CIND820 Initial Coding

November 17, 2020

```
[5]: import os
     import warnings
     warnings.filterwarnings('ignore')
     import pandas as pd
     import numpy as np
     import matplotlib.pyplot as plt
     plt.style.use('fivethirtyeight')
     from pylab import rcParams
     rcParams['figure.figsize'] = 10, 6
     from datetime import datetime
     from statsmodels.tsa.stattools import adfuller
     from statsmodels.tsa.seasonal import seasonal_decompose
     from statsmodels.tsa.arima_model import ARIMA
     from sklearn.metrics import mean squared error, mean_absolute_error
     import math
     from statsmodels.tsa.stattools import acf, pacf
```

[4]: pip install pmdarima

```
Collecting pmdarima
```

```
Using cached pmdarima-1.7.1-cp37-cp37m-manylinux1_x86_64.whl (1.5 MB)
Requirement already satisfied: scikit-learn>=0.22 in
/opt/conda/lib/python3.7/site-packages (from pmdarima) (0.22.2.post1)
Requirement already satisfied: numpy>=1.17.3 in /opt/conda/lib/python3.7/site-
packages (from pmdarima) (1.18.4)
Requirement already satisfied: setuptools<50.0.0 in
/opt/conda/lib/python3.7/site-packages (from pmdarima) (46.1.3.post20200325)
Requirement already satisfied: pandas>=0.19 in /opt/conda/lib/python3.7/site-
packages (from pmdarima) (1.0.3)
Requirement already satisfied: urllib3 in /opt/conda/lib/python3.7/site-packages
(from pmdarima) (1.25.9)
Requirement already satisfied: scipy>=1.3.2 in /opt/conda/lib/python3.7/site-
packages (from pmdarima) (1.4.1)
Collecting Cython<0.29.18,>=0.29
 Using cached Cython-0.29.17-cp37-cp37m-manylinux1_x86_64.whl (2.1 MB)
Requirement already satisfied: statsmodels<0.12,>=0.11 in
/opt/conda/lib/python3.7/site-packages (from pmdarima) (0.11.1)
Requirement already satisfied: joblib>=0.11 in /opt/conda/lib/python3.7/site-
```

```
packages (from pmdarima) (0.15.1)
     Requirement already satisfied: pytz>=2017.2 in /opt/conda/lib/python3.7/site-
     packages (from pandas>=0.19->pmdarima) (2020.1)
     Requirement already satisfied: python-dateutil>=2.6.1 in
     /opt/conda/lib/python3.7/site-packages (from pandas>=0.19->pmdarima) (2.8.1)
     Requirement already satisfied: patsy>=0.5 in /opt/conda/lib/python3.7/site-
     packages (from statsmodels<0.12,>=0.11->pmdarima) (0.5.1)
     Requirement already satisfied: six>=1.5 in /opt/conda/lib/python3.7/site-
     packages (from python-dateutil>=2.6.1->pandas>=0.19->pmdarima) (1.14.0)
     Installing collected packages: Cython, pmdarima
       Attempting uninstall: Cython
         Found existing installation: Cython 0.29.19
         Uninstalling Cython-0.29.19:
           Successfully uninstalled Cython-0.29.19
     Successfully installed Cython-0.29.17 pmdarima-1.7.1
     Note: you may need to restart the kernel to use updated packages.
 [6]: from pmdarima.arima import auto_arima
 [7]: #import NASDAQ data
      df=pd.read_csv("IXIC_v1.csv", sep=",")
 [8]: #understand data format and clean up data
      from datetime import datetime
      con=df['Date']
      df['Date'] = pd.to_datetime(df['Date'])
      df.set_index('Date', inplace=True)
      #check datatype of index
      df.index
 [8]: DatetimeIndex(['2010-01-04', '2010-01-05', '2010-01-06', '2010-01-07',
                     '2010-01-08', '2010-01-11', '2010-01-12', '2010-01-13',
                     '2010-01-14', '2010-01-15',
                     '2020-09-17', '2020-09-18', '2020-09-21', '2020-09-22',
                     '2020-09-23', '2020-09-24', '2020-09-25', '2020-09-28',
                     '2020-09-29', '2020-09-30'],
                    dtype='datetime64[ns]', name='Date', length=2705, freq=None)
 [9]: df['year'] = df.index.year
      df['month'] = df.index.month
      df['day'] = df.index.day
[10]: df.sample(5, random_state=0)
[10]:
                        Close year month day
     Date
```

```
      2010-05-17
      2354.229980
      2010
      5
      17

      2018-02-01
      7385.859863
      2018
      2
      1

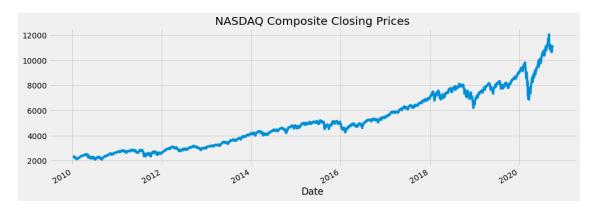
      2013-07-29
      3599.139893
      2013
      7
      29

      2016-11-08
      5193.490234
      2016
      11
      8

      2014-06-13
      4310.649902
      2014
      6
      13
```

```
[11]: #plot NASDAQ trend
temp=df.groupby(['Date'])['Close'].mean()
temp.plot(figsize=(15,5), title= 'NASDAQ Composite Closing Prices', fontsize=14)
```

[11]: <matplotlib.axes._subplots.AxesSubplot at 0x7f9f03551210>

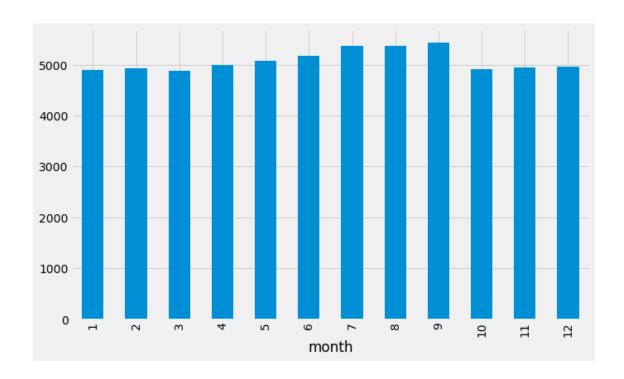


[12]: df.groupby('month')['Close'].mean().plot.bar()

#on average, september has the highest average price compares to the other

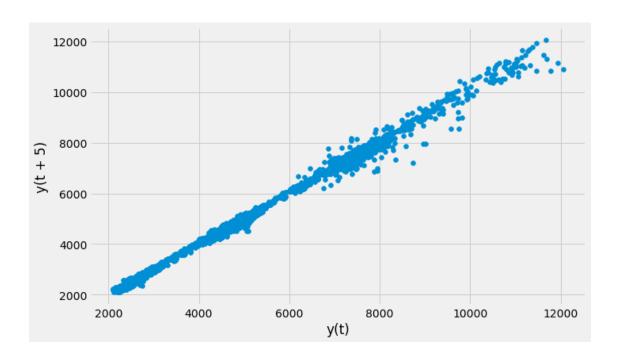
→months.

[12]: <matplotlib.axes._subplots.AxesSubplot at 0x7f9f034c8b50>



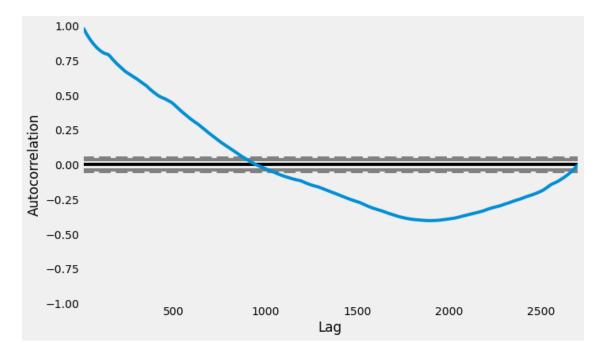
[13]: #lag plot from pandas.plotting import lag_plot lag_plot(df['Close'],lag=5) #Graph shows a linear pattern. Implies data points are non random and suggests → that an autoregressive model might be appropriate.

