Introduction to Statistical Methods

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Team ISM

Session No 6

Sampling & Estimation

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Contact Session	List of Topic Titles	Reference
CS – 6	Sampling & Estimation	R1 : Chapter – 6 & 7
HW	Homework Problems	R1 : Chapter – 6 & 7

Sampling

➢ Sampling is widely used in business as a means of gathering useful information about a population.

➢ Data are gathered from samples and conclusions are drawn about the population as a part of the inferential statistics process

➢ A sample provides a reasonable means for gathering useful decision-making information that might be otherwise unattainable and unaffordable.

Reasons for Sampling

Taking a sample instead of conducting a census offers several advantages

1. The sample can save money.

2. The sample can save time.

3. For given resources, the sample can broaden the scope of the study.

4. If accessing the population is impossible, the sample is the only option.

Random Versus Non random Sampling

➢ In **random** sampling every unit of the population has the same probability of being selected into the sample.

➢ In **nonrandom** sampling not every unit of the population has the same probability of being selected into the sample.

Stratified Random Sampling

➤ In this, the population is divided into non overlapping **subpopulations** called **strata**.

➤ The researcher then extracts a random sample from each of the subpopulations.

➤ The main reason for using stratified random sampling is that it has the potential for reducing sampling error.

➤ With stratified random sampling, the potential to match the sample closely to the population is greater than it is with simple random sampling because portions of the total sample are taken from different population subgroups.

Sampling Error

➢ **Sampling error** occurs *when the sample is not representative of the population.*

➢ When random sampling techniques are used to select elements for the sample, sampling error occurs by chance.

Population of Wages of employees of an organization

1861	2495	1000	2497	1865	791	2090	2637	1327	1678
1680	2858	795	2495	2496	2501	1160	1480	1860	2490
2090	2840	2490	2640	659	827	2646	2638	2643	868
1327	1866	1861	2486	2865	3011	2494	1489	1865	2855
2840	2499	2093	2660	1165	2600	2085	2640	2998	1861
2956	2495	2865	1865	3000	3019	1670	2858	2642	1680
3038	3000	1313	596	656	3240	590	2501	2485	3015
2092	1679	3024	2497	2825	2630	2070	2900	1861	2636
2495	2637	2497	1159	2640	3050	870	2896	2500	2638
926	2860	1481	875	2482	1860	2086	934	3200	2490

Select different samples of varied sizes

Sample 1

| 3000 | 2486 | 820 | 1678 | 2070 | 2638 | 2490 | 1865 | 1000 | 2090 | 596 | 3200 |

Sample 2

| 2840 | 2858 | 3000 | 2490 | 2998 | 3050 | 2070 | 2896 | 3200 | 2490 | 3280 |

Sample 3

| 2858 | 3240 | 2497 | 2865 | 656 | 2093 | 934 | 1861 | 868 | 795 |

Sample 4

| 2086 | 1000 | 2497 | 596 | 656 | 875 | 2085 | 934 | 1313 |

Sample 5

| 820 | 1313 | 3000 | 2640 | 596 | 2640 | 2600 | 2495 | 934 | 2500 |

Select different samples of varied sizes

Sample 6

2840	2499	1327	1861	2495	3024	3038	2497

Sample 7

2858	2490	868	1670	1480	2643	1480	1680	2085	2490

Sample 8

2495	2858	1861	2092	2499	3000	2660	1000	1679	926	2660

Sample 9

795	791	3200	2085	2638	2497	2486	1159	2640

Sample 10

3019	3240	3200	3050	3000	3015	2900	2896	2998

Compute sample mean of these samples

Sample No.	Sample size	Mean	SD
1	12	1994.42	843.23
2	11	2830.18	349.94
3	10	1866.70	988.57
4	9	1338.00	704.36
5	10	1953.80	920.44
6	8	2447.63	590.64
7	10	1974.40	638.05
8	11	2157.27	715.10
9	9	2032.33	891.53
10	9	3035.33	117.40
Overall	100	2162.24	732.26

Sampling Variability

➢ The term "sampling variability" refers to the fact that the statistical information from a sample (called a *statistic*) will vary as the random sampling is repeated.

➢ **Sampling variability** will **decrease** as the **sample size increases.**

➢ the samples must be randomly chosen, must be of the same size (not smaller than 30), and the more samples that are used, the more reliable the information gathered will be.

Do you consider these sample means and sample SDs as variable?

If yes, should we not describe the distribution of these variables?

The distribution of the sample estimates is called sampling distribution

For example the distribution of sample means is called Sampling distribution of mean

Definition

➢ The probability distribution of a statistic (sample estimate) is called sampling distribution.

➢ The sampling distribution of a statistic depends on the distribution of the population, the size of the sample, and the method of sample selection.

Sampling Distribution Of $\bar{x}$

➢ The sample mean is one of the more common statistics used in the inferential process.

➢ The **distribution** of the values of the sample mean ($\bar{x}$) in repeated **samples** is called the **sampling distribution of** $\bar{x}$

➢ One way to examine the distribution possibilities is to take a population with a particular distribution, randomly select samples of a given size, compute the sample means, and attempt to determine how the means are distributed.

