

The optimal weights are [0.3301, 0.0473, 0.6226], where the asset weights are relatively balanced, with no negative weights (i.e., no short positions). The maximum RR_p is 0.2946, which is smaller than the Sharpe ratio but shows better performance in controlling extreme loss risks. By optimizing tail risks, the RR_p portfolio might perform more stably during market volatility.

Key Differences:

1. Risk Measurement:

- The Sharpe ratio considers overall volatility (standard deviation) and optimizes the return-to-volatility ratio.
- RR_p, in addition to volatility, includes expected shortfall, focusing on risk in extreme market conditions (i.e., the probability and extent of large losses).

2. Weight Differences:

- In the maximum Sharpe ratio portfolio, one asset has a negative weight, indicating a short position to reduce volatility and improve the Sharpe ratio.
- In the maximum RR_p portfolio, no negative weights are used; instead, the weights are adjusted to optimize return while minimizing tail risk.

3. Risk-adjusted Focus:

- The maximum Sharpe ratio portfolio focuses on the overall risk-return ratio, suitable for stable market conditions.
- The maximum RR_p portfolio is more suitable for investors focusing on extreme losses or seeking a more robust investment strategy during volatile markets.

Maximum Sharpe Ratio Portfolio and Maximum RR_p Portfolio:

- **Maximum Sharpe Ratio Portfolio:** The Sharpe ratio is 0.3441, indicating an optimal risk-return ratio. Despite volatility, its return is high relative to risk.
 - Weights: $A1 = 0.1520$, $A2 = -0.1330$ (short position), $A3 = 0.9810$. This portfolio is more dependent on $A3$, with shorting $A2$ to reduce risk.
- **Maximum RR_p Portfolio:** The RR_p is 0.2946, slightly lower than the Sharpe ratio but better at managing extreme risk.
 - Weights: $A1 = 0.3301$, $A2 = 0.0473$, $A3 = 0.6226$. There are no short positions, and the weight distribution aims to reduce extreme losses.

Comparative Analysis:

- The **maximum Sharpe ratio** portfolio has a higher return (0.3441) but relies on higher volatility and shorting strategies.
- The **maximum RR_p** portfolio, with a return of 0.2946, focuses on controlling tail risks, making it more conservative and stable, especially in extreme market conditions.

Conclusion:

- The maximum Sharpe ratio portfolio is better suited for stable markets but may suffer significant volatility during market extremes.
- The maximum RR_p portfolio, with its focus on minimizing tail risks, is ideal for those concerned with performance under extreme market conditions, though it offers a slightly lower return.