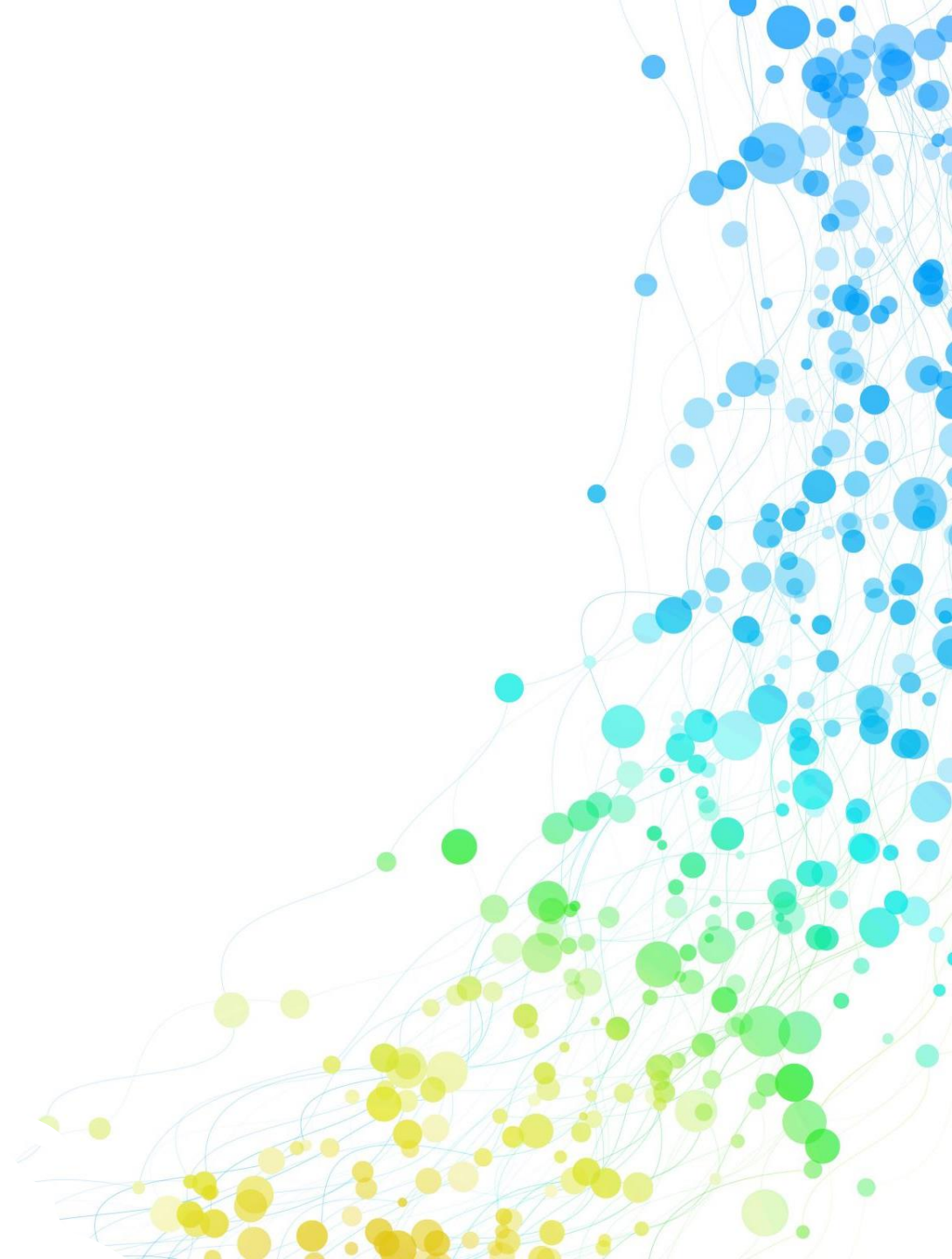


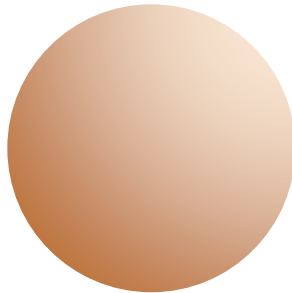
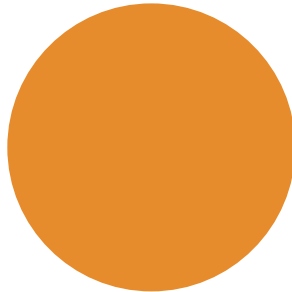
# Lighting

