

ModEDI

An Extendable Software Architecture for Examining
the Effects of Developmental Interactions on
Evolutionary Trajectories

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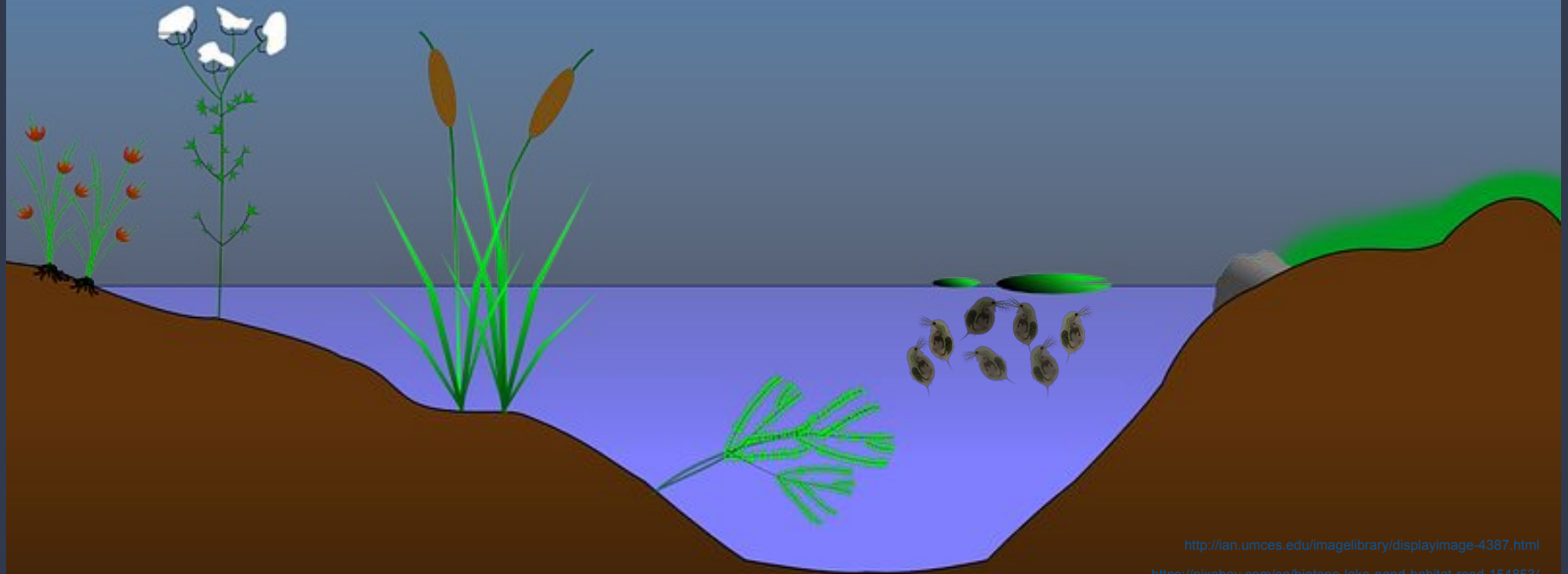
Background – *Quantitative Genetics*