Example

➢ Suppose a small finite population consists of only *N* = 8 numbers:

➢   54 55 59 63 64 68 69 70

➢ Using an Excel-produced histogram, we can see the shape of the distribution of this population of data.
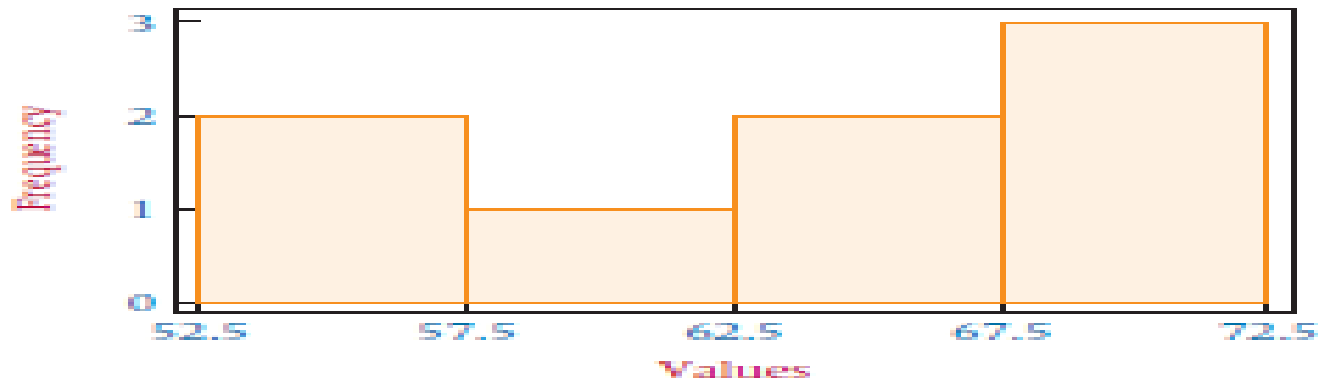
➢ Suppose we take all possible samples of size *n* = 2 from this population with replacement.

Example

The result is the following pairs of data.

(54,54)	(55,54)	(59,54)	(63,54)
(54,55)	(55,55)	(59,55)	(63,55)
(54,59)	(55,59)	(59,59)	(63,59)
(54,63)	(55,63)	(59,63)	(63,63)
(54,64)	(55,64)	(59,64)	(63,64)
(54,68)	(55,68)	(59,68)	(63,68)
(54,69)	(55,69)	(59,69)	(63,69)
(54,70)	(55,70)	(59,70)	(63,70)
(64,54)	(68,54)	(69,54)	(70,54)
(64,55)	(68,55)	(69,55)	(70,55)
(64,59)	(68,59)	(69,59)	(70,59)
(64,63)	(68,63)	(69,63)	(70,63)
(64,64)	(68,64)	(69,64)	(70,64)
(64,68)	(68,68)	(69,68)	(70,68)
(64,69)	(68,69)	(69,69)	(70,69)
(64,70)	(68,70)	(69,70)	(70,70)

The means of each of these samples follow.

54	54.5	56.5	58.5	59	61	61.5	62
54.5	55	57	59	59.5	61.5	62	62.5
56.5	57	59	61	61.5	63.5	64	64.5
58.5	59	61	63	63.5	65.5	66	66.5
59	59.5	61.5	63.5	64	66	66.5	67
60	61.5	63.5	65.5	66	68	68.5	69
61.5	62	64	66	66.5	68.5	69	69.5
62	62.5	64.5	66.5	67	69	69.5	70

➤ Again using an Excel-produced histogram, we can see the shape of the distribution of these sample means.
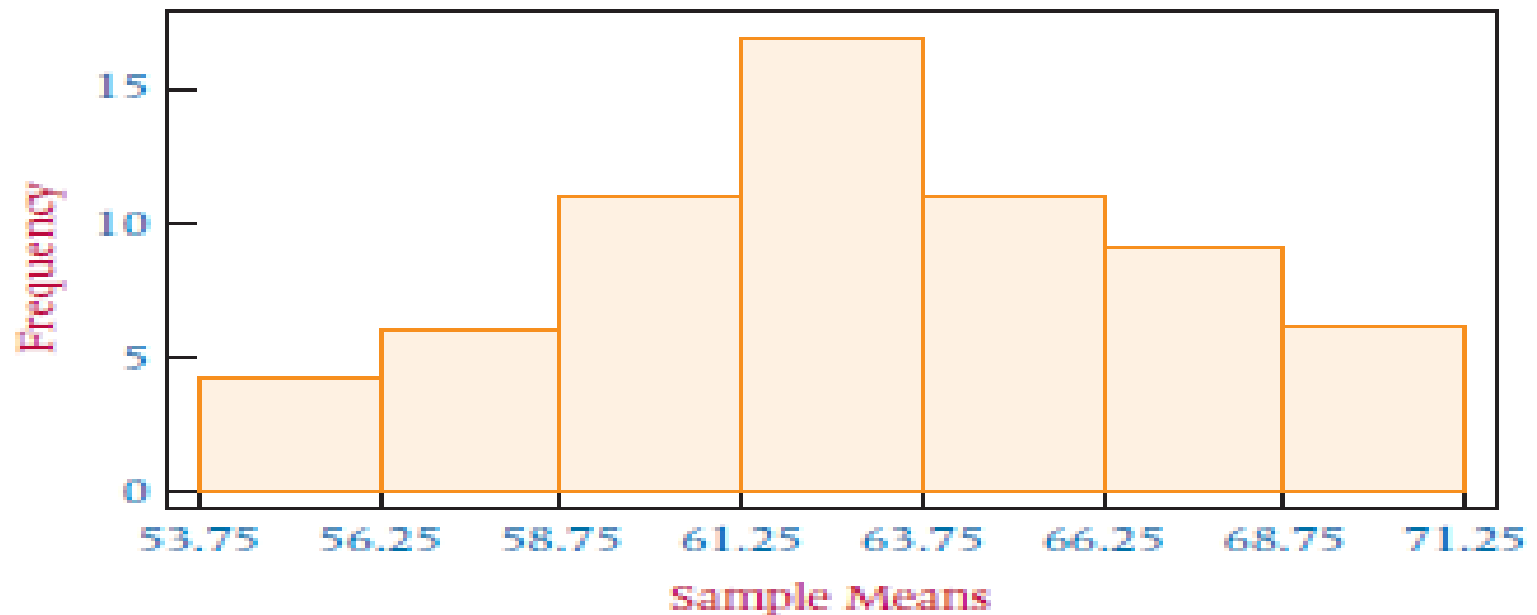
Conclusions

➢ Notice that the shape of the histogram for sample means is quite unlike the shape of the histogram for the population.