[13]: <matplotlib.axes._subplots.AxesSubplot at 0x7f9f0333a690>



[14]: from pandas.plotting import autocorrelation_plot autocorrelation_plot(df['Close'])
#there is high level of correlation

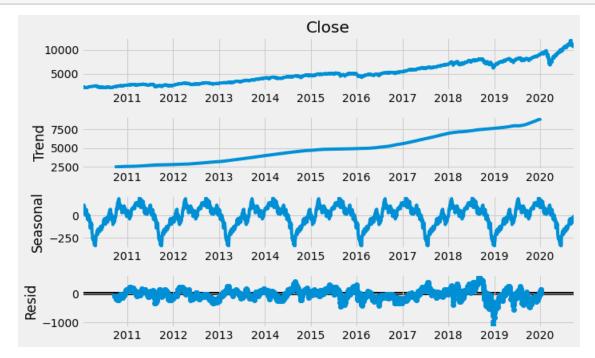
[14]: <matplotlib.axes._subplots.AxesSubplot at 0x7f9f0325c710>



```
[15]: #data is not stationary based on high p value
from statsmodels.tsa.stattools import adfuller
result = adfuller(df.Close.dropna())
print(f"ADF Statstic: {result[0]}")
print(f"p-value:{result[1]}")
```

ADF Statstic: 1.4430465972942679 p-value:0.9973011850493003

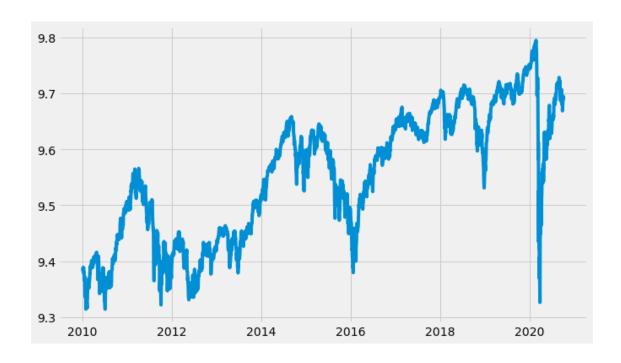
```
[16]: #decompose data
import statsmodels.api as sm
res = sm.tsa.seasonal_decompose(df['Close'],model= 'addictive',period = 365)
resplot = res.plot()
#data shows upward trend and presents seasonlity
```



```
[97]: def plot_df(df,x,y,title= "", xlabel = "Date", ylabel='Value',dpi=100):
    plt.plot(x,y)
    plt.show()
```

```
[98]: #apply log transformation to stablize data plt.plot(df.apply(np.log)['Close'])
```

[98]: [<matplotlib.lines.Line2D at 0x7f9e5808b950>]

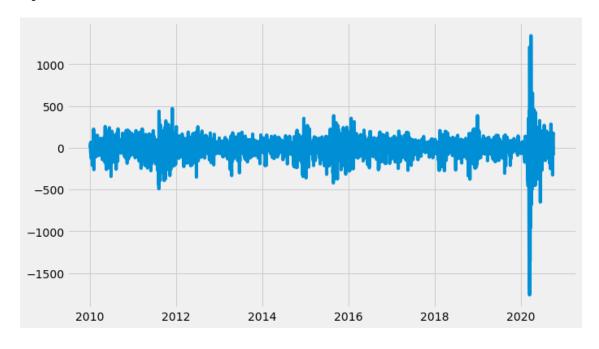


[96]: #To covert data into stationary dataset, first differencing has to be applied.

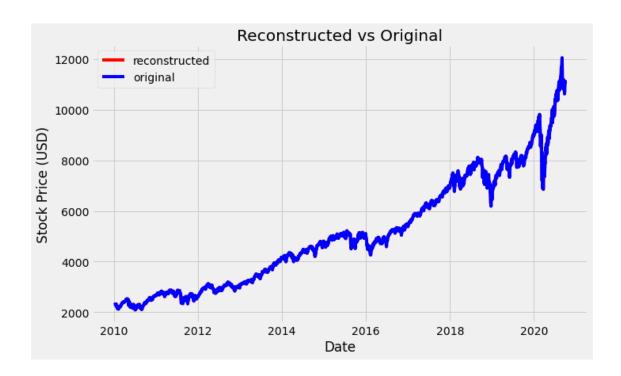
→With first differencing, empty field needs to be filled as 0.

plt.plot(df['Close'].diff(1).fillna(0))

[96]: [<matplotlib.lines.Line2D at 0x7f9e58131f90>]



```
[20]: #confirm stationarity
      from statsmodels.tsa.stattools import adfuller
      result = adfuller(np.log(df['Close']).diff(1).fillna(0))
      print(f"ADF Statstic: {result[0]}")
      print(f"p-value:{result[1]}")
     ADF Statstic: -11.770291597674845
     p-value:1.0940406662618215e-21
[21]: df_st= df.diff(1).fillna(0)
[22]: #understand the structure of the stationary dataset
      df_st.head()
[22]:
                     Close year month day
     Date
      2010-01-04 0.000000
                             0.0
                                    0.0 0.0
      2010-01-05 0.290039
                             0.0
                                    0.0 1.0
      2010-01-06 -7.619873
                             0.0
                                    0.0 1.0
      2010-01-07 -1.040039
                             0.0
                                    0.0 1.0
      2010-01-08 17.119873
                             0.0
                                    0.0 1.0
[23]: #With transformation to maintain stationarity, we need to be model back to the
      →original dataset in order to predict stock price.
      df reconstruct=df st.copy()
      df_resconstruct=df_reconstruct.cumsum()
[24]: df_reconstruct=df_st.copy()
      df_reconstruct.iloc[0,:]=df.iloc[0,:]
      df_reconstruct = df_reconstruct.cumsum()
[25]: plt.plot(df.index, df_reconstruct['Close'], 'r-', label='reconstructed')
      plt.plot(df.index, df['Close'], 'b-', label = 'original')
      plt.xlabel('Date'); plt.ylabel('Stock Price (USD)')
      plt.title('Reconstructed vs Original')
      plt.legend();
      #plot confirms the same pattern of data
```



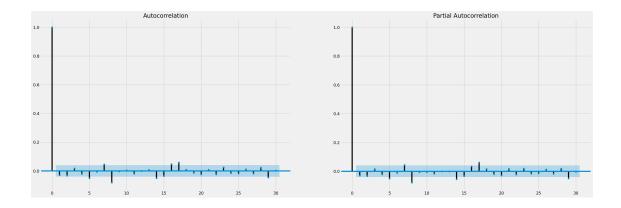
```
[26]: #define data
class TimeSeriesData():
    def __init__(self, df):
        self.data = df
        self.stationary = self.stationarize(df)
        self.reconstructed = self.reconstruct(self.stationary, self.data)

def reconstruct(self, st, org):
        x = st.copy()
        x.iloc[0,:] = org.iloc[0,:]
        return x.cumsum()

def stationarize(self, data):
        return data.diff(1).fillna(0)
```

```
[27]: #split dataset
x_train = TimeSeriesData(df[:int((len(df)*0.9))])
x_valid = TimeSeriesData(df[int((len(df)*0.9)):])
```

```
[28]: #plot ACF and PACF for the stationary dataset
from statsmodels.graphics.tsaplots import plot_acf, plot_pacf
fig, axes = plt.subplots(1,2,figsize=(30,10), dpi= 100)
plot_acf(x_train.stationary['Close'].values.tolist(), lags=30, ax=axes[0]);
plot_pacf(x_train.stationary['Close'].values.tolist(), lags=30, ax=axes[1]);
```



```
[29]: #using auto_arima to aquire p and q value with min AIC.

from pmdarima import auto_arima

model = auto_arima(x_train.data['Close'], trace=True, error_action='ignore',

suppress_warnings=True)

model.fit(x_train.data['Close'])
```

```
Performing stepwise search to minimize aic
```

```
ARIMA(2,1,2)(0,0,0)[0] intercept
                                   : AIC=26066.202, Time=2.11 sec
ARIMA(0,1,0)(0,0,0)[0] intercept
                                   : AIC=26076.884, Time=0.06 sec
ARIMA(1,1,0)(0,0,0)[0] intercept
                                   : AIC=26076.691, Time=0.12 sec
                                   : AIC=26076.549, Time=0.17 sec
ARIMA(0,1,1)(0,0,0)[0] intercept
ARIMA(0,1,0)(0,0,0)[0]
                                   : AIC=26079.882, Time=0.03 sec
ARIMA(1,1,2)(0,0,0)[0] intercept
                                   : AIC=26075.487, Time=2.17 sec
ARIMA(2,1,1)(0,0,0)[0] intercept
                                   : AIC=26075.648, Time=1.86 sec
                                   : AIC=26068.264, Time=3.18 sec
ARIMA(3,1,2)(0,0,0)[0] intercept
ARIMA(2,1,3)(0,0,0)[0] intercept
                                   : AIC=26068.512, Time=2.98 sec
                                   : AIC=26070.891, Time=1.45 sec
ARIMA(1,1,1)(0,0,0)[0] intercept
ARIMA(1,1,3)(0,0,0)[0] intercept
                                   : AIC=26079.396, Time=1.73 sec
                                   : AIC=26079.243, Time=1.46 sec
ARIMA(3,1,1)(0,0,0)[0] intercept
ARIMA(3,1,3)(0,0,0)[0] intercept
                                   : AIC=26065.626, Time=4.68 sec
ARIMA(4,1,3)(0,0,0)[0] intercept
                                   : AIC=26068.108, Time=4.90 sec
                                   : AIC=26065.348, Time=6.39 sec
ARIMA(3,1,4)(0,0,0)[0] intercept
ARIMA(2,1,4)(0,0,0)[0] intercept
                                   : AIC=26067.212, Time=4.68 sec
                                   : AIC=26066.196, Time=10.05 sec
ARIMA(4,1,4)(0,0,0)[0] intercept
ARIMA(3,1,5)(0,0,0)[0] intercept
                                   : AIC=26065.247, Time=14.73 sec
                                   : AIC=26067.822, Time=14.77 sec
ARIMA(2,1,5)(0,0,0)[0] intercept
ARIMA(4,1,5)(0,0,0)[0] intercept
                                   : AIC=26068.541, Time=16.31 sec
ARIMA(3,1,5)(0,0,0)[0]
                                   : AIC=26070.298, Time=3.68 sec
```