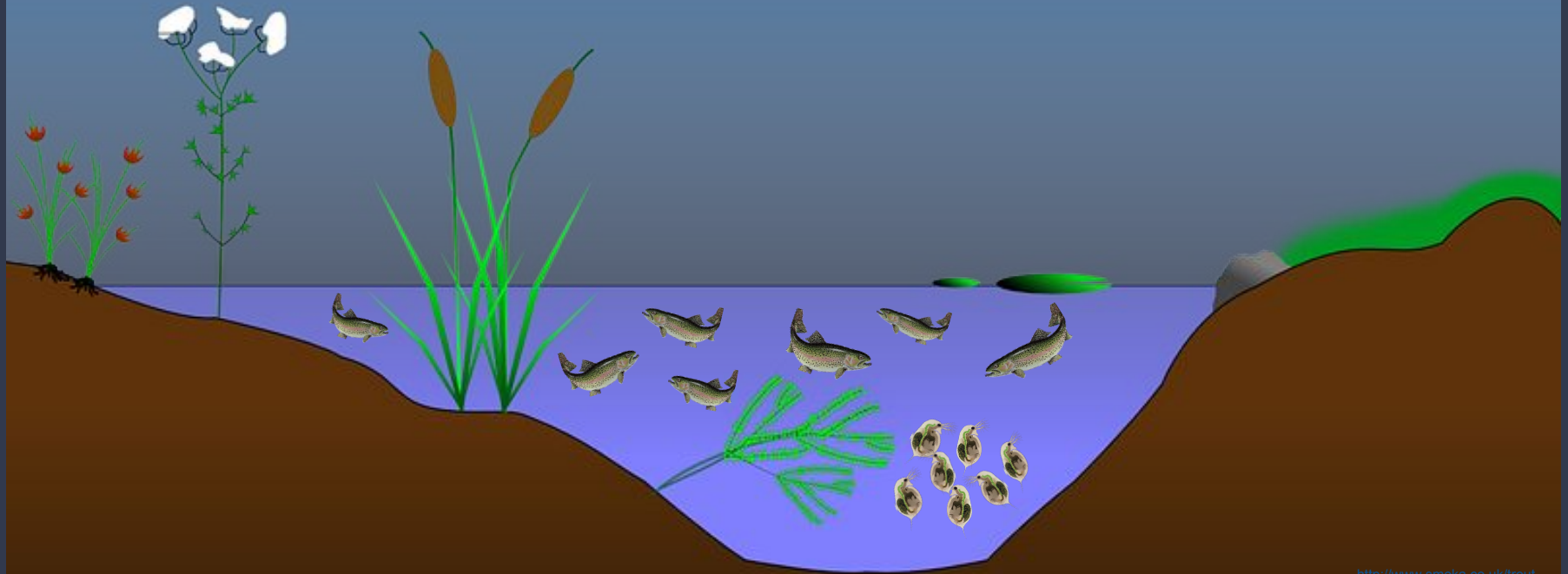
Models for *Daphnia*



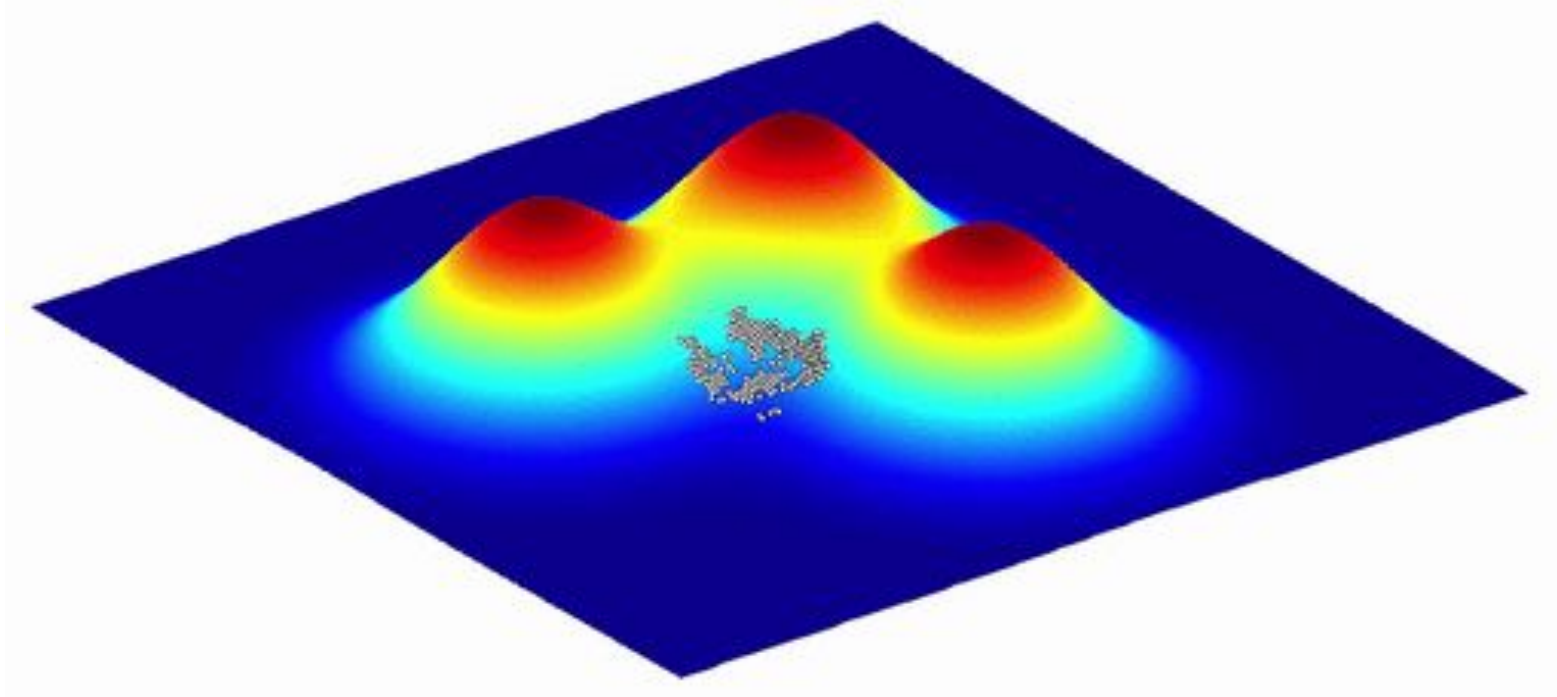
Nonlinear Developmental Interactions (NDI)



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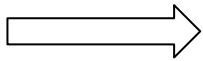