➢ The sample means appear to "pile up" toward the middle of the distribution and "tail off" toward the extremes.

➢ As sample sizes become much larger, the sample mean distributions begin to approach a **normal distribution** and the variation among the means decreases.

Sample Means from 90 Samples Ranging in Size from n = 2 to n = 30 from a Uniformly Distributed Population with a = 10 and b = 30
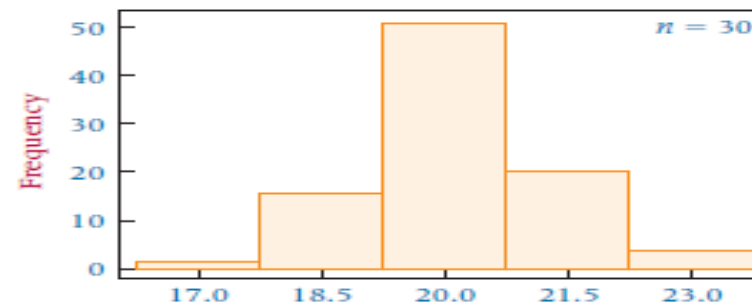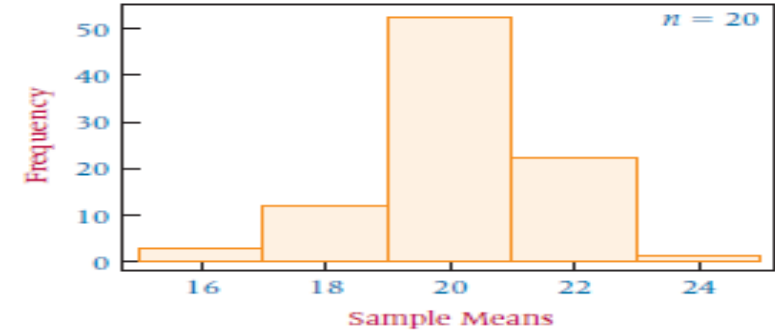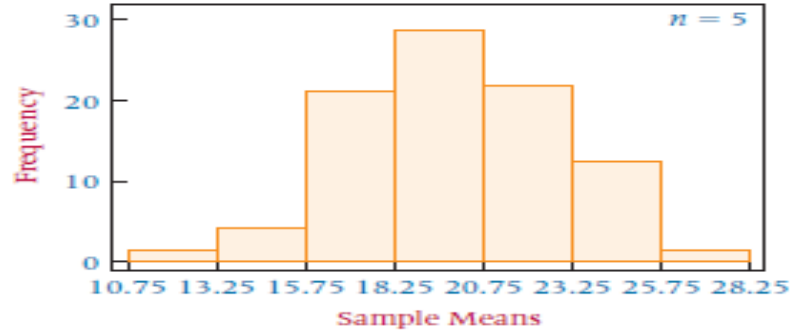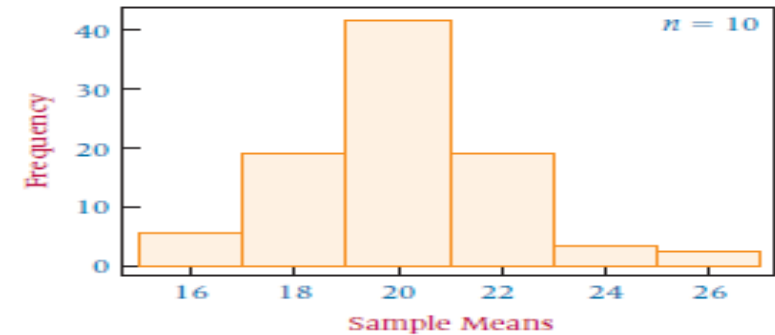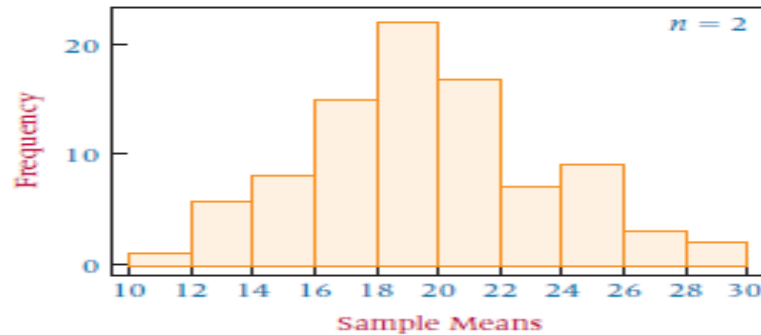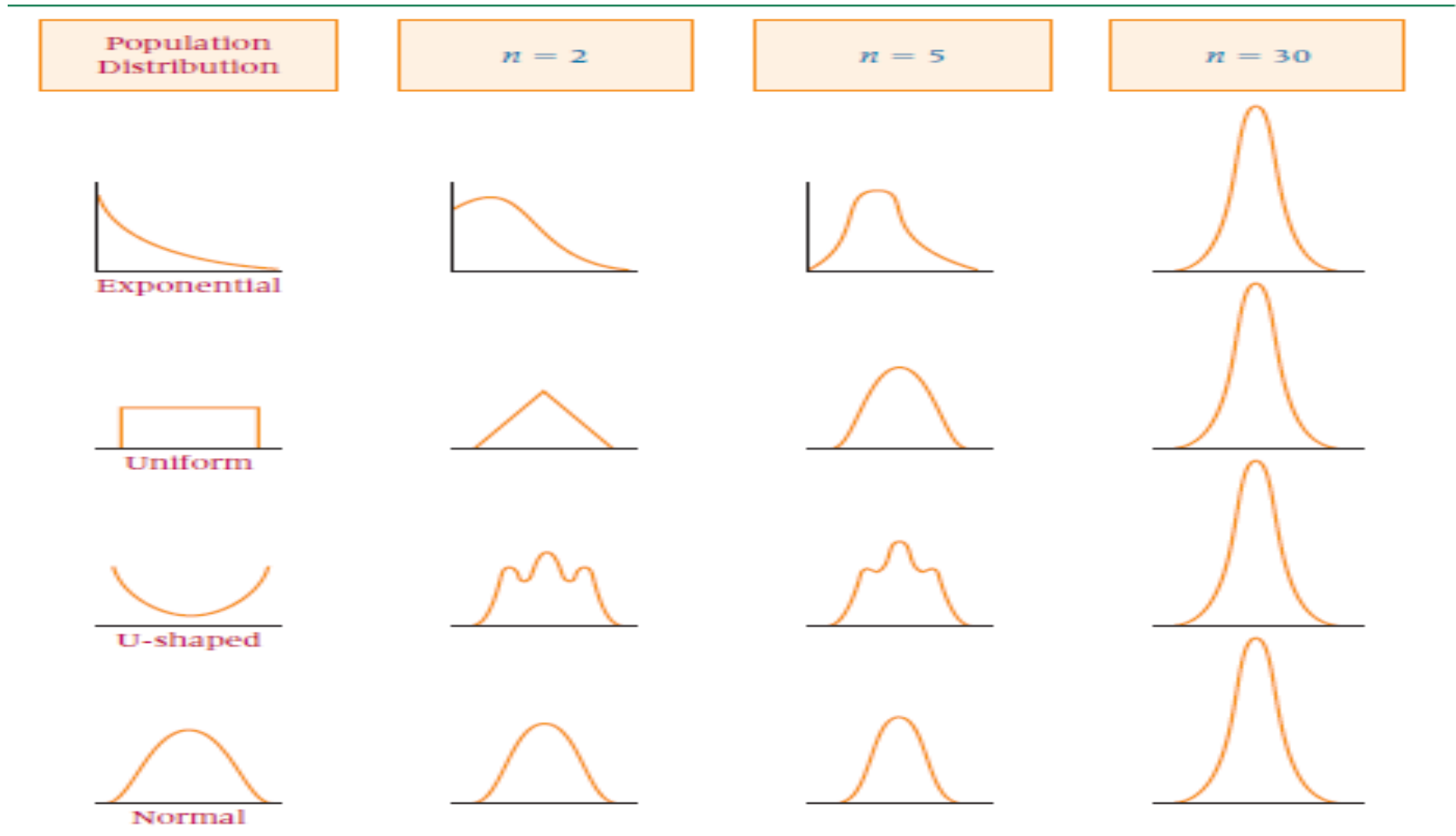
Shapes of the Distributions of Sample Means