9<sup>TH</sup> WEEK, 2021



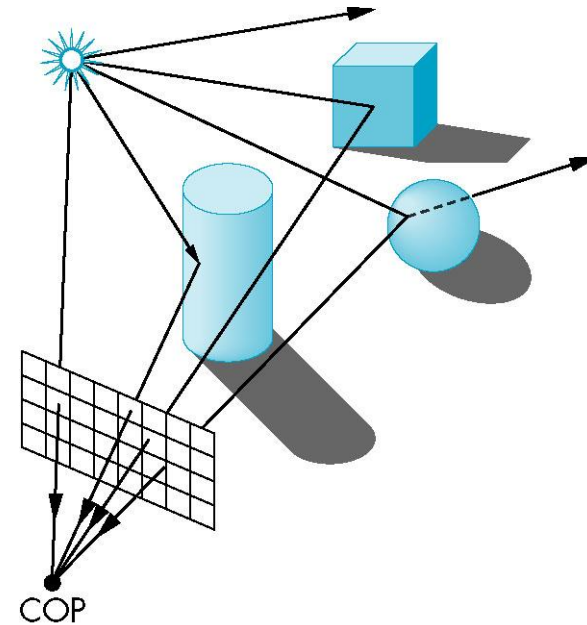
# Why We Need Shading

- Suppose we build a model of a sphere using many polygons and color it with `glColor`
- We get something like
- But we want



# Shading

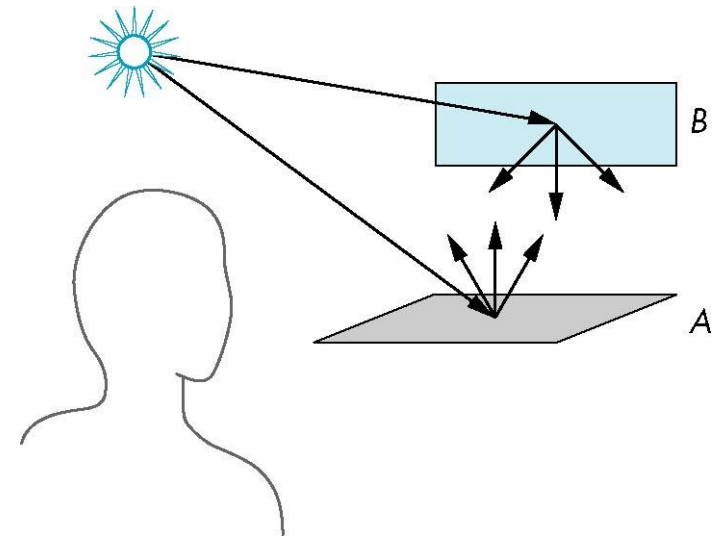
- Determining a color for each filled pixel
- Light-material interactions cause each point to have a different color or shade
- Need to consider
  - Light sources
  - Material properties
  - Location of viewer
  - Surface orientation



# Scattering of Light

- Light strikes A
  - Some scattered
  - Some absorbed
- Some of scattered light strikes B
  - Some scattered
  - Some absorbed
- Some of this scattered light strikes A and so on