Central Concept – *Fitness Surface*

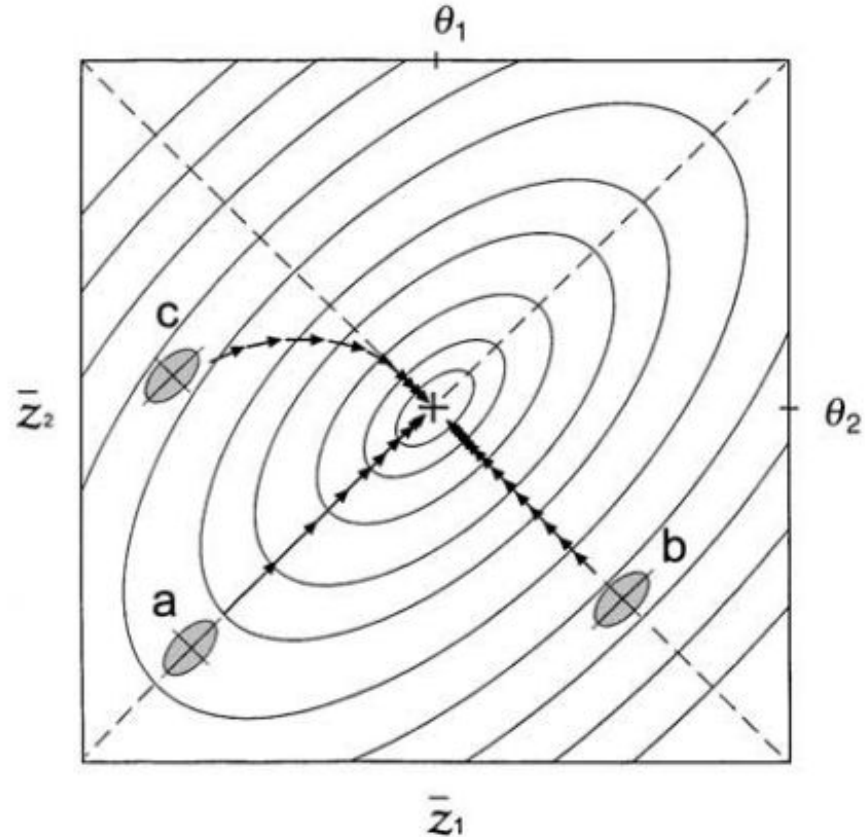
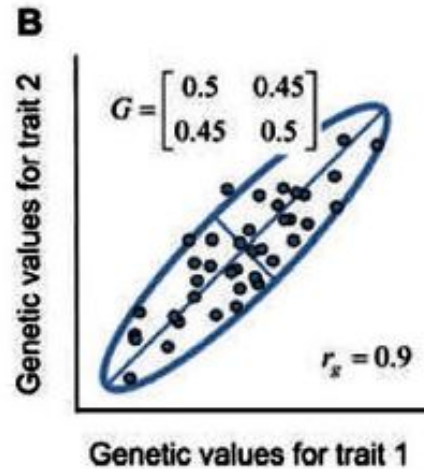
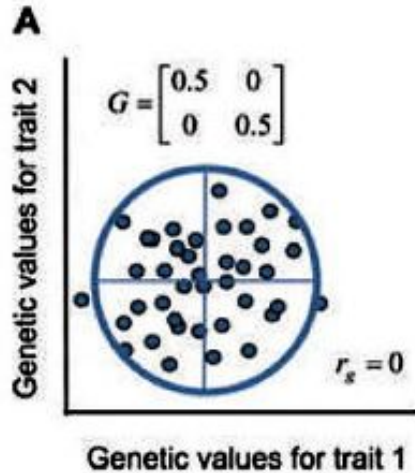


Central Concept – *G*Matrix

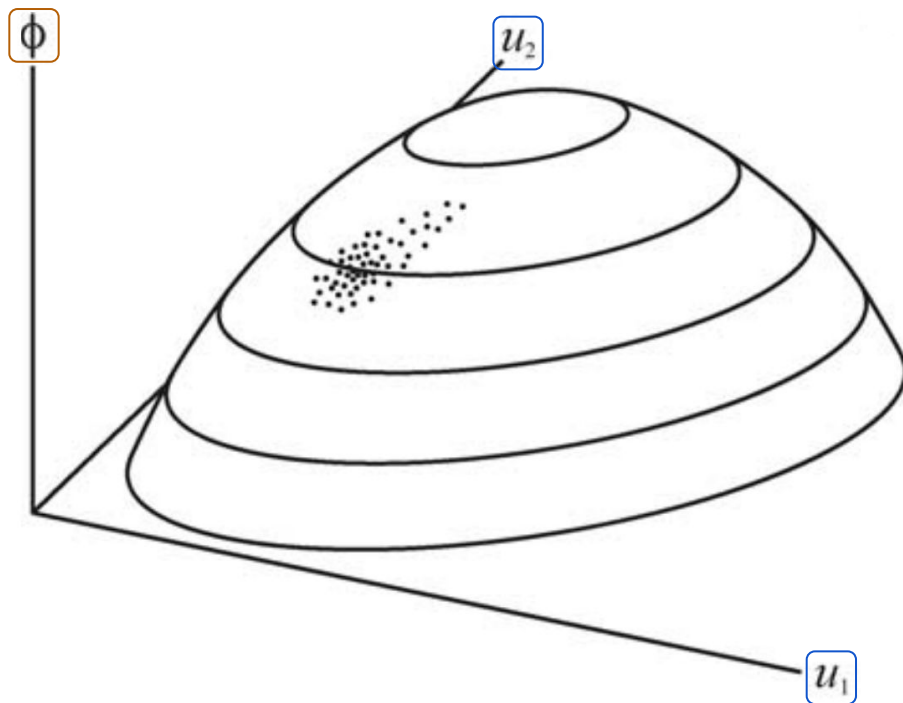
$$\Delta \mathbf{z} = \mathbf{G} \boldsymbol{\beta}$$



$$\begin{bmatrix} \Delta z_1 \\ \Delta z_2 \end{bmatrix} = \begin{bmatrix} G_{11} & G_{12} \\ G_{12} & G_{22} \end{bmatrix} \begin{bmatrix} \beta_1 \\ \beta_2 \end{bmatrix}$$