Central Limit Theorem

➢ If samples of size *n* are drawn randomly from a population that has a mean of μ and a standard deviation of σ, the sample means, $\bar{x}$, are approximately normally distributed for sufficiently large sample sizes (*n >=* 30) regardless of the shape of the population distribution.

➢ If the population is normally distributed, the sample means are normally distributed for any size sample.

➢ From mathematical expectation

$$\mu_{\bar{x}} = \mu \qquad\qquad \sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}}$$

Z score for sample means

➢ The central limit theorem states that sample means are normally distributed regardless of the shape of the population for large samples and for any sample size with normally distributed populations.

➢ Thus, **sample means** can be **analyzed** by using **z scores**

➢ The formula to determine z scores for individual values from a normal distribution:

$$z = \frac{x - \mu}{\sigma}$$

➢ If sample means are normally distributed, the z score formula applied to sample means would be

$$z = \frac{\bar{x} - \mu_{\bar{x}}}{\sigma_{\bar{x}}}$$

➢ The standard deviation of the statistic of interest is $\sigma_{\bar{x}}$, sometimes referred to as the **standard error of the mean.**

Suppose the mean expenditure per customer at a tire store is $85.00, with a standard deviation of $9.00.

If a random sample of 40 customers is taken, what is the probability that the sample average expenditure per customer for this sample will be $87.00 or more?
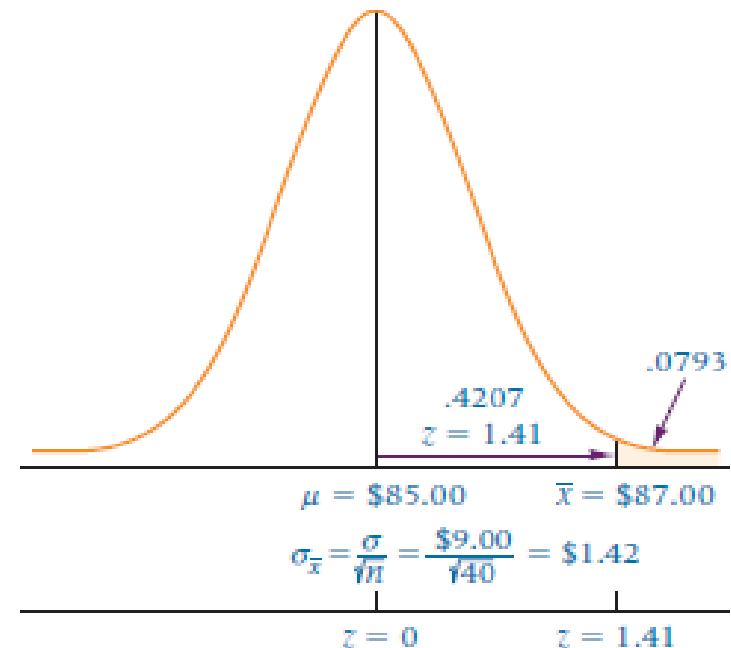
Because the sample size is greater than 30, the central limit theorem

Can be used, and the sample means are normally distributed.

