

**CS 301: Formal Languages and Functional Programming, Fall, 2016**  
**Programming Assignment 1, due: Oct 26, 23:59**

1. Implement a Scheme function called `iff`, which takes two truth values as input and returns true (`#t`) when the input values bear the "if and only if" relation to one another and false (`#f`) otherwise.

For example, `(iff #f #f)` returns `#t`.

2. Implement a Scheme function called `exclusive-or`, which takes two truth values as input and returns true if and only if they bear the exclusive-or relation to one another.

3. Implement a Scheme function called `difference`, which takes two lists interpreted as sets and returns the list representing the difference, that is, the first input set minus the second.

For example, `(difference '(a b c d) '(a c e))` returns `'(b d)`.

4. Implement a Scheme function called `symmetric-difference`. It takes as input two lists interpreted as sets and returns their symmetric difference.

For example, `(symmetric-difference '(a b c) '(b c d e))` returns `'(a d e)`.

5. Implement a Scheme function `stem`, a function that returns the list obtained by removing the last element from the argument list. Do not use the built-in function `reverse`.

6. Implement a Scheme function, `replicate`, that takes as arguments an atom and a list of atoms. The return list is the input list with each instance of the atom replicated. As a boundary condition, if the atom is not in the input list, the function returns that input list.

For example, `(replicate fi (fee fi fo fum fi))` returns `(fee fi fi fo fum fi fi)`.

7. Binary counter: Implement a Scheme function `next`, a function that returns the next binary number by incrementing the given binary number. For example,

- `(next '(0 0 1))` returns `'(0 1 0)`
- `(next '(1 1 0))` returns `'(1 1 1)`
- `(next '(1 1 1 1))` returns `'(0 0 0 0)`
- `(next '(1 0 1 1 1))` returns `'(1 1 0 0 0)`

and so forth.

*Hint:* It will be easier to implement the counter if the least significant bit is the list head instead of the last element. Call this simpler version `next1`. Then, you can use the `reverse` function that you learned in the Little Schemer to obtain `next` as

```
(define next
  (lambda (x)
    (reverse (next1 (reverse x)))))
```