

6a) (i)  $\frac{\lambda^k e^{-\lambda}}{k!}$

(ii)  $\begin{cases} p & \text{if } k = 1 \\ 1 - p & \text{if } k = 0 \end{cases}$

(iii)  $\binom{n}{k} p^k (1-p)^{n-k}$

b) (i)  $X \sim \text{Ber}(\frac{3}{5})$

$$E(X) = \frac{3}{5}$$

$$\text{Var}(X) = \frac{6}{25}$$

(ii)  $Y \sim \text{Hyp}(2000, 50, 1200)$

$$E(X) = 30$$

$$\text{Var}(X) = 12$$

(iii)  $Z \sim \text{Pois}(3)$

$$E(X) = 3$$

$$\text{Var}(X) = 3$$

c) (i)

| $y \setminus x$ | -1  | 0   | +1  | $P[Y = y]$ |
|-----------------|-----|-----|-----|------------|
| -1              | 0   | 1/4 | 0   | 1/4        |
| 0               | 1/4 | 0   | 1/4 | 1/2        |
| +1              | 0   | 1/4 | 0   | 1/4        |
| $P[X = x]$      | 1/4 | 1/2 | 1/4 | 1          |

(ii)  $E[X] = 0, E[Y] = 0$

(iii) Two discrete random variables  $S$  and  $T$  are independent if for all values  $a, b$ :

$$P[S = a, T = b] = P[S = a] \cdot P[T = b]$$

$X$  and  $Y$  are not independent above, since for example

$$P[X = 0, Y = 0] \neq P[X = 0] \cdot P[Y = 0]$$

(iv) The covariance of two random variables  $S$  and  $T$  is:

$$\text{Cov}[S, T] = E[(S - E[S]) \cdot (T - E[T])].$$

$X$  and  $Y$  above have a covariance of 0, since one of  $X$  or  $Y$  is always zero, so  $(S - 0) \cdot (T - 0)$  will always evaluate to zero.