \text{int } x; x = 2 \rightarrow \bullet[x \mapsto 2]$$

(1)
$$\frac{}{\bullet[i \mapsto 0]; i < 1 \rightarrow \text{true}}$$

(2)
$$\frac{}{\bullet[i \mapsto 0]; i = i + 1 \rightarrow \bullet[i \mapsto 1]}$$

(3)
$$\frac{}{\bullet[i \mapsto 1]; \text{while } (i < 1) (i = i + 1) \rightarrow \bullet[i \mapsto 1]}$$
$$\bullet[i \mapsto 0]; \text{while } (i < 1) (i = i + 1) \rightarrow \bullet[i \mapsto 1]$$

$$\frac{}{\bullet[i \mapsto 0](i) = 0}$$
$$\frac{}{\bullet[i \mapsto 0]; i \rightarrow 0} \quad \frac{}{\bullet[i \mapsto 0]; 1 \rightarrow 1} \quad \frac{}{\text{true is } 0 < 1}$$

(1)
$$\bullet[i \mapsto 0]; i < 1 \rightarrow \text{true}$$

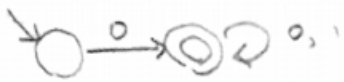
$$\begin{aligned} & \bullet [i \mid \rightarrow 0] (i) = 0 \\ & \bullet [i \mid \rightarrow 0]; i \rightarrow 0 \bullet [i \mid \rightarrow 0]; 1 \rightarrow 1 \text{ is } 0 + 1 \\ & \bullet [i \mid \rightarrow 0] (i) = 0 \quad \bullet [i \mid \rightarrow 0]; i + 1 \rightarrow 1 \\ (2) \quad & \bullet [i \mid \rightarrow 0]; i = i + 1 \rightarrow \bullet [i \mid \rightarrow 1] \end{aligned}$$

$$\begin{aligned} & \bullet [i \mid \rightarrow 1] (i) = 1 \\ & \bullet [i \mid \rightarrow 1]; i \rightarrow 1 \quad \bullet [i \mid \rightarrow 1]; 1 \rightarrow 1 \quad \text{false is } 1 < 1 \\ & \bullet [i \mid \rightarrow 1]; i < 1 \rightarrow \text{false} \\ (3) \quad & \bullet [i \mid \rightarrow 1]; \text{while } (i < 1) (i = i + 1) \rightarrow \bullet [i \mid \rightarrow 1] \end{aligned}$$

Create a FA over $\Sigma = \{0, 1\}$ that:

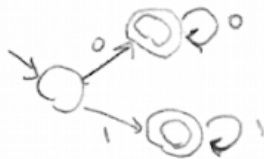
Accepts strings that start w/ 0.

(Accepts: "0", "010". Rejects: "", "100".)



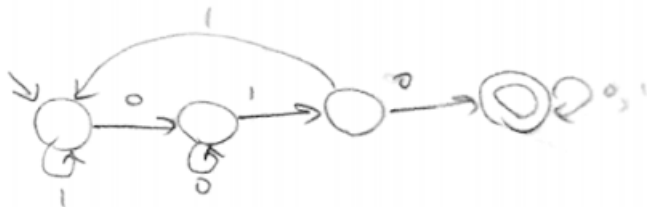
Accepts strings w/ all 0s or all 1s.

(Accepts: "000", "111". Rejects: "", "010".)



Accepts strings w/ the substring "010".

(Accepts: "010", "01010". Rejects: "00", "0110".)



Accepts strings that have a 0 mod 3 0s and 0 mod 3 1s.

(Accepts: "", "000", "000000111". Rejects: "0", "010".)