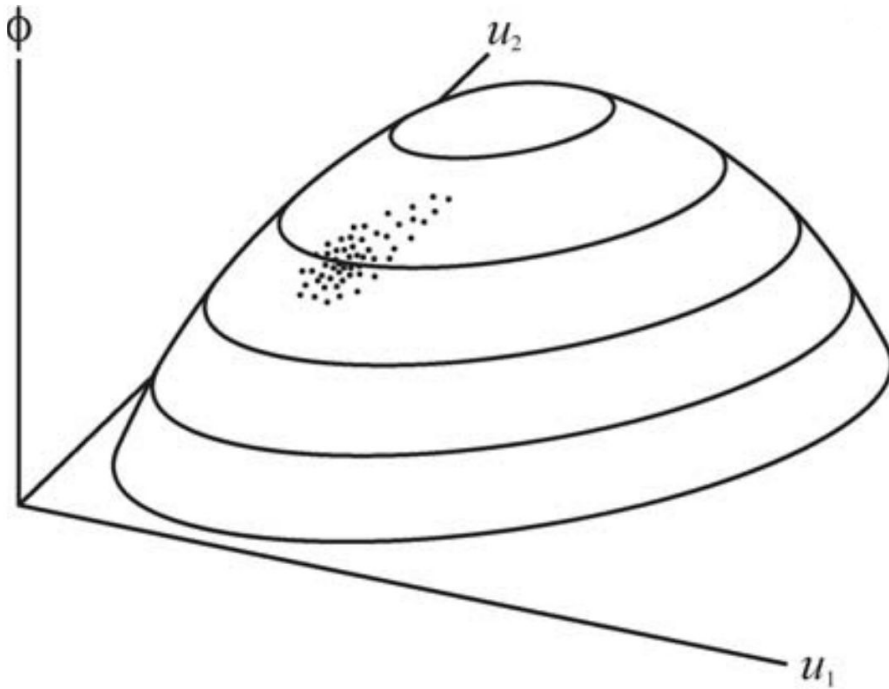


Central Concept – *Phenotype Surface*

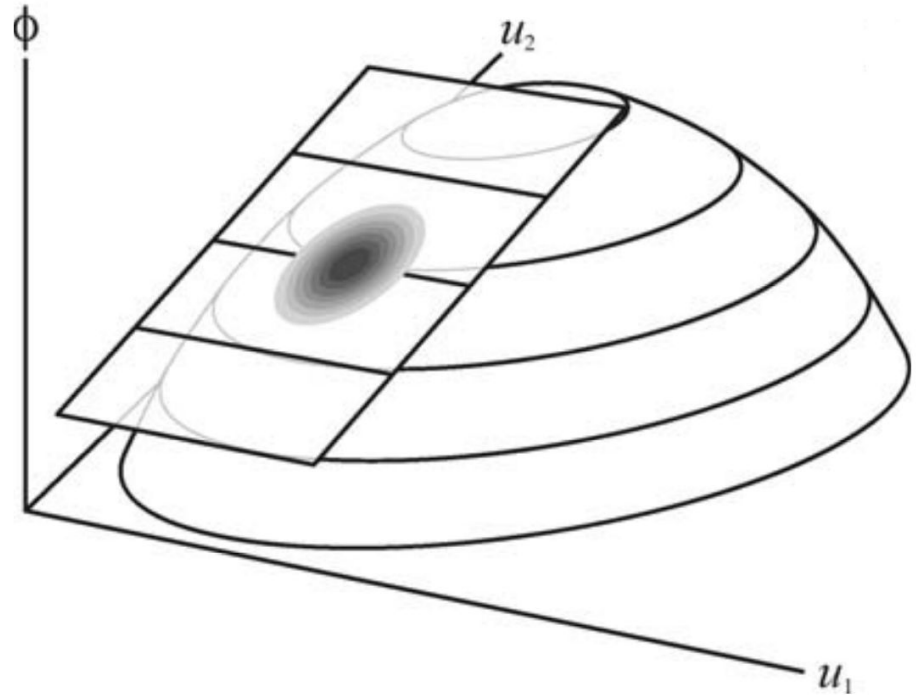


- ϕ represents a physical trait
- u_1 and u_2 represent underlying genetic factors
- Measures genetic variances
 - Additive
 - Dominance
 - Epistasis
 - Environmental

Phenotype Surface vs GMatrix



Phenotype Surface

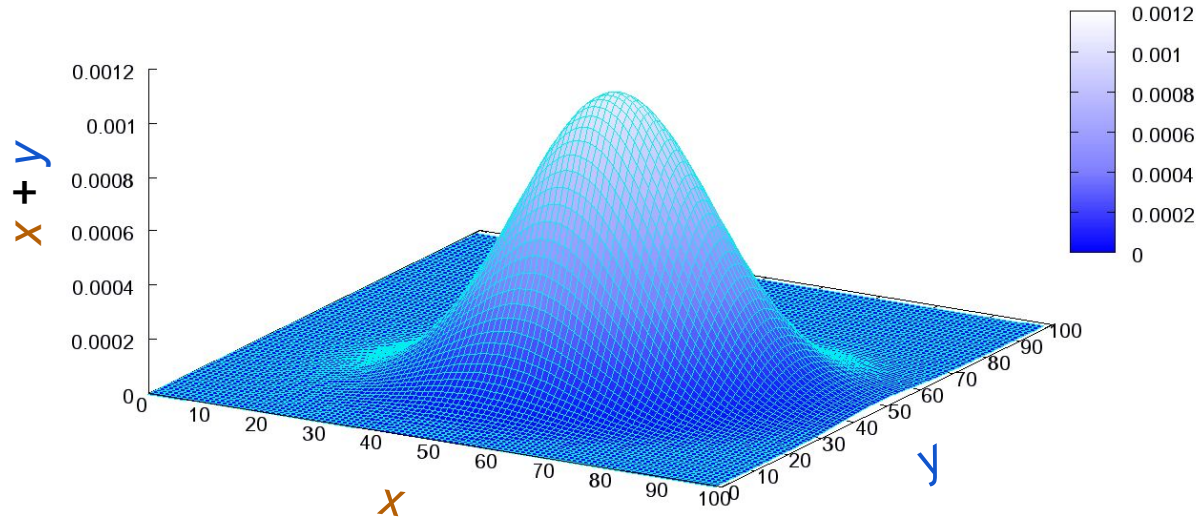


G-matrix Approximation

Surface Distribution – *Bivariate Normal*

- x and y are normally distributed values
- The sum of x and y form the bivariate normal distribution