Best model: ARIMA(3,1,5)(0,0,0)[0] intercept Total fit time: 97.554 seconds

[29]: ARIMA(maxiter=50, method='lbfgs', order=(3, 1, 5), out_of_sample_size=0, scoring='mse', scoring_args={}, seasonal_order=(0, 0, 0, 0),

start_params=None, suppress_warnings=True, trend=None,
with_intercept=True)

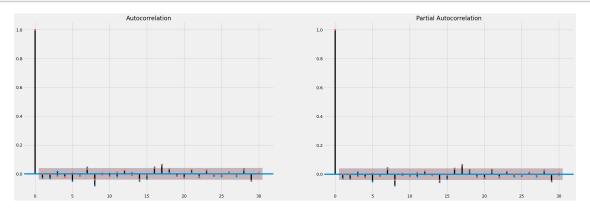
```
[30]: model_arima = ARIMA(x_train.data['Close'].values, order=(3,1,5))
[31]: result_arima = model_arima.fit(disp=-1)
[32]: print(result_arima.summary())
                                ARIMA Model Results
     Dep. Variable:
                                     D.y
                                           No. Observations:
                                                                           2433
     Model:
                          ARIMA(3, 1, 5)
                                          Log Likelihood
                                                                     -13022.009
     Method:
                                 css-mle
                                          S.D. of innovations
                                                                         51.074
     Date:
                        Mon, 16 Nov 2020
                                                                      26064.018
                                          AIC
                                17:52:43
     Time:
                                          BIC
                                                                      26121.986
     Sample:
                                       1
                                           HQIC
                                                                      26085.092
                     coef
                            std err
                                                   P>|z|
                                                              [0.025
                                                                         0.975
     const
                   2.3632
                              0.574
                                         4.119
                                                   0.000
                                                               1.239
                                                                          3.488
                                                   0.002
     ar.L1.D.y
                   0.2905
                              0.093
                                         3.125
                                                               0.108
                                                                          0.473
     ar.L2.D.y
                  -0.2264
                              0.079
                                       -2.873
                                                   0.004
                                                              -0.381
                                                                         -0.072
                                       12.920
     ar.L3.D.y
                              0.065
                                                   0.000
                  0.8377
                                                              0.711
                                                                          0.965
    ma.L1.D.y
                  -0.3212
                              0.095
                                       -3.377
                                                   0.001
                                                              -0.508
                                                                         -0.135
    ma.L2.D.y
                  0.2058
                              0.084
                                        2.462
                                                   0.014
                                                              0.042
                                                                          0.370
     ma.L3.D.y
                                       -11.125
                  -0.8151
                              0.073
                                                   0.000
                                                              -0.959
                                                                         -0.671
     ma.L4.D.y
                  0.0069
                              0.027
                                        0.254
                                                   0.799
                                                              -0.046
                                                                          0.060
     ma.L5.D.y
                  -0.0224
                              0.024
                                        -0.948
                                                   0.343
                                                              -0.069
                                                                          0.024
                                       Roots
     ______
                      Real
                                   Imaginary
                                                      Modulus
                                                                     Frequency
     AR.1
                    1.0402
                                    -0.0000j
                                                       1.0402
                                                                       -0.0000
     AR.2
                   -0.3849
                                    -0.9997j
                                                       1.0713
                                                                       -0.3085
     AR.3
                  -0.3849
                                    +0.9997j
                                                       1.0713
                                                                        0.3085
    MA.1
                                    -0.0000j
                   1.0216
                                                       1.0216
                                                                       -0.0000
    MA.2
                   -0.4009
                                    -1.0266j
                                                       1.1021
                                                                       -0.3092
    MA.3
                   -0.4009
                                    +1.0266j
                                                       1.1021
                                                                        0.3092
    MA.4
                   0.0430
                                    -5.9919j
                                                       5.9921
                                                                       -0.2489
     MA.5
                    0.0430
                                    +5.9919j
                                                       5.9921
                                                                        0.2489
```

[33]: #understand residual

residuals = pd.DataFrame(result_arima.resid)

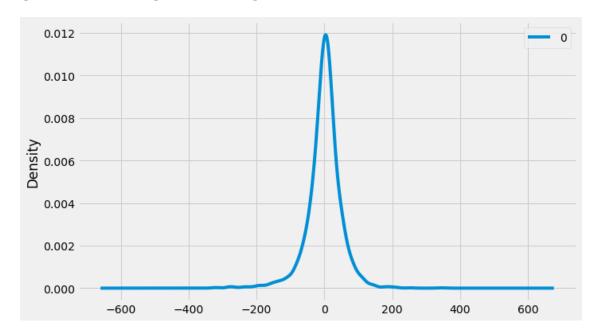
[34]: plot_acf(residuals, lags=30, ax=axes[0]) plot_pacf(residuals, lags=30, ax=axes[1])

[34]:

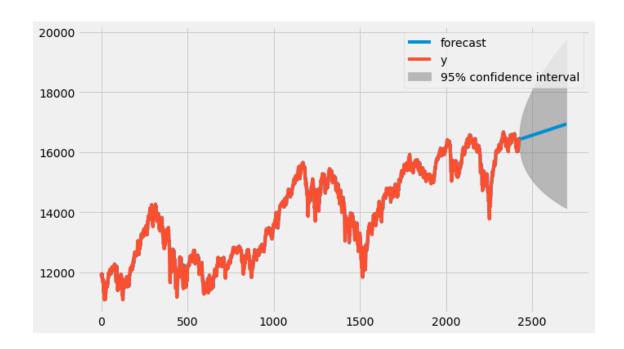


[35]: residuals.plot(kind='kde')

[35]: <matplotlib.axes._subplots.AxesSubplot at 0x7f9effa0b3d0>



[122]: result_arima.plot_predict(1,2700);



```
[81]: prediction = result_arima.predict(len(df)-208,len(df)-1)
      def rmse(validation, prediction):
          error = validation - prediction
          return np.sqrt(np.mean(error**2))
[82]: from statsmodels.tools.eval_measures import rmse
      #RMSE for ARIMA Model
      err_LSTM = rmse(x_valid.data['Close'], np.append(x_train.data.iloc[-1,:
      →]['Close'], prediction).cumsum()[1:])
      print('RMSE with LSTM', err_LSTM)
     RMSE with LSTM 1361.2487894244925
 []:
 []: #same analysis for TSX price
[83]: #upload TSX price
      df=pd.read_csv("GSPTSE_v1.csv", sep=",")
[84]: #understand the data and covert date format
      from datetime import datetime
      con=df['Date']
      df['Date']=pd.to_datetime(df['Date'])
      df.set_index('Date', inplace=True)
      #check datatype of index
      df.index
```

```
[85]: df['year'] = df.index.year
df['month'] = df.index.month
df['day'] = df.index.day
```

```
[86]: df.sample(5, random_state=0)
```

```
[86]:
                       Close
                            year month day
     Date
     2012-09-06 12139.70020
                             2012
                                            6
     2016-03-04 13212.50000 2016
                                       3
                                            4
     2014-09-23 15125.70020 2014
                                       9
                                           23
     2017-05-31 15349.90039 2017
                                       5
                                           31
     2016-02-16 12555.00000 2016
                                       2
                                           16
```