μ= $85 σ= $9

$$z = \frac{\bar{x} - \mu}{\frac{\sigma}{\sqrt{n}}} = \frac{\$87.00 - \$85.00}{\frac{\$9.00}{\sqrt{40}}} = \frac{\$2.00}{\$1.42} = 1.41$$

.0793

.4207
z = 1.41

μ = \$85.00 $\bar{x}$ = \$87.00

$$\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}} = \frac{\$9.00}{\sqrt{40}} = \$1.42$$

z = 0   z = 1.41

Suppose that during any hour in a large department store, the average number of shoppers is 448, with a standard deviation of 21 shoppers.

What is the probability that a random sample of 49 different shopping hours will yield a sample mean between 441 and 446 shoppers?

For this problem, μ= 448, σ= 21, and n = 49. The problem is to determine

P(441<= $\bar{x}$ <=446).

The following

$$z = \frac{441 - 448}{\frac{21}{\sqrt{49}}} = \frac{-7}{3} = -2.33$$

$$z = \frac{446 - 448}{\frac{21}{\sqrt{49}}} = \frac{-2}{3} = -0.67$$

Sampling from a Finite Population

➢ The earlier example was based on the assumption that the population was infinitely or extremely large.

➢ In cases of a finite population, *a statistical adjustment can be made to the z formula for sample means*. The adjustment is called the **finite correction factor**

$$\sqrt{\frac{N - n}{N - 1}}.$$

➢ Following is the z formula for sample means when samples are drawn from finite populations.

$$z = \frac{\bar{x} - \mu}{\frac{\sigma}{\sqrt{n}}\sqrt{\frac{N - n}{N - 1}}}$$

Rules for finite population

➢ As the size of the finite population becomes larger in relation to sample size, the finite correction factor approaches 1.

➢ In theory, whenever researchers are working with a finite population, they can use the finite correction factor.

➢ A rough rule of thumb for many researchers is that, if the sample size is **less** than **5%** of the finite population size or *n/N* **< 0.05**, the finite correction factor does **not** significantly modify the solution.

Example

A production company's 350 hourly employees average 37.6 years of age, with a standard deviation of 8.3 years.

If a random sample of 45 hourly employees is taken, what is the probability that the sample will have an average age of less than 40 years?

Solution

➢ The population mean is 37.6, with a population standard deviation of 8.3.

➢ The sample size is 45, but it is being drawn from a finite population of 350; that is, n = 45 and N = 350.

➢ The sample mean under consideration is 40

➢ Using the z formula with the finite correction factor gives

$$z = \frac{40 - 37.6}{\frac{8.3}{\sqrt{45}}\sqrt{\frac{350 - 45}{350 - 1}}} = \frac{2.4}{1.157} = 2.07$$

➢ This z value yields a probability of .480

➢ Therefore, the probability of getting a

➢ sample average age of less than

➢ 40 years is **.4808 + .5000 = .9808.**

$\mu = 37.6$ $\bar{x} = 40$

$z = 0$ $z = 2.07$
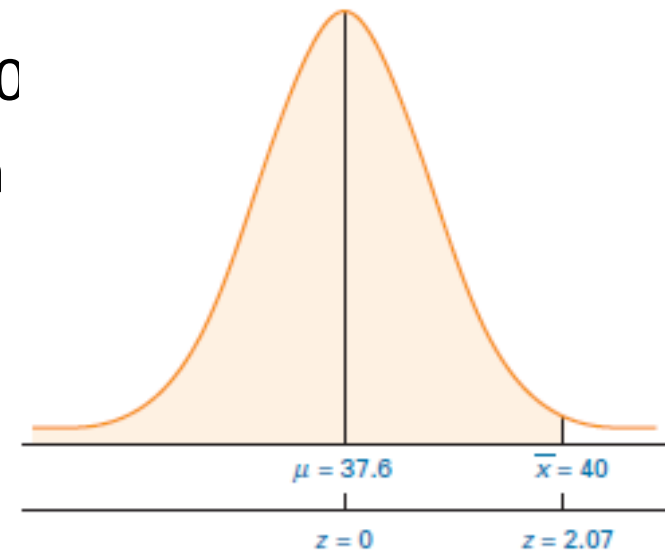
Sampling Distribution Of Sample Proportion

➢ If research results in **countable** items such as how many people in a sample have a flexible work schedule, the sample proportion is often the statistic of choice.

SAMPLE PROPORTION

$$\hat{p} = \frac{x}{n}$$

where

x = number of items in a sample that have the characteristic

n = number of items in the sample

Example

➢ In a sample of 100 factory workers, 30 workers might belong to a union.

➢ The value of sample proportion for this characteristic, union membership, is

$$30/100 = 0.30$$

How does a researcher use the sample proportion in analysis?

➢ The central limit theorem applies to sample proportions in that the normal distribution approximates the shape of the distribution of sample proportions

➢ If $n*p > 5$ and $n*q > 5$(p is the population proportion and q = 1 - p).

