Bifurcations affect our ability to learn parameters of dynamical systems.

Parameter inference in dynamical systems with co-dimension 1 bifurcations

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INTRO

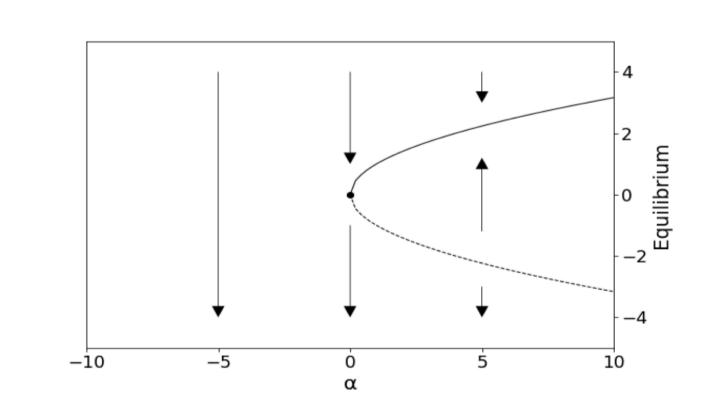
- We want to gain **mechanistic insights** into dynamical systems via **reverse engineering**:
 - 1. develop **models**
 - 2. design discriminatory experiments
 - 3. make testable **predictions**
- It is important to understand in which cases reverse engineering methods work well.
- Here, we evaluate the ability to perform parameter inference in respect to qualitative model dynamics.

METHODS

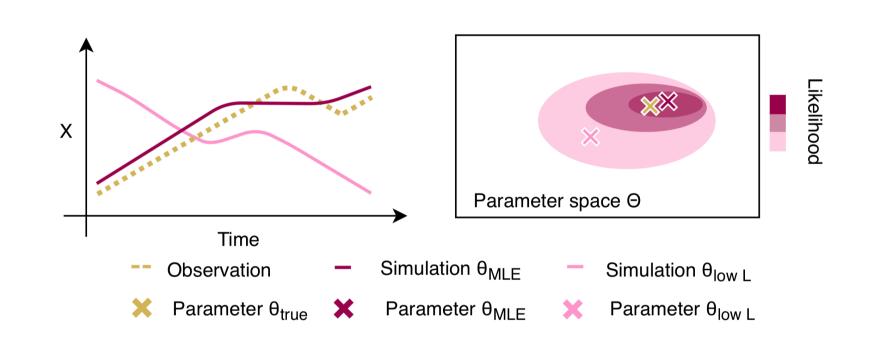
 A dynamical system is often described via a ordinary differential equation (ODE).

$$\frac{\partial \mathbf{X}}{\partial \mathbf{t}} = \alpha - \mathbf{X}^2$$

• Here, we us ODEs to describe dynamical systems with **bifurcations**.



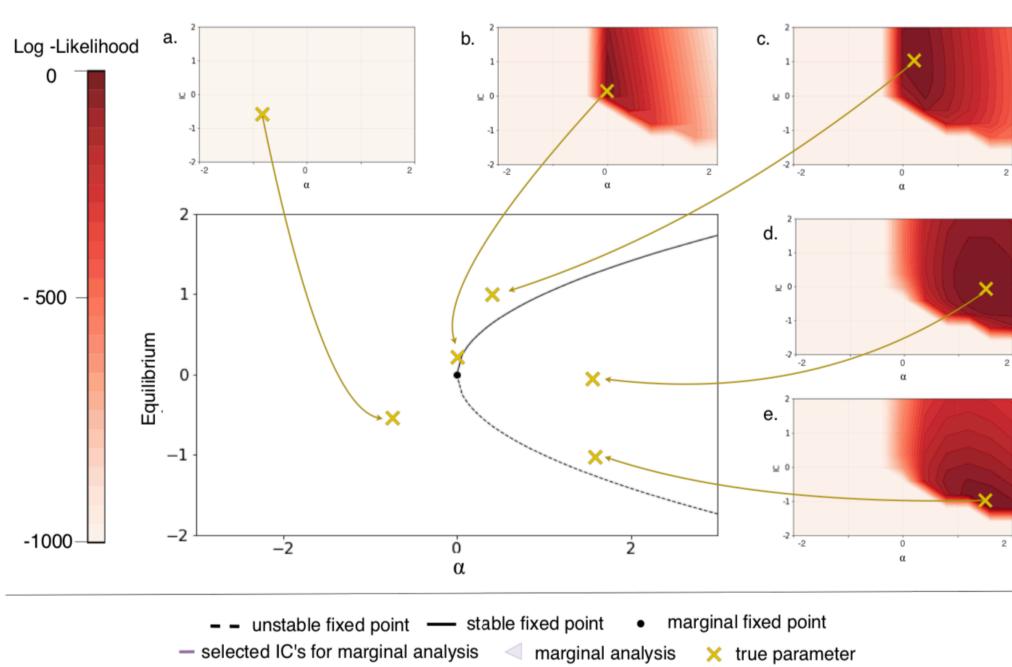
We use the maximum likelihood estimate
 (MLE) to identify which parameters of the
 bifurcating systems explain observed data
 well.

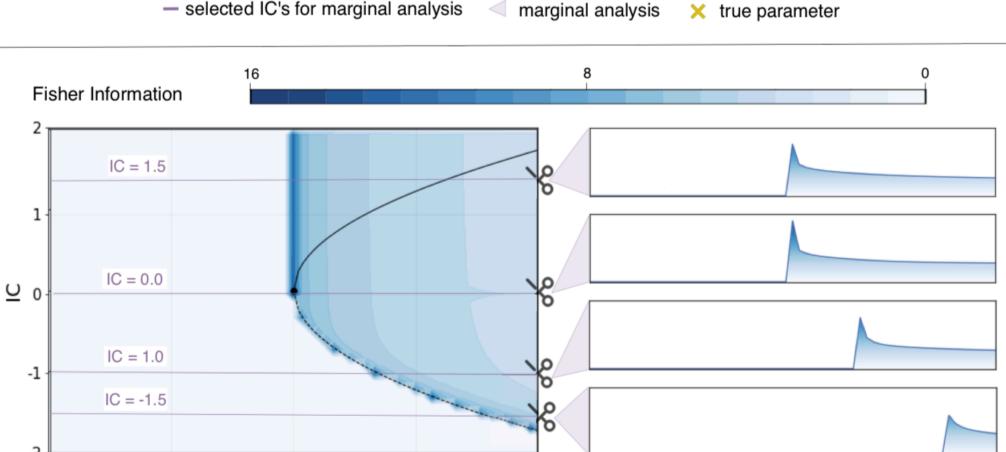


RESULTS + DISCUSSION

- We analyse four dynamical with distinct
 co-dimension 1 bifurcations.
- We infer bifurcation parameters and initial conditions using the MLE.
- We evaluate the performance by investigating the observed Fisher information.
- For all bifurcations, the global stability properties affect our ability to perform parameter inference.
- Our analysis suggests that some parameters will be **systematically** more difficult to infer than others.

Parameter inference of the Saddle node bifurcation





Parameter inference of three co-dimension 1 bifurcations

1.5

-1.5