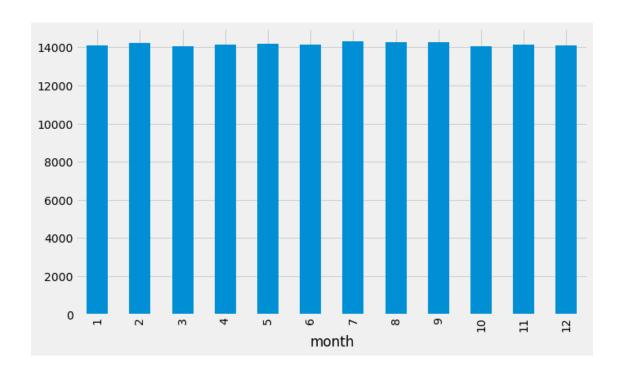
```
[88]: #plot TSX trend
temp=df.groupby(['Date'])['Close'].mean()
temp.plot(figsize=(15,5), title= 'TSX Composite Closing Prices', fontsize=14)
```

[88]: <matplotlib.axes._subplots.AxesSubplot at 0x7f9e58d0f950>



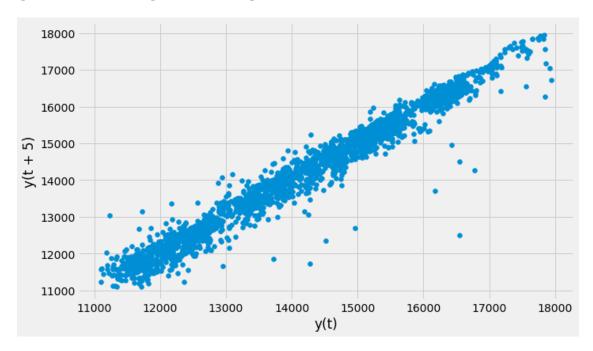
```
[89]: df.groupby('month')['Close'].mean().plot.bar()
```

[89]: <matplotlib.axes._subplots.AxesSubplot at 0x7f9e903a3410>



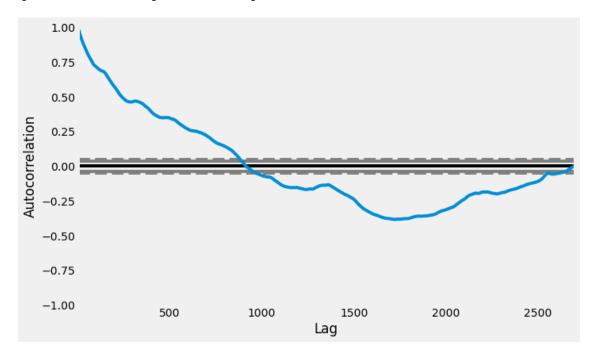
```
[90]: #lag plot
from pandas.plotting import lag_plot
lag_plot(df['Close'],lag=5)
#a linear plot also indicates non random dataset
```

[90]: <matplotlib.axes._subplots.AxesSubplot at 0x7f9e58c3da90>



```
[91]: from pandas.plotting import autocorrelation_plot autocorrelation_plot(df['Close']) #autocorrelation suggests arima might be a good model
```

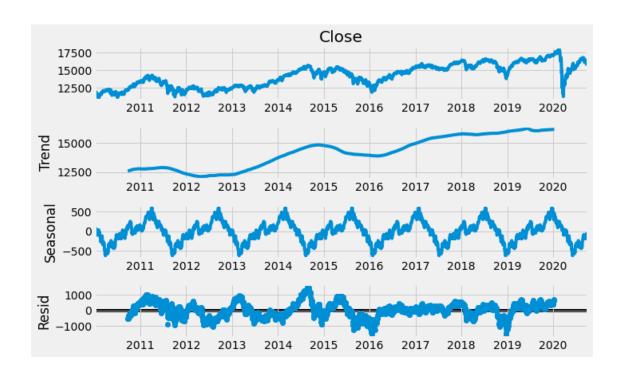
[91]: <matplotlib.axes._subplots.AxesSubplot at 0x7f9e58bf0910>



```
[92]: #original data shows as not stationary due to high p level
from statsmodels.tsa.stattools import adfuller
result = adfuller(df.Close.dropna())
print(f"ADF Statstic: {result[0]}")
print(f"p-value:{result[1]}")
```

ADF Statstic: -2.1272017170757755 p-value:0.23371823999228158

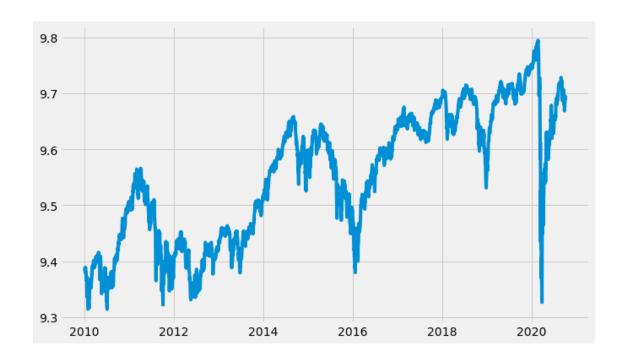
```
[93]: #decompose data
import statsmodels.api as sm
res = sm.tsa.seasonal_decompose(df['Close'],model= 'addictive',period = 365)
resplot = res.plot()
#upward trend
```



```
[100]: def plot_df(df,x,y,title= "", xlabel = "Date", ylabel='Value',dpi=100):
    plt.plot(x,y)
    plt.show()

[101]: #apply log transformation to stablize data
    plt.plot(df.apply(np.log)['Close'])
```

[101]: [<matplotlib.lines.Line2D at 0x7f9e3a7c8290>]

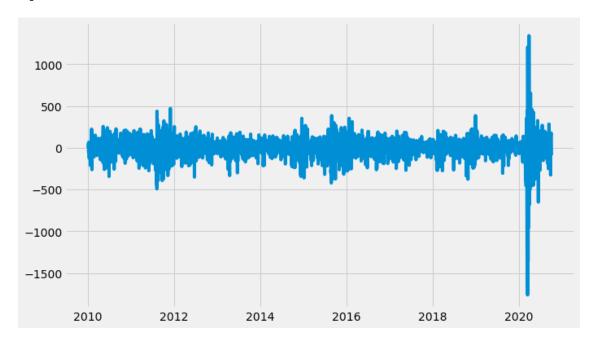


[102]: #To covert data into stationary dataset, first differencing has to be applied.