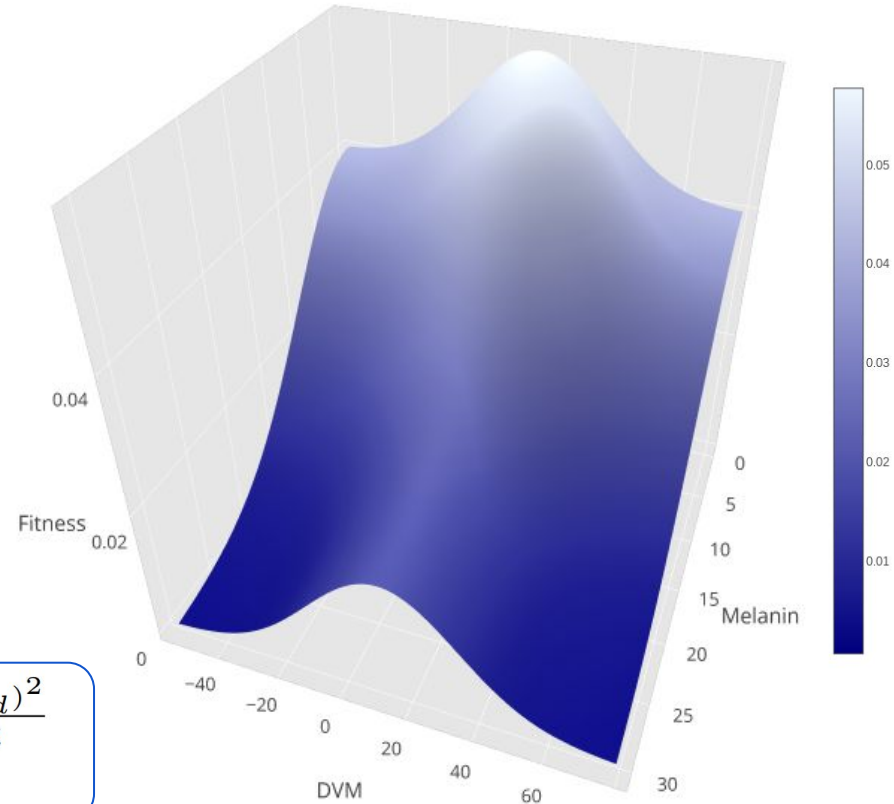
$$w = N(\langle x \rangle, \sigma_x) + N(\langle y \rangle, \sigma_y)$$



Surface Distribution – *Bivariate Normal*

- **Melanin** and **DVM** are normally distributed trait values
- The sum of **Melanin** and **DVM** form the bivariate normal distribution

$$w = \frac{1}{\sqrt{v_m}2\pi} e^{-\frac{(m-\omega_m)^2}{2v_m}} + \frac{1}{\sqrt{v_d}2\pi} e^{-\frac{(d-\omega_d)^2}{2v_d}}$$



Classic Model - *G-matrix*

- h^2 is the diagonal values of the heritability matrix
- \bar{w} is the mean population fitness
- σ_d and σ_m are the DVM (\bar{d}) and Melanin (\bar{m}) phenotypic variances

$$\boxed{\Delta \mathbf{z} = \mathbf{G} \boldsymbol{\beta}} \quad \longrightarrow \quad \boxed{\begin{bmatrix} \Delta z_1 \\ \Delta z_2 \end{bmatrix} = \begin{bmatrix} G_{11} & G_{12} \\ G_{12} & G_{22} \end{bmatrix} \begin{bmatrix} \beta_1 \\ \beta_2 \end{bmatrix}}$$

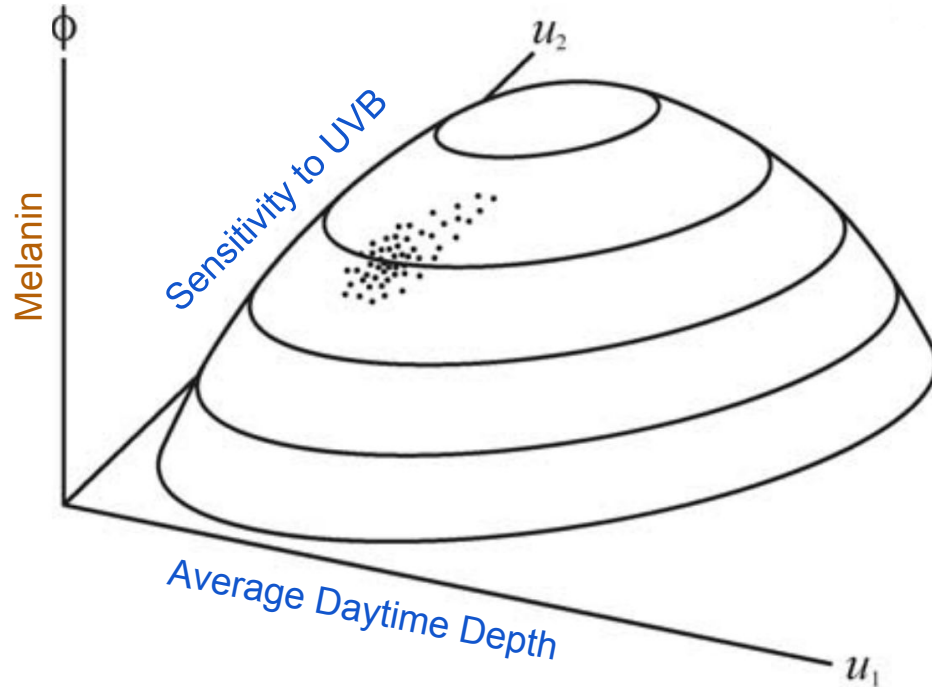
Melanin development:

$$\bar{m}_{t+1} = \bar{m}_t + h^2 \frac{1}{\bar{w}} \frac{\partial w}{\partial m} \sigma_m$$