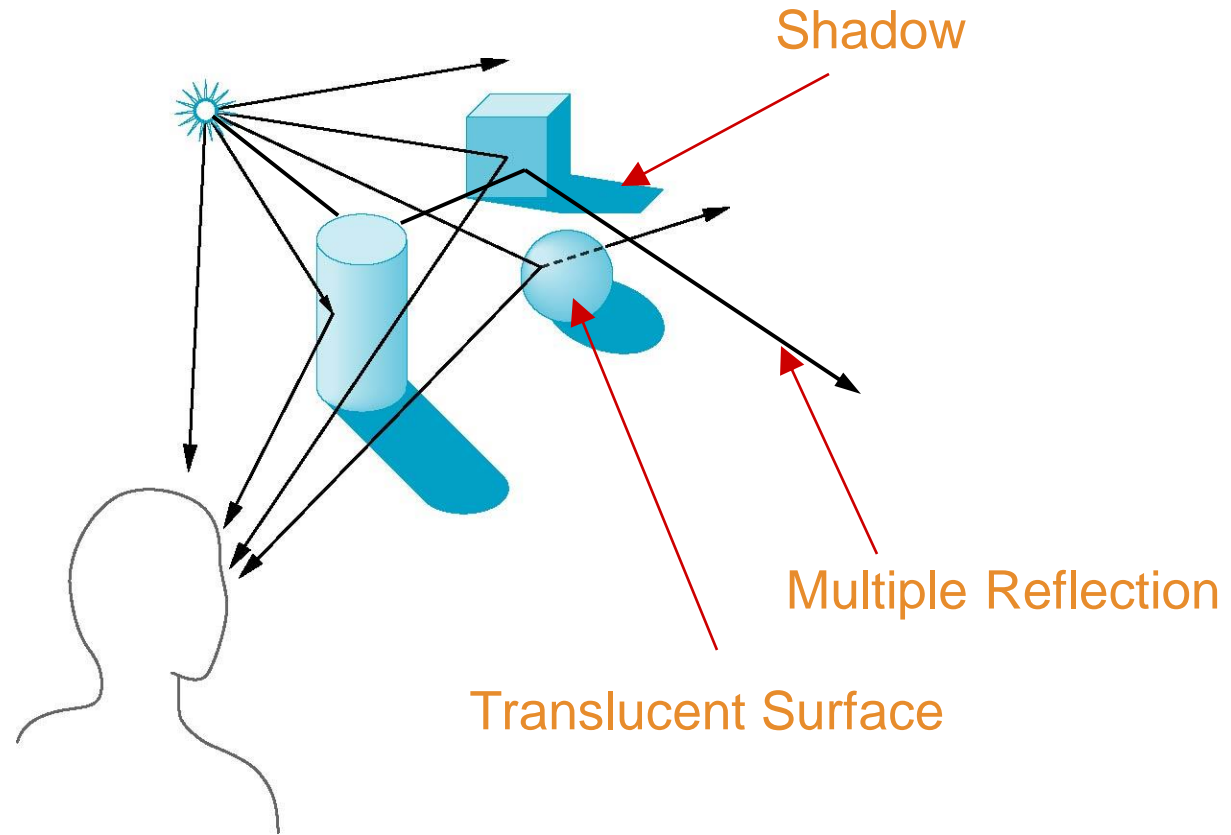
➔ Rendering Equation



# Rendering Equation

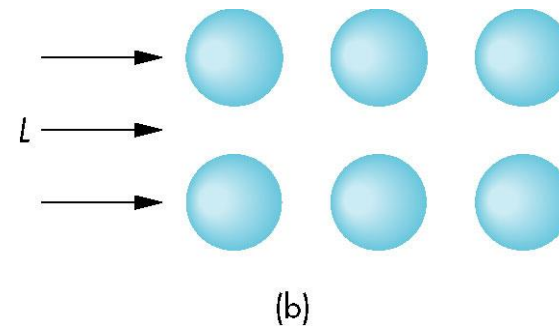
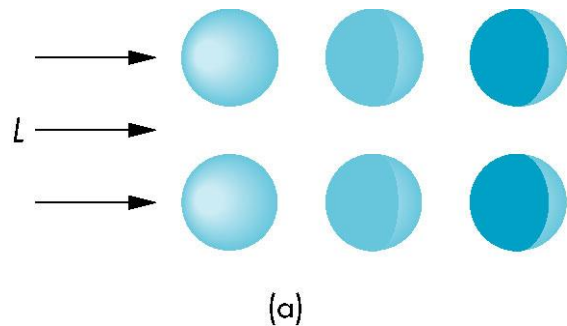
- The infinite scattering and absorption of light can be described by the *rendering equation*
  - Cannot be solved in general
  - Ray tracing is a special case for perfectly reflecting surfaces
- Rendering equation is global and includes
  - Shadows
  - Multiple scattering from object to object