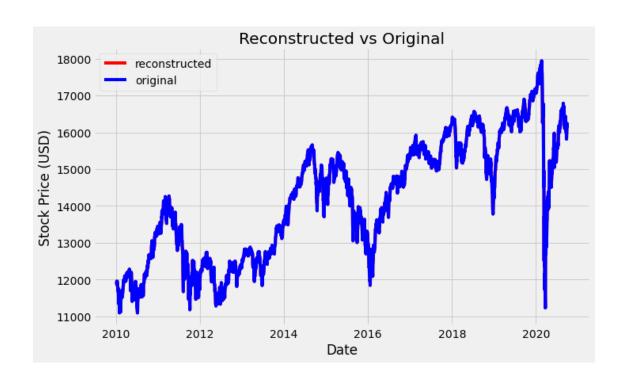
With first differencing, empty field needs to be filled as 0.

plt.plot(df['Close'].diff(1).fillna(0))

[102]: [<matplotlib.lines.Line2D at 0x7f9e3a7acd10>]



```
[103]: #confirm stationarity
      from statsmodels.tsa.stattools import adfuller
      result = adfuller(np.log(df['Close']).diff(1).fillna(0))
      print(f"ADF Statstic: {result[0]}")
      print(f"p-value:{result[1]}")
      ADF Statstic: -10.92108896454532
      p-value:1.037610106877016e-19
[104]: df_st= df.diff(1).fillna(0)
[105]: #understand the structure of the stationary dataset
      df_st.head()
[105]:
                     Close year month day
      Date
      2010-01-04 0.00000 0.0
                                    0.0 0.0
      2010-01-05 21.19922
                             0.0
                                    0.0 1.0
      2010-01-06 56.40039
                                    0.0 1.0
                             0.0
      2010-01-07 -57.00000
                             0.0
                                    0.0 1.0
      2010-01-08 66.29981
                             0.0
                                    0.0 1.0
[106]: | #With transformation to maintain stationarity, we need to be model back to the
       →original dataset in order to predict stock price.
      df reconstruct=df st.copy()
      df_resconstruct=df_reconstruct.cumsum()
[107]: df_reconstruct=df_st.copy()
      df_reconstruct.iloc[0,:]=df.iloc[0,:]
      df_reconstruct = df_reconstruct.cumsum()
[108]: plt.plot(df.index, df_reconstruct['Close'], 'r-', label='reconstructed')
      plt.plot(df.index, df['Close'], 'b-', label = 'original')
      plt.xlabel('Date'); plt.ylabel('Stock Price (USD)')
      plt.title('Reconstructed vs Original')
      plt.legend();
       #plot confirms the same pattern of data
```



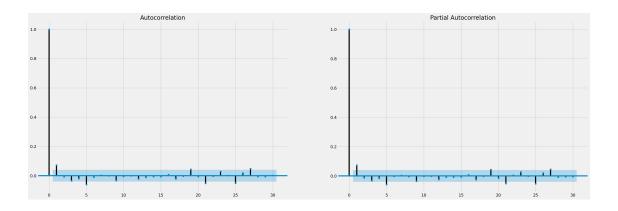
```
[109]: #define data
class TimeSeriesData():
    def __init__(self, df):
        self.data = df
        self.stationary = self.stationarize(df)
        self.reconstructed = self.reconstruct(self.stationary, self.data)

    def reconstruct(self, st, org):
        x = st.copy()
        x.iloc[0,:] = org.iloc[0,:]
        return x.cumsum()

    def stationarize(self, data):
        return data.diff(1).fillna(0)
```

```
[110]: #split dataset
x_train = TimeSeriesData(df[:int((len(df)*0.9))])
x_valid = TimeSeriesData(df[int((len(df)*0.9)):])
```

```
[111]: #plot ACF and PACF for the stationary dataset
from statsmodels.graphics.tsaplots import plot_acf, plot_pacf
fig, axes = plt.subplots(1,2,figsize=(30,10), dpi= 100)
plot_acf(x_train.stationary['Close'].values.tolist(), lags=30, ax=axes[0]);
plot_pacf(x_train.stationary['Close'].values.tolist(), lags=30, ax=axes[1]);
```



```
[112]: #using auto_arima to aquire p and q value with min AIC.

from pmdarima import auto_arima

model = auto_arima(x_train.data['Close'], trace=True, error_action='ignore',

suppress_warnings=True)

model.fit(x_train.data['Close'])
```

```
Performing stepwise search to minimize aic
```

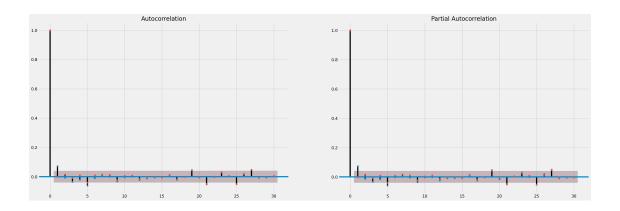
```
ARIMA(2,1,2)(0,0,0)[0] intercept
                                    : AIC=29284.460, Time=3.54 sec
ARIMA(0,1,0)(0,0,0)[0] intercept
                                    : AIC=29299.150, Time=0.06 sec
ARIMA(1,1,0)(0,0,0)[0] intercept
                                    : AIC=29288.301, Time=0.12 sec
ARIMA(0,1,1)(0,0,0)[0] intercept
                                    : AIC=29288.102, Time=0.41 sec
ARIMA(0,1,0)(0,0,0)[0]
                                    : AIC=29297.992, Time=0.04 sec
                                    : AIC=29284.372, Time=2.10 sec
ARIMA(1,1,2)(0,0,0)[0] intercept
ARIMA(0,1,2)(0,0,0)[0] intercept
                                    : AIC=29290.093, Time=0.33 sec
                                    : AIC=29290.101, Time=0.24 sec
ARIMA(1,1,1)(0,0,0)[0] intercept
                                    : AIC=29284.493, Time=1.98 sec
ARIMA(1,1,3)(0,0,0)[0] intercept
                                    : AIC=29289.281, Time=0.46 sec
ARIMA(0,1,3)(0,0,0)[0] intercept
ARIMA(2,1,1)(0,0,0)[0] intercept
                                    : AIC=29283.355, Time=2.06 sec
                                    : AIC=29289.908, Time=0.19 sec
ARIMA(2,1,0)(0,0,0)[0] intercept
ARIMA(3,1,1)(0,0,0)[0] intercept
                                    : AIC=29284.421, Time=1.83 sec
ARIMA(3,1,0)(0,0,0)[0] intercept
                                    : AIC=29289.212, Time=0.37 sec
                                    : AIC=29284.636, Time=2.49 sec
ARIMA(3,1,2)(0,0,0)[0] intercept
ARIMA(2,1,1)(0,0,0)[0]
                                    : AIC=29282.546, Time=0.43 sec
                                    : AIC=29288.830, Time=0.07 sec
ARIMA(1,1,1)(0,0,0)[0]
ARIMA(2,1,0)(0,0,0)[0]
                                    : AIC=29288.652, Time=0.07 sec
                                    : AIC=29283.585, Time=0.62 sec
ARIMA(3,1,1)(0,0,0)[0]
ARIMA(2,1,2)(0,0,0)[0]
                                    : AIC=29283.622, Time=0.82 sec
ARIMA(1,1,0)(0,0,0)[0]
                                    : AIC=29287.027, Time=0.37 sec
                                    : AIC=29283.536, Time=0.76 sec
ARIMA(1,1,2)(0,0,0)[0]
ARIMA(3,1,0)(0,0,0)[0]
                                    : AIC=29288.009, Time=0.10 sec
ARIMA(3,1,2)(0,0,0)[0]
                                    : AIC=29283.809, Time=1.00 sec
```

Best model: ARIMA(2,1,1)(0,0,0)[0] Total fit time: 20.474 seconds

```
[112]: ARIMA(maxiter=50, method='lbfgs', order=(2, 1, 1), out_of_sample_size=0,
           scoring='mse', scoring_args={}, seasonal_order=(0, 0, 0, 0),
           start_params=None, suppress_warnings=True, trend=None,
           with_intercept=False)
[113]: model_arima = ARIMA(x_train.data['Close'].values, order=(2,1,1))
[114]: result_arima = model_arima.fit(disp=-1)
[115]: print(result_arima.summary())
                                ARIMA Model Results
     Dep. Variable:
                                    D.y
                                          No. Observations:
                                                                         2426
     Model:
                         ARIMA(2, 1, 1)
                                         Log Likelihood
                                                                   -14636.746
     Method:
                                 css-mle S.D. of innovations
                                                                       100.921
     Date:
                       Mon, 16 Nov 2020
                                         AIC
                                                                     29283.491
     Time:
                                22:39:29 BIC
                                                                     29312.461
     Sample:
                                     1 HQIC
                                                                     29294.025
                                                  P>|z|
                                                             [0.025
                                                                        0.975
                     coef
                            std err
                  1.8895
                              1.741
                                       1.085
                                                  0.278
                                                             -1.523
                                                                        5.301
                                    16.248
                                                 0.000
     ar.L1.D.y
                 0.9539
                              0.059
                                                            0.839
                                                                        1.069
     ar.L2.D.y
                  -0.0924
                              0.020
                                      -4.543
                                                 0.000
                                                            -0.132
                                                                       -0.053
                                                                       -0.773
     ma.L1.D.y
                  -0.8825
                              0.056
                                      -15.821
                                                  0.000
                                                            -0.992
                                      Roots
     ______
                      Real
                                   Imaginary
                                                     Modulus
                                                                   Frequency
     AR.1
                                   +0.0000j
                    1.1840
                                                      1.1840
                                                                       0.0000
                                   +0.0000j
     AR.2
                   9.1437
                                                     9.1437
                                                                       0.0000
                                                      1.1332
     MA.1
                    1.1332
                                   +0.0000j
                                                                       0.0000
[116]: #understand residual
      residuals = pd.DataFrame(result_arima.resid)
[117]: plot acf(residuals, lags=30, ax=axes[0])
      plot_pacf(residuals, lags=30, ax=axes[1])
```