DVM development:

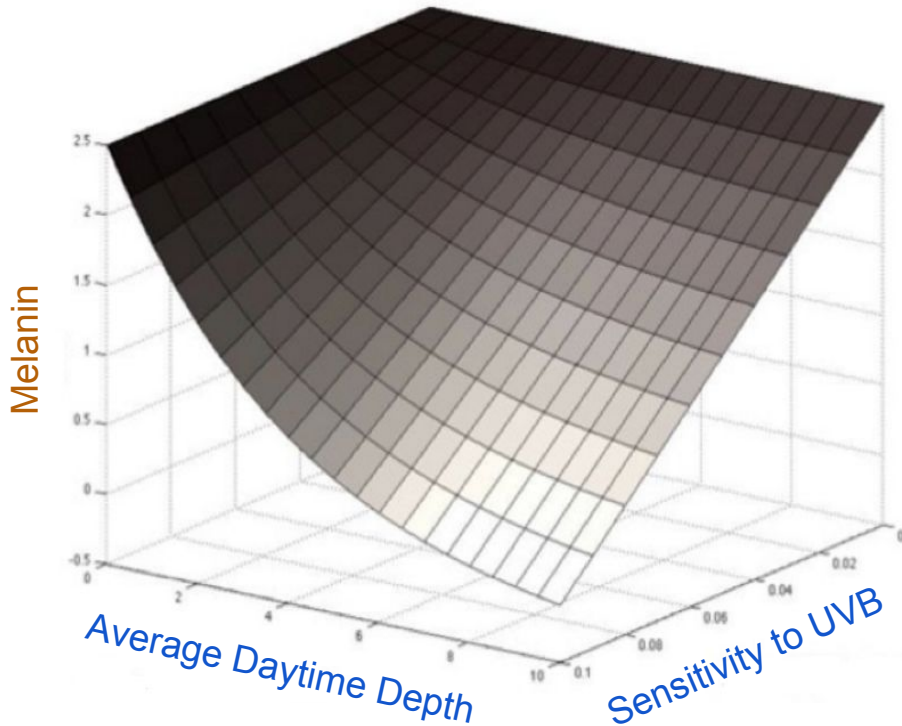
$$\bar{d}_{t+1} = \bar{d}_t + h^2 \frac{1}{\bar{w}} \frac{\partial w}{\partial d} \sigma_d$$

Tanning Model – *Phenotype Surface*



- ϕ represents a physical trait, **Melanin**
- u_1 and u_2 represent underlying genetic factors, **Average Daytime Depth** and **Sensitivity to UVB**

Tanning Model – *Phenotype Surface*



$$m = z + pa$$

- z is the concentration of melanin produced in response to UV light
- p is the slope of the reaction norm indicating sensitivity to UVB
- a is the change in UVB exposure

Tanning Model - *NDI*

- **d** is DVM, treated as a quantitative genetic trait

$$\boxed{\Delta \mathbf{z} = \mathbf{G}\boldsymbol{\beta}} \longrightarrow \boxed{\begin{bmatrix} \Delta z_1 \\ \Delta z_2 \end{bmatrix} = \begin{bmatrix} G_{11} & G_{12} \\ G_{12} & G_{22} \end{bmatrix} \begin{bmatrix} \beta_1 \\ \beta_2 \end{bmatrix}}$$

- **H** is the heritability matrix
- **U** represents the change in DVM, simplified
- **V** represents the change in Melanin, simplified

Melanin production:

$$m = z + pa$$

Development of genetic factors:

$$\begin{pmatrix} \bar{z} \\ \bar{p} \\ \bar{d} \end{pmatrix}_{t+1} = \begin{pmatrix} \bar{z} \\ \bar{p} \\ \bar{d} \end{pmatrix}_t + H \frac{1}{\bar{w}} \boxed{U} \boxed{V}$$

Daphnia Species Objects

- States represent phenotypic traits, **DVM** and **Melanin**
- Behaviours represent the phenotypic functions of the **Classic** and **Tanning** *Daphnia* models

