

Exercise 1.

$$1. \quad h^2 \leq 36205 < (h+1)^2$$

$h = ?$

$$h = \left(36205 + \frac{36205}{36205} \right) / 2 = \frac{36205}{2} = 18103$$

$$h = \left(18103 + \frac{36205}{18103} \right) / 2 = \frac{18104}{2} = 9052$$

$$h = \left(9052 + \frac{36205}{9052} \right) / 2 = \frac{9055}{2} = 4527$$

$$h = \left(4527 + \frac{36205}{4527} \right) / 2 = \frac{4534}{2} = 2267$$

$$h = \left(2267 + \frac{36205}{2267} \right) / 2 = \frac{2282}{2} = 1141$$

$$h = \left(1141 + \frac{36205}{1141} \right) / 2 = \frac{1172}{2} = 586$$

$$h = \left(586 + \frac{36205}{586} \right) / 2 = \frac{647}{2} = 323$$

$$h = \left(323 + \frac{36205}{323} \right) / 2 = \frac{435}{2} = 217$$

$$h = \left(217 + \frac{36205}{217} \right) / 2 = \frac{383}{2} = 191$$

$$h = \left(191 + \frac{36205}{191} \right) / 2 = \frac{380}{2} = 190$$

$$h = \left(190 + \frac{36205}{190} \right) / 2 = \frac{380}{2} = 190$$

Answer: $h = 190$.

$$2. \quad 2002 = 1001 \cdot 2 = 143 \cdot 7 \cdot 2 = 13 \cdot 11 \cdot 7 \cdot 2$$

Answer: $2002 = 2 \cdot 7 \cdot 11 \cdot 13$

$$3. \quad 59x + 30y = 2002$$

$$59 = 30 \cdot 1 + \textcircled{29} \uparrow$$

$$30 = 29 \cdot 1 + \textcircled{1}$$

$$29 = 1 \cdot 29$$

$$59x_0 + 30y_0 = 1$$

$$1 = 30 - 29$$

$$29 = 59 - 30$$

$$1 = 30 - (59 - 30)$$

$$1 = 59 \cdot (-1) + 2 \cdot 30$$

$$x_0 = -1, \quad y_0 = 2$$

$$59 \cdot 2002x_0 + 30 \cdot 2002y_0 = 2002$$

$$59 \cdot (2002x_0 + 30x) + 30 \cdot (2002y_0 - 59x) = 2002$$

$$\text{Answer: } x = -2002 + 30x, \quad y = 4004 - 59x$$

$$4.2. \quad 3x + 112_7 = 346_7$$

$$I. \quad \overset{2}{1}\overset{1}{1}\overset{0}{2}_7 = 49 + 7 + 2 = 58_{10} \quad ; \quad \overset{2}{3}\overset{1}{4}\overset{0}{6}_7 = 147 + 28 + 6 = 181_{10}$$

$$3x + 58_{10} = 181_{10}$$

$$3x = 123$$

$$x = 41_{10}$$

$$x = 56_7$$

41	7	
35	5	7
60	0	0
	5	

$$\begin{array}{r} \text{II.} \quad - \quad 346_7 \\ \quad \quad 112_7 \\ \hline \quad \quad 234_7 \end{array}$$

$$3X = 234_7$$

$$\begin{array}{r} - \quad 234 \mid 3 \\ \quad 21 \mid 56_7 \\ \hline \quad \quad 24 \\ \quad \quad 24 \\ \hline \quad \quad 0 \end{array}$$

$$X = 56_7$$