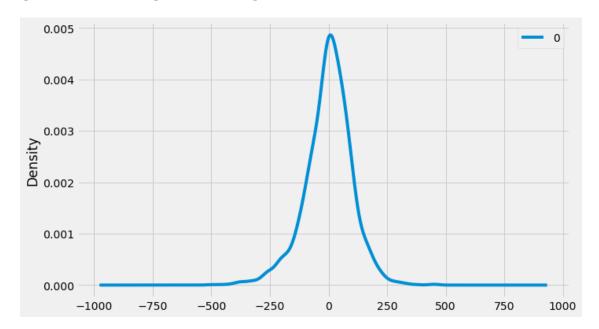
22

[117]:

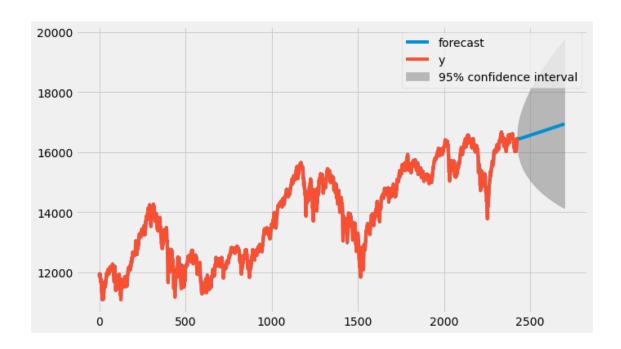


[118]: residuals.plot(kind='kde')

[118]: <matplotlib.axes._subplots.AxesSubplot at 0x7f9e58d08290>



[123]: result_arima.plot_predict(1,2700);



```
[120]: prediction = result_arima.predict(len(df)-208,len(df)-1)
       def rmse(validation, prediction):
          error = validation - prediction
          return np.sqrt(np.mean(error**2))
[121]: from statsmodels.tools.eval_measures import rmse
       #RMSE for ARIMA Model
       err_LSTM = rmse(x_valid.data['Close'], np.append(x_train.data.iloc[-1,:
       →]['Close'], prediction).cumsum()[1:])
       print('RMSE with LSTM', err_LSTM)
      RMSE with LSTM 1476.4252612252953
 []:
 []:
       #using LSTM to predict stock price
      pip install tensorflow
[44]:
      Collecting tensorflow
        Using cached tensorflow-2.3.1-cp37-cp37m-manylinux2010_x86_64.whl (320.4 MB)
      Requirement already satisfied: six>=1.12.0 in /opt/conda/lib/python3.7/site-
      packages (from tensorflow) (1.14.0)
      Collecting grpcio>=1.8.6
        Using cached grpcio-1.33.2-cp37-cp37m-manylinux2014_x86_64.whl (3.8 MB)
```

```
Collecting google-pasta>=0.1.8
  Using cached google_pasta-0.2.0-py3-none-any.whl (57 kB)
Collecting astunparse==1.6.3
  Using cached astunparse-1.6.3-py2.py3-none-any.whl (12 kB)
Requirement already satisfied: h5py<2.11.0,>=2.10.0 in
/opt/conda/lib/python3.7/site-packages (from tensorflow) (2.10.0)
Collecting keras-preprocessing<1.2,>=1.1.1
  Using cached Keras_Preprocessing-1.1.2-py2.py3-none-any.whl (42 kB)
Collecting tensorboard<3,>=2.3.0
  Using cached tensorboard-2.4.0-py3-none-any.whl (10.6 MB)
Collecting tensorflow-estimator<2.4.0,>=2.3.0
  Using cached tensorflow_estimator-2.3.0-py2.py3-none-any.whl (459 kB)
Collecting opt-einsum>=2.3.2
  Using cached opt_einsum-3.3.0-py3-none-any.whl (65 kB)
Collecting absl-py>=0.7.0
 Using cached absl_py-0.11.0-py3-none-any.whl (127 kB)
Requirement already satisfied: numpy<1.19.0,>=1.16.0 in
/opt/conda/lib/python3.7/site-packages (from tensorflow) (1.18.4)
Processing ./.cache/pip/wheels/3f/e3/ec/8a8336ff196023622fbcb36de0c5a5c218cbb241
11d1d4c7f2/termcolor-1.1.0-py3-none-any.whl
Requirement already satisfied: wheel>=0.26 in /opt/conda/lib/python3.7/site-
packages (from tensorflow) (0.34.2)
Requirement already satisfied: protobuf>=3.9.2 in /opt/conda/lib/python3.7/site-
packages (from tensorflow) (3.11.4)
Processing ./.cache/pip/wheels/62/76/4c/aa25851149f3f6d9785f6c869387ad82b3fd3758
2fa8147ac6/wrapt-1.12.1-cp37-cp37m-linux_x86_64.whl
Collecting gast==0.3.3
 Using cached gast-0.3.3-py2.py3-none-any.whl (9.7 kB)
Requirement already satisfied: requests<3,>=2.21.0 in
/opt/conda/lib/python3.7/site-packages (from tensorboard<3,>=2.3.0->tensorflow)
(2.23.0)
Requirement already satisfied: setuptools>=41.0.0 in
/opt/conda/lib/python3.7/site-packages (from tensorboard<3,>=2.3.0->tensorflow)
(46.1.3.post20200325)
Collecting werkzeug>=0.11.15
  Using cached Werkzeug-1.0.1-py2.py3-none-any.whl (298 kB)
Collecting markdown>=2.6.8
  Using cached Markdown-3.3.3-py3-none-any.whl (96 kB)
Collecting tensorboard-plugin-wit>=1.6.0
  Using cached tensorboard_plugin_wit-1.7.0-py3-none-any.whl (779 kB)
Collecting google-auth-oauthlib<0.5,>=0.4.1
 Using cached google_auth_oauthlib-0.4.2-py2.py3-none-any.whl (18 kB)
Requirement already satisfied: google-auth<2,>=1.6.3 in
/opt/conda/lib/python3.7/site-packages (from tensorboard<3,>=2.3.0->tensorflow)
(1.16.1)
Requirement already satisfied: idna<3,>=2.5 in /opt/conda/lib/python3.7/site-
packages (from requests<3,>=2.21.0->tensorboard<3,>=2.3.0->tensorflow) (2.9)
Requirement already satisfied: urllib3!=1.25.0,!=1.25.1,<1.26,>=1.21.1 in
```

```
/opt/conda/lib/python3.7/site-packages (from
requests<3,>=2.21.0->tensorboard<3,>=2.3.0->tensorflow) (1.25.9)
Requirement already satisfied: certifi>=2017.4.17 in
/opt/conda/lib/python3.7/site-packages (from
requests<3,>=2.21.0->tensorboard<3,>=2.3.0->tensorflow) (2020.4.5.2)
Requirement already satisfied: chardet<4,>=3.0.2 in
/opt/conda/lib/python3.7/site-packages (from
requests<3,>=2.21.0->tensorboard<3,>=2.3.0->tensorflow) (3.0.4)
Requirement already satisfied: importlib-metadata; python version < "3.8" in
/opt/conda/lib/python3.7/site-packages (from
markdown>=2.6.8->tensorboard<3,>=2.3.0->tensorflow) (1.6.0)
Requirement already satisfied: requests-oauthlib>=0.7.0 in
/opt/conda/lib/python3.7/site-packages (from google-auth-
oauthlib<0.5,>=0.4.1-ytensorboard<3,>=2.3.0-ytensorflow) (1.3.0)
Requirement already satisfied: pyasn1-modules>=0.2.1 in
/opt/conda/lib/python3.7/site-packages (from google-
auth<2,>=1.6.3->tensorboard<3,>=2.3.0->tensorflow) (0.2.8)
Requirement already satisfied: rsa<4.1,>=3.1.4 in /opt/conda/lib/python3.7/site-
packages (from google-auth<2,>=1.6.3->tensorboard<3,>=2.3.0->tensorflow) (4.0)
Requirement already satisfied: cachetools<5.0,>=2.0.0 in
/opt/conda/lib/python3.7/site-packages (from google-
auth<2,>=1.6.3->tensorboard<3,>=2.3.0->tensorflow) (4.1.0)
Requirement already satisfied: zipp>=0.5 in /opt/conda/lib/python3.7/site-
packages (from importlib-metadata; python_version <</pre>
"3.8"->markdown>=2.6.8->tensorboard<3,>=2.3.0->tensorflow) (3.1.0)
Requirement already satisfied: oauthlib>=3.0.0 in /opt/conda/lib/python3.7/site-
packages (from requests-oauthlib>=0.7.0->google-auth-
oauthlib<0.5,>=0.4.1->tensorboard<3,>=2.3.0->tensorflow) (3.0.1)
Requirement already satisfied: pyasn1<0.5.0,>=0.4.6 in
/opt/conda/lib/python3.7/site-packages (from pyasn1-modules>=0.2.1->google-
auth<2,>=1.6.3->tensorboard<3,>=2.3.0->tensorflow) (0.4.8)
Installing collected packages: grpcio, google-pasta, astunparse, keras-
preprocessing, absl-py, werkzeug, markdown, tensorboard-plugin-wit, google-auth-
oauthlib, tensorboard, tensorflow-estimator, opt-einsum, termcolor, wrapt, gast,
tensorflow
Successfully installed absl-py-0.11.0 astunparse-1.6.3 gast-0.3.3 google-auth-
oauthlib-0.4.2 google-pasta-0.2.0 grpcio-1.33.2 keras-preprocessing-1.1.2
markdown-3.3.3 opt-einsum-3.3.0 tensorboard-2.4.0 tensorboard-plugin-wit-1.7.0
tensorflow-2.3.1 tensorflow-estimator-2.3.0 termcolor-1.1.0 werkzeug-1.0.1
wrapt-1.12.1
Note: you may need to restart the kernel to use updated packages.
```