Daphnia Blueprint



*Daphnia
melanica*

- **DVM**: int
- **Melanin**: int

+ setDVM
+ setMelanin

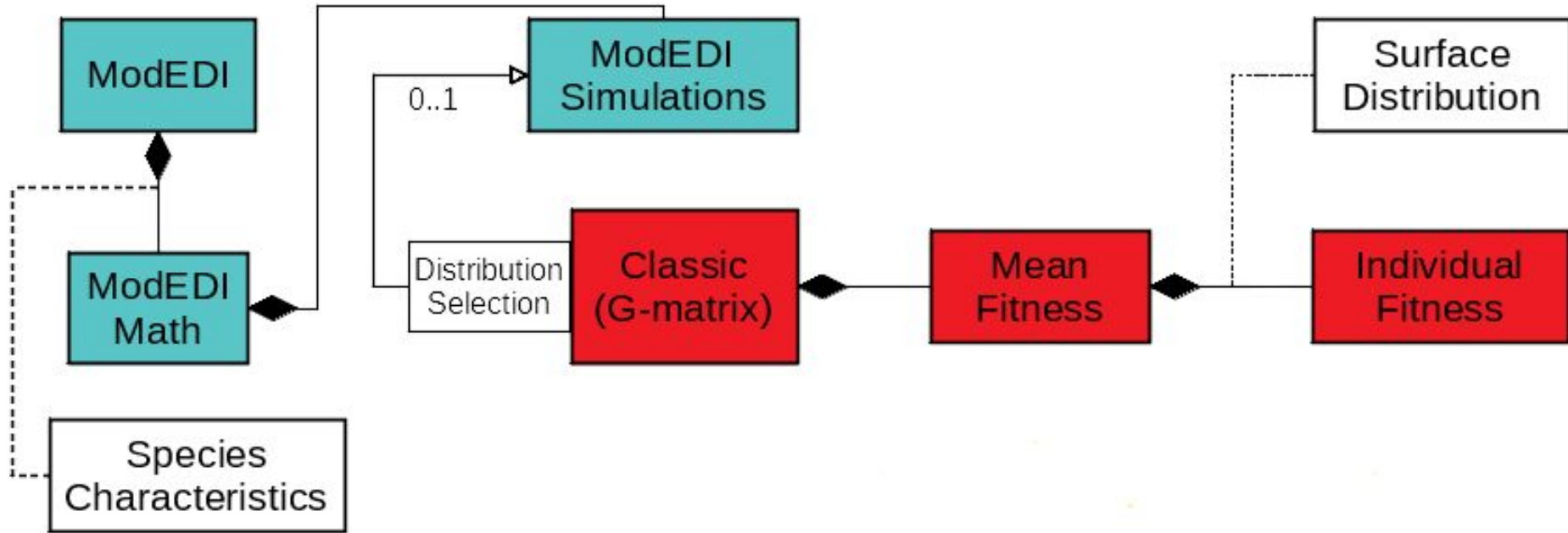
Daphnia Objects



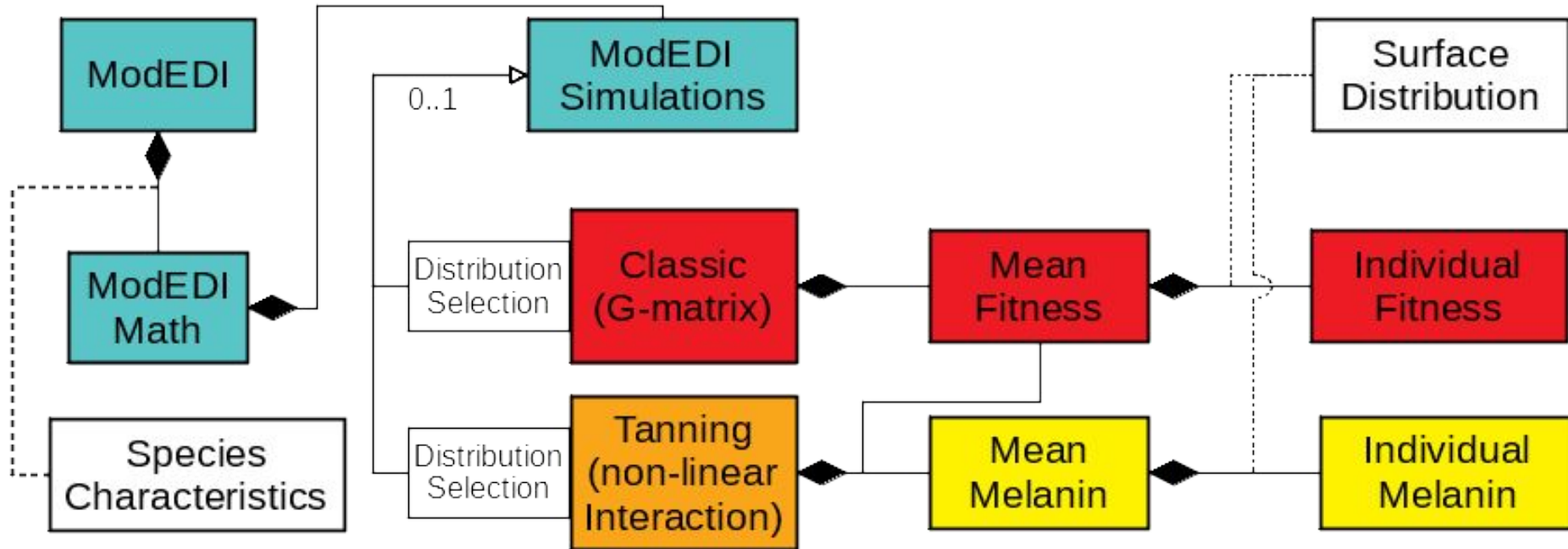
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https://www.researchgate.net/figure/51073279_fig5_Fig-5-Pigmented-zooplankton-Melanised-Daphnia-umbra-left-and-Eudiaptomus-graciloides