➢ The mean of sample proportions for all samples of size n randomly drawn from a population is p (the population proportion) and the standard deviation of sample proportions is $\sqrt{\dfrac{p \cdot q}{n}}$

➢ sometimes referred to as the **standard error of the proportion**

Z Formula For Sample Proportions

For *n*p* > 5 and *n*q* > 5

$$z = \frac{\hat{p} - p}{\sqrt{\dfrac{p \cdot q}{n}}}$$

where

$\hat{p}$ = sample proportion
n = sample size
p = population proportion
$q = 1 - p$

Example

Suppose 60% of the electrical contractors in a region use a particular brand of wire. What is the probability of taking a random sample of size 120 from these electrical contractors and finding that .50 or less use that brand of wire?
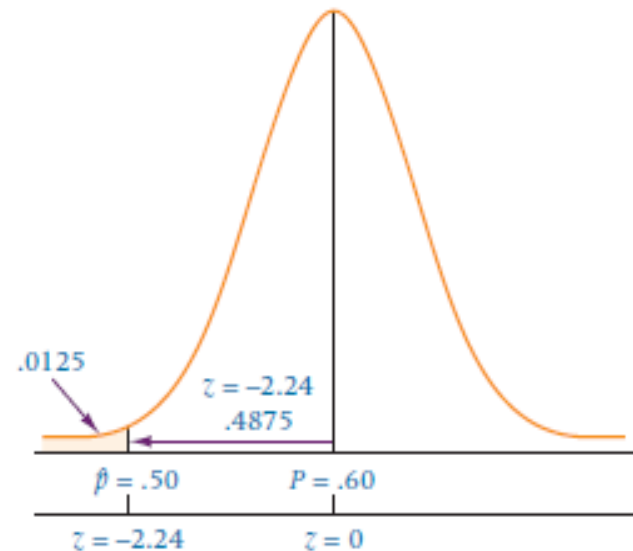
Solution

$p = .60 \quad \hat{p} = .50 \quad n = 120$

The z formula yields

$$z = \frac{.50 - .60}{\sqrt{\dfrac{(.60)(.40)}{120}}} = \frac{-.10}{.0447} = -2.24$$

= -2.24 is .4875.

.0125

$z = -2.24$
.4875

$\hat{p} = .50$ $P = .60$

$z = -2.24$ $z = 0$

For $z < -2.24$ (the tail of the distribution), the answer is .5000 - .4875 = **.0125**.
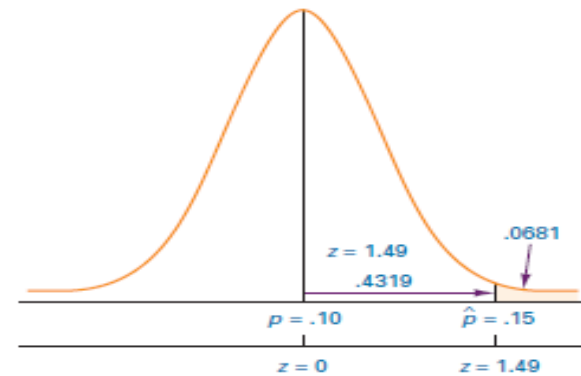
Example

If 10% of a population of parts is defective, what is the probability of randomly selecting 80 parts and finding that 12 or more parts are defective?

Solution

Here, $p = .10$, $\hat{p} = 12/80 = .15$, and $n = 80$. Entering these values in the z formula yields

$$z = \frac{.15 - .10}{\sqrt{\dfrac{(.10)(.90)}{80}}} = \frac{.05}{.0335} = 1.49$$

- The probability of .4319 for a z value of 1.49, which is the area between the sample proportion, .15, and the population proportion, .10. The answer to the question is

$$P(\hat{p} \geq .15) = .5000 - .4319 = .0681.$$

Forms Of Statistical Inference

❖ Three forms of statistical inference

➢ Point estimation

➢ Interval estimation

➢ Hypothesis testing

Point Estimate

- ➢ A **point estimate** is a statistic taken from a sample that is used to estimate a population parameter.
- ➢ A point estimate is only as good as the representativeness of its sample.
- ➢ If other random samples are taken from the population, the point estimates derived from those samples are likely to vary.

Interval Estimate

➢ Because of variation in sample statistics, estimating a population parameter with an interval estimate is often preferable to using a point estimate.

➢ An interval estimate (**confidence interval**) is a range of values within which the analyst can declare, with some confidence, the population parameter lies.

Confidence Interval to Estimate μ

$100(1-\alpha)\%$ CONFIDENCE

INTERVAL TO ESTIMATE μ:

σ KNOWN (8.1)   or
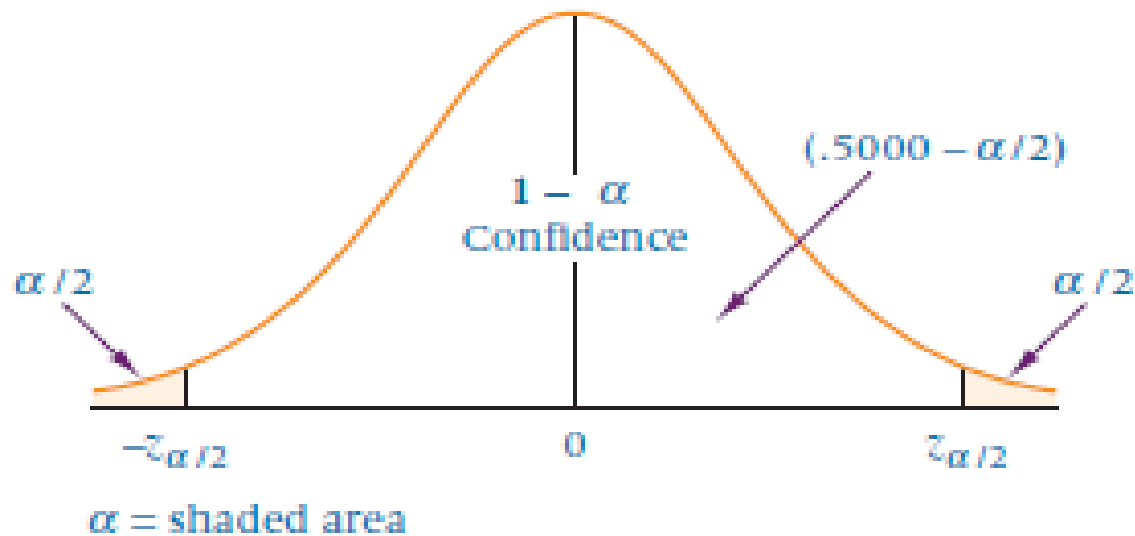
$$\bar{x} \pm z_{\alpha/2}\frac{\sigma}{\sqrt{n}}$$

$$\bar{x} - z_{\alpha/2}\frac{\sigma}{\sqrt{n}} \leq \mu \leq \bar{x} + z_{\alpha/2}\frac{\sigma}{\sqrt{n}}$$

where

α = the area under the normal curve outside the confidence interval area

$\alpha/2$ = the area in one end (tail) of the distribution outside the confidence interval