[45]: pip install keras

Collecting keras

Using cached Keras-2.4.3-py2.py3-none-any.whl (36 kB)
Requirement already satisfied: scipy>=0.14 in /opt/conda/lib/python3.7/site-packages (from keras) (1.4.1)

```
Requirement already satisfied: numpy>=1.9.1 in /opt/conda/lib/python3.7/site-
     packages (from keras) (1.18.4)
     Requirement already satisfied: h5py in /opt/conda/lib/python3.7/site-packages
     (from keras) (2.10.0)
     Requirement already satisfied: pyyaml in /opt/conda/lib/python3.7/site-packages
     (from keras) (5.3.1)
     Requirement already satisfied: six in /opt/conda/lib/python3.7/site-packages
     (from h5py->keras) (1.14.0)
     Installing collected packages: keras
     Successfully installed keras-2.4.3
     Note: you may need to restart the kernel to use updated packages.
[46]: pip install pandas-datareader
     Requirement already satisfied: pandas-datareader in
     /opt/conda/lib/python3.7/site-packages (0.9.0)
     Requirement already satisfied: lxml in /opt/conda/lib/python3.7/site-packages
     (from pandas-datareader) (4.5.1)
     Requirement already satisfied: requests>=2.19.0 in
     /opt/conda/lib/python3.7/site-packages (from pandas-datareader) (2.23.0)
     Requirement already satisfied: pandas>=0.23 in /opt/conda/lib/python3.7/site-
     packages (from pandas-datareader) (1.0.3)
     Requirement already satisfied: certifi>=2017.4.17 in
     /opt/conda/lib/python3.7/site-packages (from requests>=2.19.0->pandas-
     datareader) (2020.4.5.2)
     Requirement already satisfied: urllib3!=1.25.0,!=1.25.1,<1.26,>=1.21.1 in
     /opt/conda/lib/python3.7/site-packages (from requests>=2.19.0->pandas-
     datareader) (1.25.9)
     Requirement already satisfied: chardet<4,>=3.0.2 in
     /opt/conda/lib/python3.7/site-packages (from requests>=2.19.0->pandas-
     datareader) (3.0.4)
     Requirement already satisfied: idna<3,>=2.5 in /opt/conda/lib/python3.7/site-
     packages (from requests>=2.19.0->pandas-datareader) (2.9)
     Requirement already satisfied: python-dateutil>=2.6.1 in
     /opt/conda/lib/python3.7/site-packages (from pandas>=0.23->pandas-datareader)
     (2.8.1)
     Requirement already satisfied: pytz>=2017.2 in /opt/conda/lib/python3.7/site-
     packages (from pandas>=0.23->pandas-datareader) (2020.1)
     Requirement already satisfied: numpy>=1.13.3 in /opt/conda/lib/python3.7/site-
     packages (from pandas>=0.23->pandas-datareader) (1.18.4)
     Requirement already satisfied: six>=1.5 in /opt/conda/lib/python3.7/site-
     packages (from python-dateutil>=2.6.1->pandas>=0.23->pandas-datareader) (1.14.0)
     Note: you may need to restart the kernel to use updated packages.
[47]: from pandas_datareader import data
      import datetime as dt
```

from matplotlib import pyplot as plt

```
from sklearn import model_selection
      from sklearn.metrics import confusion_matrix
      from sklearn.preprocessing import StandardScaler
      from sklearn.model_selection import train_test_split
      import numpy as np
      import pandas as pd
      from sklearn.preprocessing import MinMaxScaler
      from keras.models import Sequential
      from keras.layers import Dense
      from keras.layers import LSTM
      from keras.layers import Dropout
[48]: #similar to before, upload NASDAQ data
      df=pd.read_csv("IXIC_v1.csv", sep=",")
      from datetime import datetime
      con=df['Date']
      df['Date']=pd.to datetime(df['Date'])
      df.set_index('Date', inplace=True)
      test = df[2164:]
      train = df[:2163]
[49]: df['Date'] = df.index
      data2 = pd.DataFrame(columns = ['Date', 'Close'])
      data2['Date'] = df['Date']
      data2['Close'] = df['Close']
[50]: #scale and reshape data
      train_set = data2.iloc[:, 1:2].values
      sc = MinMaxScaler(feature_range = (0, 1))
      training_set_scaled = sc.fit_transform(train_set)
      X_train = []
      y_train = []
      for i in range(60, 2600):
          X_train.append(training_set_scaled[i-60:i, 0])
          y_train.append(training_set_scaled[i, 0])
      X_train, y_train = np.array(X_train), np.array(y_train)
      X_train = np.reshape(X_train, (X_train.shape[0], X_train.shape[1], 1))
[51]: #add layers
      regressor = Sequential()
      regressor.add(LSTM(units = 50, return sequences = True, input_shape = (X_train.
      →shape[1], 1)))
      regressor.add(Dropout(0.2))
      regressor.add(LSTM(units = 50, return_sequences = True))
      regressor.add(Dropout(0.2))
      regressor.add(LSTM(units = 50, return_sequences = True))
      regressor.add(Dropout(0.2))
```

```
regressor.add(LSTM(units = 50))
   regressor.add(Dropout(0.2))
   regressor.add(Dense(units = 1))
[52]: #add optimizer and build model
   regressor.compile(optimizer = 'adam', loss = 'mean_squared_error')
   regressor.fit(X_train, y_train, epochs = 35, batch_size = 30)
  Epoch 1/35
  Epoch 2/35
  85/85 [============= ] - 12s 144ms/step - loss: 0.0021
  Epoch 3/35
  Epoch 4/35
  Epoch 5/35
  Epoch 6/35
  85/85 [============ ] - 12s 138ms/step - loss: 0.0014
  Epoch 7/35
```