Software Architecture – *Classic Model*



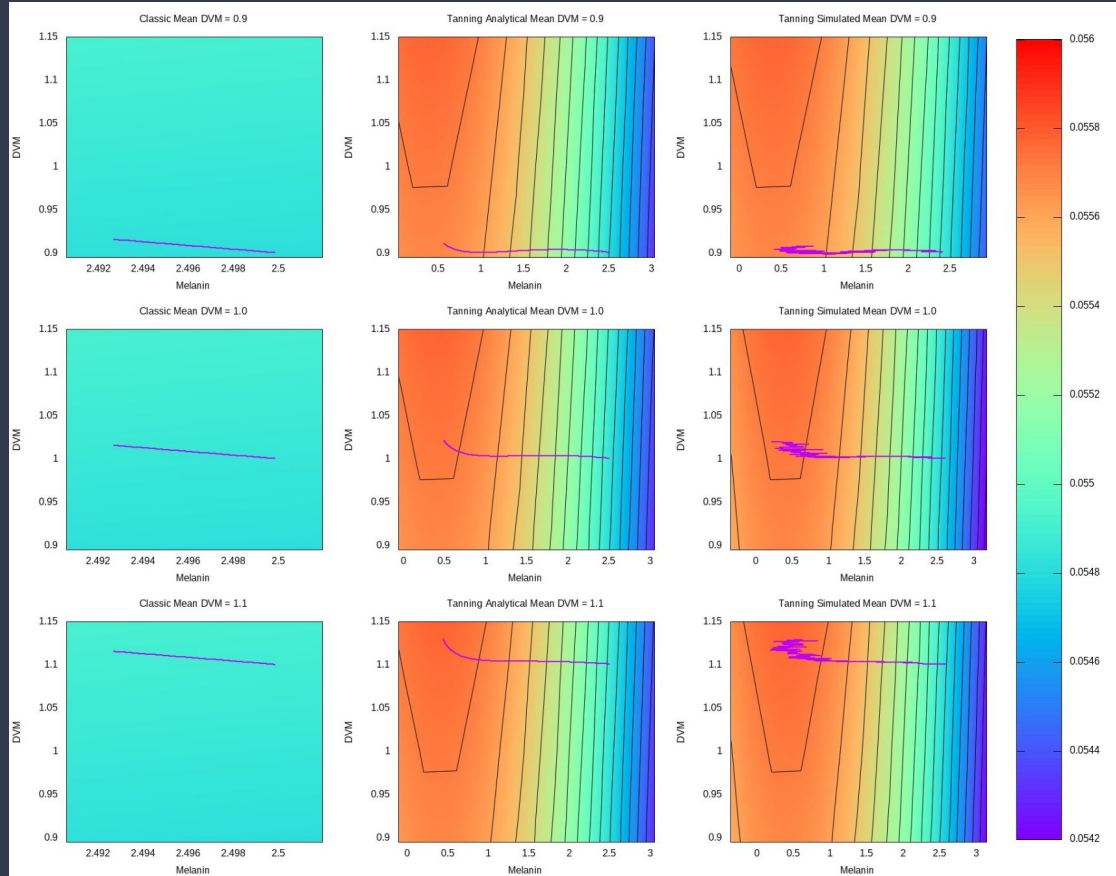
Software Architecture – *Tanning Model*



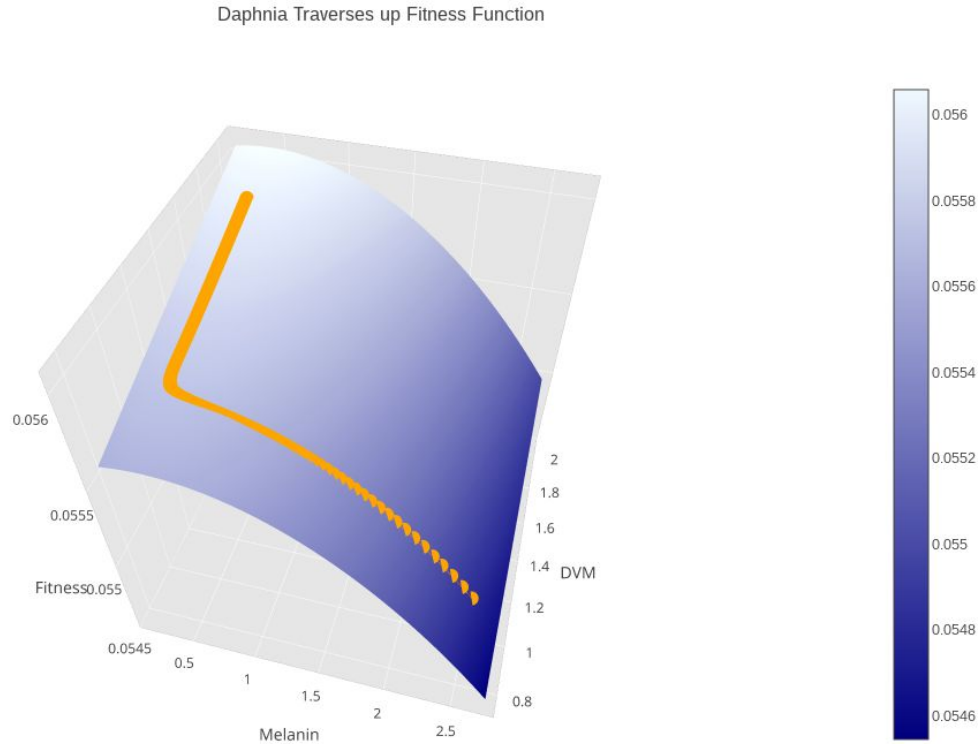
Mean DVM Parameter Sweep

Conclusions:

- Less fluctuation in trajectories
- Higher overall fitness
- Quicker to reach trait optima
- *Classic* model evolves more slowly than *Tanning*



Daphnia Case Study – Results



Future Work

- Increased generalization
 - Support any number of physical traits
 - Support any number of developmental factors for each trait
- Add support for other fitness and phenotype distributions
- Make available as a R package
- Update online user interface

Acknowledgements

- CWU Science Honors Research Program
- WWU College of the Sciences and Engineering