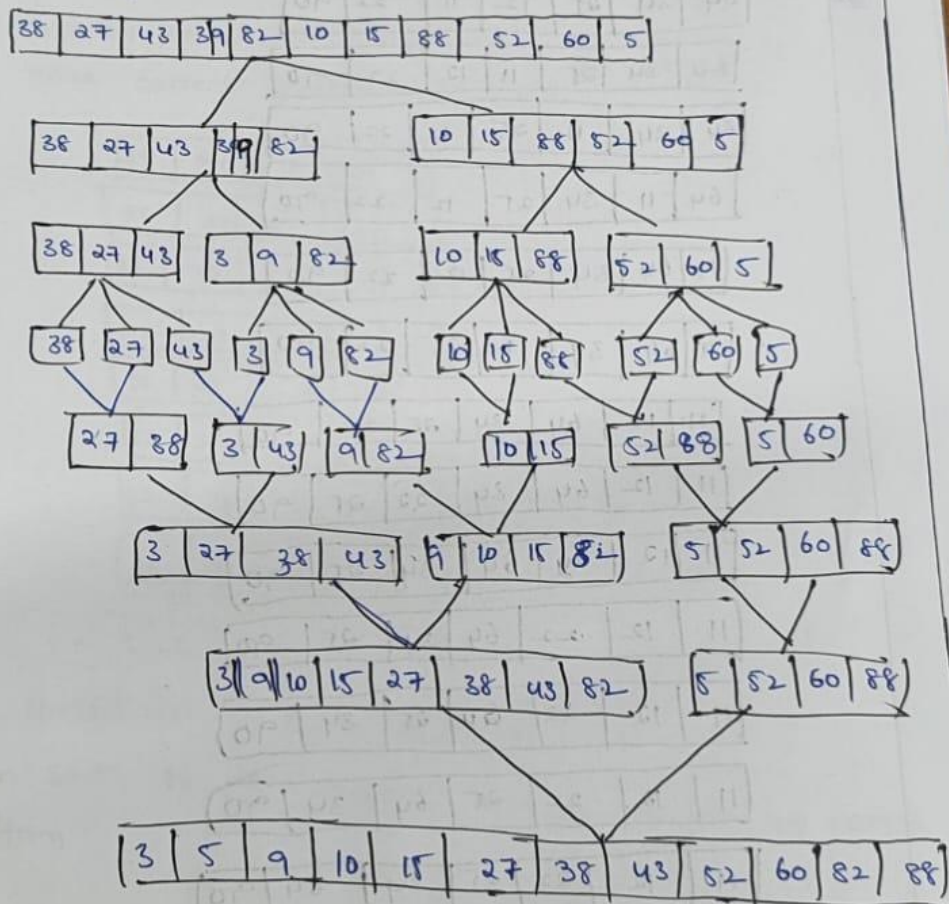


① Sort the array using merge sort data and ~~divide~~ length stage by [38, 27, 43, 39, 82, 10, 15, 88, 52, 60, 5] and analyze the time complexity of the algorithm

sol: Given array: merge sort



\therefore sorted array = [3, 5, 9, 10, 15, 27, 38, 43, 52, 60, 82, 88]

The time complexity of merge sort is $O(n \log n)$ where n is the no. of elements in the list is split into halves $\log n$ times and n

merging is all the elements at each takes $O(n)$ times

- ② sort the array 64, 34, 25, 12, 11, 22, 90 using bubble what is the time complexity of selection sort in the list worst and average case.

Sol:

64	34	25	12	11	22	90
----	----	----	----	----	----	----

64	34	25	11	12	22	90
----	----	----	----	----	----	----

64	34	11	25	12	22	90
----	----	----	----	----	----	----

64	11	34	25	12	22	90
----	----	----	----	----	----	----

11	64	34	25	12	22	90
----	----	----	----	----	----	----

11	64	34	12	25	22	90
----	----	----	----	----	----	----

11	12	64	34	25	22	90
----	----	----	----	----	----	----

11	12	64	34	22	25	90
----	----	----	----	----	----	----

11	12	22	64	34	25	90
----	----	----	----	----	----	----

11	12	22	64	34	25	90
----	----	----	----	----	----	----

11	12	22	64	25	34	90
----	----	----	----	----	----	----

11	12	22	25	64	34	90
----	----	----	----	----	----	----

11	12	22	25	34	64	90
----	----	----	----	----	----	----

③ Sort the array 64, 25, 12, 22, 11 using selection sort what is the P.C of selection sort in the best, worst and average case?