# Global Effects



# Local vs. Global Rendering

- Correct shading requires a global calculation involving all objects and light sources
  - Incompatible with pipeline model which shades each polygon independently (→ local rendering)
- In computer graphics, especially real time graphics, we are happy if things “look right”
  - Many techniques exist for approximating global effects



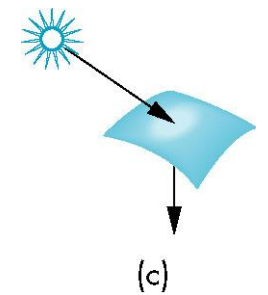
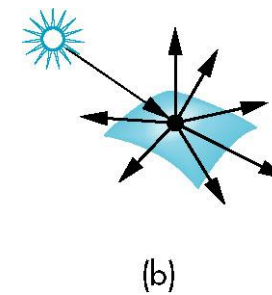
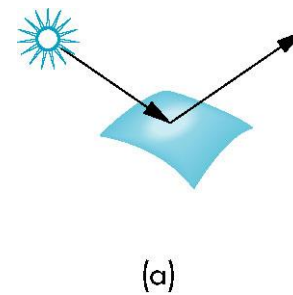
# Light-Material Interaction

- Light that strikes an object is partially absorbed and partially scattered (reflected)
- The amount reflected determines the color and brightness of the object
  - Ex) red surface under white light
- The reflected light is scattered in a manner that depends on the smoothness and orientation of the surface



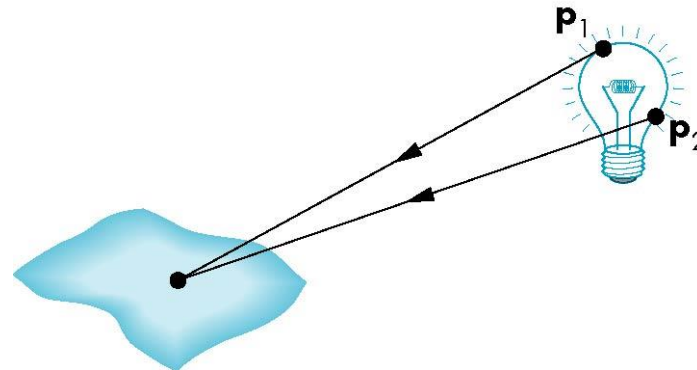
# Surface Types

- The smoother a surface, the more reflected light is concentrated in the direction a perfect mirror
  - A very rough surface scatters light in all directions
- Specular surfaces – mirror
  - Scattering reflected light in a narrow range of angle
- Diffuse surfaces – chalk, clay
  - Scattering reflected light all directions
- Translucent surfaces – glass, water
  - Refraction



# Light Sources

- General light sources are difficult to work with because we must integrate light coming from all points on the surface



- Simple mathematical models:
  - Point light
  - Distant light (directional light)
  - Spotlight

# Point Light Sources

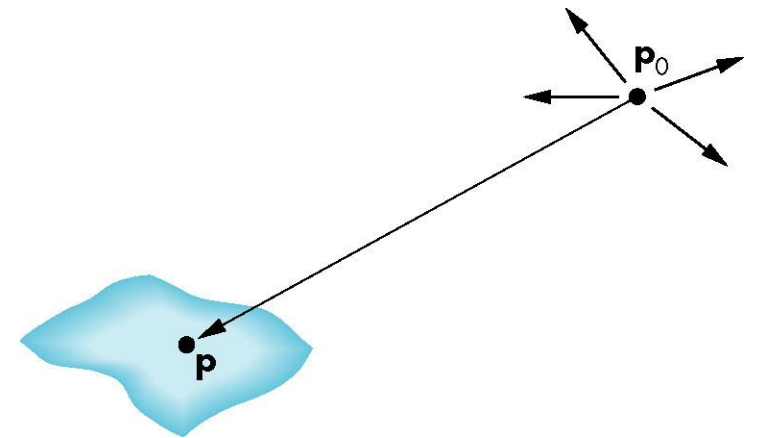
- Emitting light equally in all directions
  - $\mathbf{p}_0$ : the location of a point light source

$$\mathbf{I}(\mathbf{p}_0) = \begin{bmatrix} I_r(\mathbf{p}_0) \\ I_g(\mathbf{p}_0) \\ I_b(\mathbf{p}_0) \end{bmatrix}$$