Confidence Intervals

In the cellular telephone company, problem of estimating the population mean number of minutes called per residential user per month, from the sample of 85 bills it was determined that the sample mean is 510 minutes.

Suppose past history and similar studies indicate that the population standard deviation is 46 minutes.

Determine a 95% confidence interval.

The business researcher can now complete the cellular telephone problem. To determine a 95% confidence interval for $\bar{x} = 510$, $\sigma = 46$, $n = 85$, and $z = 1.96$, the researcher estimates the average call length by including the value of z in formula 8.1.

$$510 - 1.96\frac{46}{\sqrt{85}} \leq \mu \leq 510 + 1.96\frac{46}{\sqrt{85}}$$

$$510 - 9.78 \leq \mu \leq 510 + 9.78$$

$$500.22 \leq \mu \leq 519.78$$

➢ The confidence interval is constructed from the point estimate, which in this problem is 510 minutes, and the error of this estimate, which is 9.78 minutes.

➢ The resulting confidence interval is 500.22 <= μ <= 519.78.

➢ The cellular telephone company researcher is 95%, confident that the average length of a call for the population is between 500.22 and 519.78 minutes.

Example

A survey was taken of U.S. companies that do business with firms in India. One of the questions on the survey was: Approximately how many years has your company been trading with firms in India?

A random sample of 44 responses to this question yielded a mean of 10.455 years. Suppose the population standard deviation for this question is 7.7 years.

Using this information, construct a 90% confidence interval for the mean number of years that a company has been trading in India for the population of U.S. companies trading with firms in India.

Solution

Here, n= 44, $\bar{x}$= 10.455 and σ= 7.7. To determine the value of $z_{\alpha/2}$, divide the 90% confidence in half, or take .5000 - α/2= .5000 - .0500= 0.45 where α= 10%.

Z table yields a z value of 1.645 for the area of .45

The confidence interval is

$$\bar{x} - z\frac{\sigma}{\sqrt{n}} \le \mu \le \bar{x} + z\frac{\sigma}{\sqrt{n}}$$

$$10.455 - 1.645\frac{7.7}{\sqrt{44}} \le \mu \le 10.455 + 1.645\frac{7.7}{\sqrt{44}}$$

$$10.455 - 1.910 \le \mu \le 10.455 + 1.910$$

$$8.545 \le \mu \le 12.365$$

A study is conducted in a company that employs 800 engineers. A random sample of 50 engineers reveals that the average sample age is 34.3 years. Historically, the population standard deviation of the age of the company's engineers is approximately 8 years.

Construct a 98% confidence interval to estimate the average age of all the engineers in this company.

Solution

❖ This problem has a finite population. The sample size, 50, is greater than 5% of the population, so the finite correction factor may be helpful.

❖ In this case N = 800, n = 50, $\bar{x}$ = 34.3 and σ = 8

❖ The z value for a 98% confidence interval is 2.33

$$34.30 - 2.33 \frac{8}{\sqrt{50}} \sqrt{\frac{750}{799}} \leq \mu \leq 34.30 + 2.33 \frac{8}{\sqrt{50}} \sqrt{\frac{750}{799}}$$

$$34.30 - 2.55 \leq \mu \leq 34.30 + 2.55$$

$$31.75 \leq \mu \leq 36.85$$

Estimating The Population Proportion

- Methods similar to those used earlier can be used to estimate the population proportion.

- The central limit theorem for sample proportions led to the following formula

$$z = \frac{\hat{p} - p}{\sqrt{\frac{p \cdot q}{n}}}$$

- where q = 1 - p. Recall that this formula can be applied only when n*p and n*q are **greater** than **5**.

- for confidence interval purposes only and for large sample sizes— is substituted for p in the denominator, yielding

$$z = \frac{\hat{p} - p}{\sqrt{\frac{\hat{p} \cdot \hat{q}}{n}}}$$

Confidence Interval To Estimate P

$$\hat{p} - z_{\alpha/2}\sqrt{\frac{\hat{p} \cdot \hat{q}}{n}} \le p \le \hat{p} + z_{\alpha/2}\sqrt{\frac{\hat{p} \cdot \hat{q}}{n}}$$

where

$\hat{p} = $ sample proportion

$\hat{q} = 1 - \hat{p}$

$p = $ population proportion

$n = $ sample size

In this formula, $\hat{p}$ is the point estimate and $\pm z_{\alpha/2}\sqrt{\frac{\hat{p} \cdot \hat{q}}{n}}$ is the error of the estimation.

Example

A study of 87 randomly selected companies with a telemarketing operation revealed that 39% of the sampled companies used telemarketing to assist them in order processing.

Using this information, how could a researcher estimate the *population* proportion of telemarketing companies that use their telemarketing operation to assist them in order processing?