64	25	12	22	11
----	----	----	----	----

In the selection we will find that from the largest element in the array correct position first 50

25	64	12	22	11
----	----	----	----	----

25	12	64	22	11
----	----	----	----	----

25	12	22	64	11
----	----	----	----	----

25	12	22	11	64
----	----	----	----	----

12	25	22	11	64
----	----	----	----	----

12	22	25	11	64
----	----	----	----	----

12	22	11	25	64
----	----	----	----	----

12	11	22	25	64
----	----	----	----	----

11	12	22	25	64
----	----	----	----	----

The sorted list is 11, 12, 22, 25, 64.

Selection sort is another simple comparison sorted algorithm

Best case: $O(n^2)$

Average case: $O(n^2)$

Worst case: $O(n^2)$

- ④ Given an array of $[4, -2, 5, 3, 10, -5, 2, 8, -3, 6, 7, -4, 1, 9, -1, 0, -6, -8, 11, -9]$ integers, sort the following elements using insertion sort using Brute Force Approach strategy analyze complexity of the algorithm.

sol: Given array

$[4, -2, 5, 3, 10, -5, 2, 8, -3, 6, 7, -4, 1, 9, -1, 0, -6, -8, 11, -9]$

Insert 4, -2

$[-2 | 4]$

Insert 5

$[-2 | 4 | 5]$

Insert 10

$[-2 | 3 | 4 | 5 | 10]$

Insert -5

$[-5 | -2 | 3 | 4 | 5 | 10]$

Insert 2

$[-5 | -2 | 2 | 3 | 4 | 5 | 10]$

Insert 8

$[-5 | -2 | 2 | 3 | 4 | 5 | 8 | 10]$

Insert -3

$[-5 | -3 | -2 | 2 | 3 | 4 | 5 | 8 | 10]$

Insert 6

$[-5 | -3 | -2 | 2 | 3 | 4 | 5 | 6 | 8 | 10]$

Insert 7

$[-5 | -3 | -2 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 10]$

Insert -4

$[-5 | -4 | -3 | -2 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 10]$

Insert 9

$[-5 | -4 | -3 | -2 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10]$

Insert -1

$[-5 | -4 | -3 | -2 | -1 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10]$

Insert -6

$[-6 | -5 | -4 | -3 | -2 | -1 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10]$

Insert -8

$[-8 | -6 | -5 | -4 | -3 | -2 | -1 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10]$

Insert -9

$[-9 | -8 | -6 | -5 | -4 | -3 | -2 | -1 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10]$

Time Complexity!

Best case! - $O(n)$ this occurs when the array is already sorted the inner loop runs 300 times for every element

Average case.

This happens because on average the algorithm will have to move half of the element for each insertion

Worst case! $O(n^2)$

This occurs when the array is sorted in reverse order each insertion takes $O(n)$ times

- 5) Sort the following elements using insertion sort using brute force approach strategy [38, 27, 43, 3, 9, 38, 10, 15, 34, 52, 60, 5] and analyse complexity of the algorithm

sol. Insert 38, 27

[27 | 38]

Insert 43!

[27 | 38 | 43]

Insert 3!

[3 | 27 | 38 | 43]

Insert 82!

[3 | 9 | 27 | 38 | 43 | 82]

Insert 10!

[3 | 9 | 10 | 27 | 38 | 43 | 82]

Insert 15!

[3 | 9 | 10 | 15 | 27 | 38 | 43 | 82]

Insert 88!

[3 | 9 | 10 | 15 | 27 | 38 | 43 | 82 | 88]

Insert 62

3	9	10	25	27	38	43	52	62	88
---	---	----	----	----	----	----	----	----	----

Insert 60

3	9	10	25	27	38	43	52	60	82	88
---	---	----	----	----	----	----	----	----	----	----

Insert 5

3	5	9	10	25	27	38	43	52	60	82	88
---	---	---	----	----	----	----	----	----	----	----	----

Time complexity

Best case: $O(n)$

Average case: $O(n^2)$

Worst case: $O(n^2)$