- Attenuation
  - Proportional to the inverse square distance

$$\mathbf{I}(\mathbf{p}, \mathbf{p}_0) = \frac{1}{|\mathbf{p} - \mathbf{p}_0|^2} \mathbf{I}(\mathbf{p}_0)$$

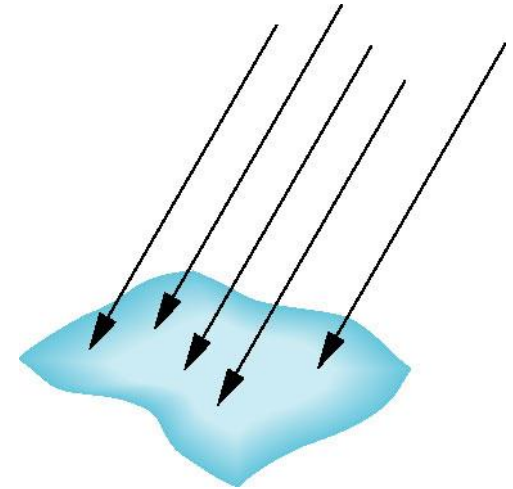
$$\mathbf{I}(\mathbf{p}, \mathbf{p}_0) = \frac{1}{k_c + k_l d + k_q d^2} \mathbf{I}(\mathbf{p}_0)$$



# Directional Light Sources

- Parallel direction of lights
  - Infinite distance away from the surface
  - Location  $\rightarrow$  direction

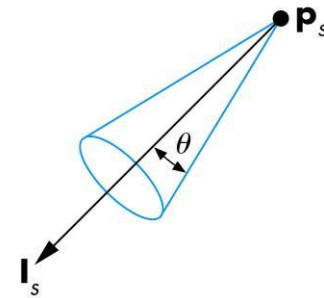
$$\mathbf{p}_0 = \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix} \quad \rightarrow \quad \mathbf{p}_0 = \begin{bmatrix} x \\ y \\ z \\ 0 \end{bmatrix}$$



# Spotlight Sources

- Characterized by a narrow range of angle through which light is emitted

- $\mathbf{p}_s$ : apex of a cone
- $\mathbf{l}_s$ : direction of pointing
- $\theta$ : angle to determine width