Solution

The sample proportion, $\hat{p}$ = .39, is the *point estimate* of the population proportion, p. For n = 87 and $\hat{p}$ = .39, a 95% confidence interval can be computed to determine the interval estimation of p. The z value for 95% confidence is 1.96. The value of $\hat{q}$ = 1 − $\hat{p}$ = 1 − .39 = .61. The confidence interval estimate is

$$.39 - 1.96\sqrt{\frac{(.39)(.61)}{87}} \le p \le .39 + 1.96\sqrt{\frac{(.39)(.61)}{87}}$$

$$.39 - .10 \le p \le .39 + .10$$

$$.29 \le p \le .49$$

Example

Coopers & Lybrand surveyed 210 chief executives of fast-growing small companies. Only 51% of these executives had a management succession plan in place. A spokesperson for Cooper & Lybrand said that many companies do not worry about management succession unless it is an immediate problem. However, the unexpected exit of a corporate leader can disrupt and unfocus a company for long enough to cause it to lose its momentum.

Use the data given to compute a 92% confidence interval to estimate the proportions

The point estimate is the sample proportion given to be .51. It is estimated that .51, or 51% of all fast-growing small companies have a management succession plan. Realizing that the point estimate might change with another sample selection, we calculate a confidence interval.

The value of n is 210; $\hat{p}$ is .51, and $\hat{q} = 1 - \hat{p} = .49$. Because the level of confidence is 92%, the value of $z_{.04} = 1.75$. The confidence interval is computed as

$$.51 - 1.75\sqrt{\frac{(.51)(.49)}{210}} \leq p \leq .51 + 1.75\sqrt{\frac{(.51)(.49)}{210}}$$

$$.51 - .06 \leq p \leq .51 + .06$$

$$.45 \leq p \leq .57$$

Exercise

A clothing company produces men's jeans. The jeans are made and sold with either a regular cut or a boot cut. In an effort to estimate the proportion of their men's jeans market in Oklahoma City that prefers boot-cut jeans, the analyst takes a random sample of 212 jeans sales from the company's two Oklahoma City retail outlets. Only 34 of the sales were for boot-cut jeans.

Construct a 90% confidence interval to estimate the proportion of the population in Oklahoma City who prefer boot-cut jeans.

The sample size is 212, and the number preferring boot-cut jeans is 34. The sample proportion is $\hat{p} = 34/212 = .16$. A point estimate for boot-cut jeans in the population is .16, or 16%. The z value for a 90% level of confidence is 1.645, and the value of $\hat{q} = 1 - \hat{p} = 1 - .16 = .84$. The confidence interval estimate is

$$.16 - 1.645\sqrt{\frac{(.16)(.84)}{212}} \leq p \leq .16 + 1.645\sqrt{\frac{(.16)(.84)}{212}}$$

$$.16 - .04 \leq p \leq .16 + .04$$

$$.12 \leq p \leq .20$$

Estimating The Population Variance

➢ Sample variance is computed by using the formula $\qquad s^2 = \dfrac{\sum(x - \bar{x})^2}{n - 1}$

➢ Mathematical adjustment is made in the denominator by using n - 1 to make the sample variance an unbiased estimator of the population variance.

➢ Suppose a researcher wants to estimate the population variance from the sample variance in a manner that is similar to the estimation of the population mean from a sample mean.

➢ The relationship of the sample variance to the population variance is captured by the **chi-square distribution**

Chi-square Statistic

➢ Although the technique is still rather widely presented as a mechanism for constructing confidence intervals to estimate a population variance, you should proceed with extreme caution and **apply** the technique **only** in cases **where** the **population** is known to be **normally distributed**. We can say that this technique lacks robustness.

χ^2 **FORMULA FOR SINGLE VARIANCE (8.5)**

$$\chi^2 = \frac{(n-1)s^2}{\sigma^2}$$

$$df = n - 1$$
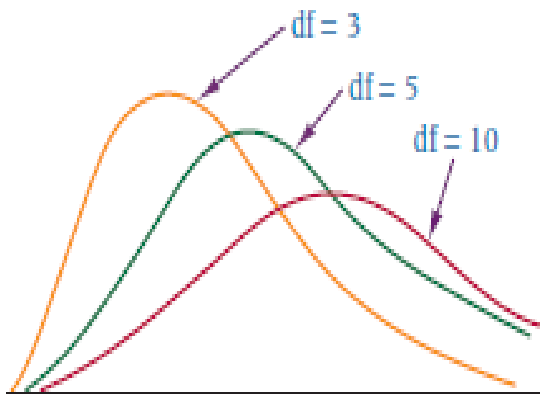
df = 3
df = 5
df = 10

Three Chi-Square Distributions

Question :

Car mufflers are constructed by nearly automatic machine. One manufacturer finds that, for any type of car muffler, the time for a person to set up and complete a production run has a normal distribution with mean 1.82 hours and standard deviation 1.20.

What is the probability that the sample mean of the next 40 runs will be from 1.65 to 2.04 hours ?

Question :

Engine bearings depend on a film of oil to keep shaft and bearing surfaces separated. Insufficient lubrication causes bearings to be overloaded. The insufficient lubrication can be modeled as a random variable having a mean 0.6520 ml and standard deviation 0.0125 ml.

The sample mean of insufficient lubrication will be obtained frm a random sample of 60 bearings.

What is the probability that sample mean $\overline{x}$ will be between 0.600 ml and 0.640 ml ?

Question :

A random sample size of n = 100 is taken from a population with σ = 5.1.

Given that the sample mean is $\bar{x}$ = 2.16,

construct a 95% confidence interval for the population mean μ.

Question :

With reference to the data in section 2.1 (of R1) , we have
n = 50 , $\overline{x}$ = 305.58 nm, and s2 = 1366.86(hence, s=36.97 nm),

Construct a 99% confidence interval for the population mean of all nanopillars.

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245	333	296	304	276	336	289	234	253	292
366	323	309	284	310	338	297	314	305	330
266	391	315	305	290	300	292	311	272	312
315	355	346	337	303	265	278	276	373	271
308	276	364	390	298	290	308	221	274	343

Thank You