85/85 [=============] - 12s 141ms/step - loss: 0.0012

85/85 [============] - 12s 138ms/step - loss: 8.8376e-04

85/85 [============] - 12s 137ms/step - loss: 8.9150e-04

85/85 [===========] - 12s 139ms/step - loss: 7.4694e-04

Epoch 8/35

Epoch 9/35

Epoch 10/35

Epoch 11/35

Epoch 12/35

Epoch 13/35

Epoch 14/35

Epoch 15/35

Epoch 16/35

Epoch 17/35

Epoch 18/35

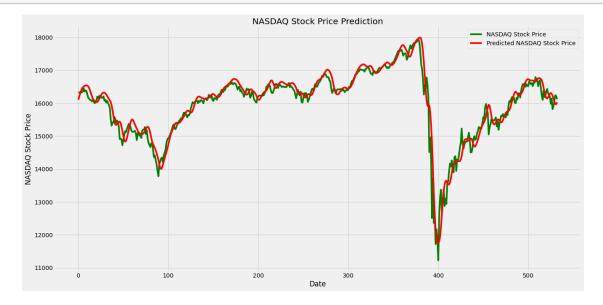
Epoch 19/35

Epoch 20/35

```
Epoch 21/35
  Epoch 22/35
  Epoch 23/35
  Epoch 24/35
  Epoch 25/35
  Epoch 26/35
  85/85 [============ ] - 12s 137ms/step - loss: 7.8931e-04
  Epoch 27/35
  Epoch 28/35
  85/85 [============= ] - 12s 136ms/step - loss: 6.9213e-04
  Epoch 29/35
  Epoch 30/35
  Epoch 31/35
  85/85 [============= ] - 11s 134ms/step - loss: 6.6173e-04
  Epoch 32/35
  Epoch 33/35
  Epoch 34/35
  Epoch 35/35
  [52]: <tensorflow.python.keras.callbacks.History at 0x7f9ed0142a10>
[70]: | #train the model
  testdataframe= test
  testdataframe['Date'] = testdataframe.index
  testdata = pd.DataFrame(columns = ['Date', 'Close'])
  testdata['Date'] = testdataframe['Date']
  testdata['Close'] = testdataframe['Close']
  real_stock_price = testdata.iloc[:, 1:2].values
  dataset_total = pd.concat((data2['Close'], testdata['Close']), axis = 0)
  inputs = dataset_total[len(dataset_total) - len(testdata) - 60:].values
  inputs = inputs.reshape(-1,1)
  inputs = sc.transform(inputs)
  X_{\text{test}} = []
  for i in range(60, 601):
```

```
X_test.append(inputs[i-60:i, 0])
X_test = np.array(X_test)
X_test = np.reshape(X_test, (X_test.shape[0], X_test.shape[1], 1))
```

```
[71]: predicted_stock_price = regressor.predict(X_test)
predicted_stock_price = sc.inverse_transform(predicted_stock_price)
```



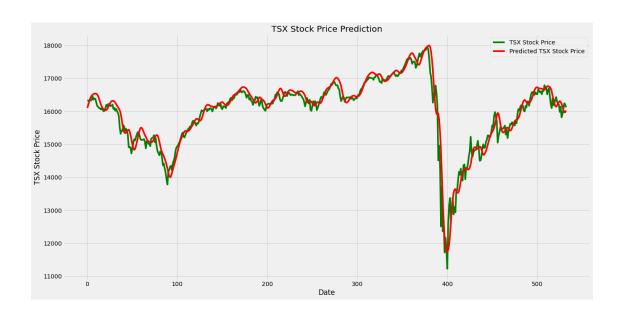
```
[74]: rmse_predict= np.reshape(predicted_stock_price,541)
[75]: test["Close"].values.shape
[75]: (541,)
[76]: rmse_predict.shape
[76]: (541,)
```

```
[77]: #RMSE for LSTM Model
       err_LSTM = rmse(test["Close"].values, rmse_predict)
       print('RMSE with LSTM', err_LSTM)
      RMSE with LSTM 396.96105468494505
[124]: #repeat the same process for TSX
       df=pd.read_csv("GSPTSE_v1.csv", sep=",")
       from datetime import datetime
       con=df['Date']
       df['Date']=pd.to_datetime(df['Date'])
       df.set_index('Date', inplace=True)
       test = df[2164:]
       train = df[:2163]
[125]: df['Date'] = df.index
       data2 = pd.DataFrame(columns = ['Date', 'Close'])
       data2['Date'] = df['Date']
       data2['Close'] = df['Close']
[134]: train_set = data2.iloc[:, 1:2].values
       sc = MinMaxScaler(feature_range = (0, 1))
       training_set_scaled = sc.fit_transform(train_set)
       X_train = []
       y_train = []
       for i in range(60, 2600):
           X_train.append(training_set_scaled[i-60:i, 0])
           y_train.append(training_set_scaled[i, 0])
       X_train, y_train = np.array(X_train), np.array(y_train)
       X_train = np.reshape(X_train, (X_train.shape[0], X_train.shape[1], 1))
[135]: regressor = Sequential()
       regressor.add(LSTM(units = 50, return sequences = True, input_shape = (X_train.
       \rightarrowshape[1], 1)))
       regressor.add(Dropout(0.2))
       regressor.add(LSTM(units = 50, return_sequences = True))
       regressor.add(Dropout(0.2))
       regressor.add(LSTM(units = 50, return_sequences = True))
       regressor.add(Dropout(0.2))
       regressor.add(LSTM(units = 50))
       regressor.add(Dropout(0.2))
       regressor.add(Dense(units = 1))
[136]: regressor.compile(optimizer = 'adam', loss = 'mean_squared_error')
       regressor.fit(X_train, y_train, epochs = 30, batch_size = 32)
```

Epoch 1/30

```
Epoch 2/30
80/80 [=========== ] - 11s 140ms/step - loss: 0.0065
Epoch 3/30
80/80 [============= ] - 11s 136ms/step - loss: 0.0059
Epoch 4/30
Epoch 5/30
Epoch 6/30
80/80 [=========== ] - 11s 134ms/step - loss: 0.0046
Epoch 7/30
80/80 [============= ] - 11s 133ms/step - loss: 0.0039
Epoch 8/30
Epoch 9/30
80/80 [============= ] - 10s 130ms/step - loss: 0.0037
Epoch 10/30
80/80 [============ ] - 10s 129ms/step - loss: 0.0033
Epoch 11/30
Epoch 12/30
Epoch 13/30
80/80 [============ ] - 10s 125ms/step - loss: 0.0033
Epoch 14/30
Epoch 15/30
Epoch 16/30
Epoch 17/30
Epoch 18/30
Epoch 19/30
Epoch 20/30
Epoch 21/30
80/80 [============== ] - 10s 126ms/step - loss: 0.0024
Epoch 22/30
Epoch 23/30
Epoch 24/30
Epoch 25/30
```

```
Epoch 26/30
    Epoch 27/30
    Epoch 28/30
    Epoch 29/30
    80/80 [============ ] - 10s 130ms/step - loss: 0.0020
    Epoch 30/30
    [136]: <tensorflow.python.keras.callbacks.History at 0x7f9e36958150>
[143]: testdataframe= test
     testdataframe['Date'] = testdataframe.index
     testdata = pd.DataFrame(columns = ['Date', 'Close'])
     testdata['Date'] = testdataframe['Date']
     testdata['Close'] = testdataframe['Close']
     real stock price = testdata.iloc[:, 1:2].values
     dataset_total = pd.concat((data2['Close'], testdata['Close']), axis = 0)
     inputs = dataset_total[len(dataset_total) - len(testdata) - 60:].values
     inputs = inputs.reshape(-1,1)
     inputs = sc.transform(inputs)
     X_{\text{test}} = []
     for i in range(60, 593):
        X_test.append(inputs[i-60:i, 0])
     X_test = np.array(X_test)
     X_test = np.reshape(X_test, (X_test.shape[0], X_test.shape[1], 1))
[144]: predicted_stock_price = regressor.predict(X_test)
     predicted_stock_price = sc.inverse_transform(predicted_stock_price)
[152]: plt.figure(figsize=(20,10))
     plt.plot(real_stock_price, color = 'green', label = 'TSX Stock Price')
     plt.plot(predicted_stock_price, color = 'red', label = 'Predicted TSX Stock_
     →Price')
     plt.title('TSX Stock Price Prediction')
     plt.xlabel('Date')
     plt.ylabel('TSX Stock Price')
     plt.legend()
     plt.show()
```



```
[147]: rmse_predict= np.reshape(predicted_stock_price,533)

[148]: test["Close"].values.shape

[148]: (533,)

[149]: rmse_predict.shape

[149]: (533,)

[150]: #RMSE for LSTM Model
    err_LSTM = rmse(test["Close"].values, rmse_predict)
    print('RMSE with LSTM', err_LSTM)

RMSE with LSTM 265.51210144690225

[ ]:
```