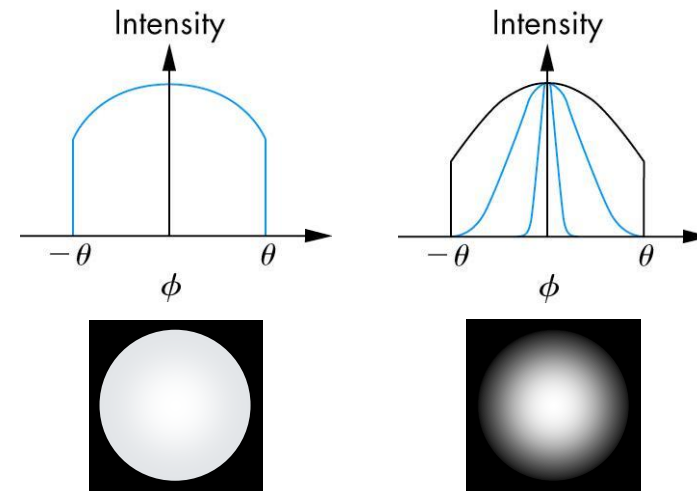


- Distribution of light
  - Concentrating in the center

$$\cos \phi = \mathbf{s} \cdot \mathbf{l}_s$$

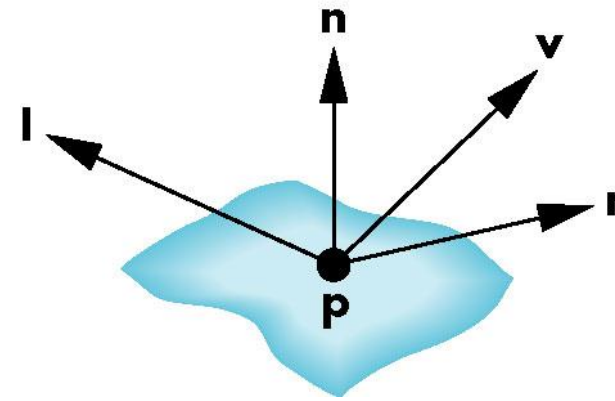
- Light intensity drop off

$$\cos^e \phi = (\mathbf{s} \cdot \mathbf{l}_s)^e$$



# Phong Reflection Model

- A simple model that can compute rapidly
- Three components (light-material interactions)
  - Ambient
  - Diffuse
  - Specular
- Using four vectors
  - **n**: normal
  - **v**: to the viewer or COP
  - **l**: to light source
  - **r**: perfect reflector



# Ambient Reflection

- Same at every point on the surface
- Ambient reflection coefficient

$$\mathbf{k}_a = (k_{ar}, k_{ag}, k_{ab}), \quad 0 \leq k_{ar}, k_{ag}, k_{ab} \leq 1$$

- Amount reflected
    - Some is absorbed and some is reflected
  - Three components (red, green, blue)
- Ambient reflection term in rendering equation

$$\mathbf{I}_a = \mathbf{k}_a \mathbf{L}_a$$

- Can be any of the individual light sources
  - Can be a global ambient term

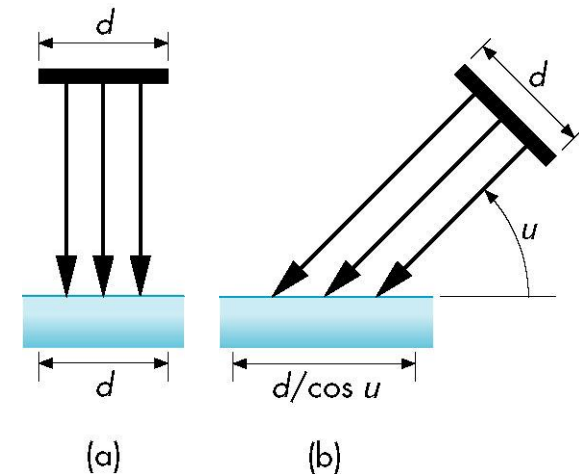
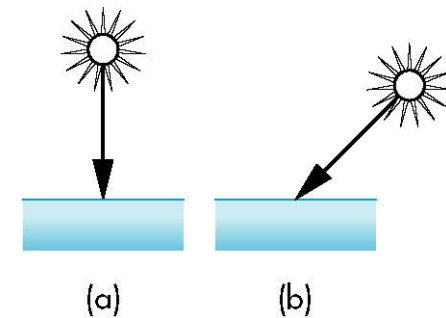
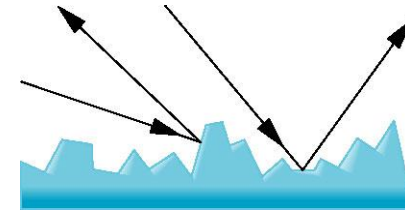
# Diffuse Reflection

- Light scattered equally in all directions
  - Perfectly diffuse surface
  - ➔ So rough that there is no preferred angle of reflection
- Lambert's law
  - Amount of light reflected is proportional to vertical component of incoming light
  - Reflected light  $\propto \cos u$
- Diffuse reflection term
  - Incorporating a distance term

$$\cos u = \mathbf{l} \cdot \mathbf{n}$$

$$\mathbf{I}_d = \mathbf{k}_d (\mathbf{l} \cdot \mathbf{n}) \mathbf{L}_d$$

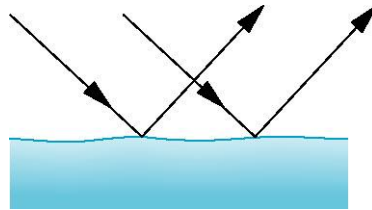
$$\mathbf{I}_d = \frac{\mathbf{k}_d}{k_c + k_l d + k_q d^2} (\mathbf{l} \cdot \mathbf{n}) \mathbf{L}_d$$





# Specular Reflection

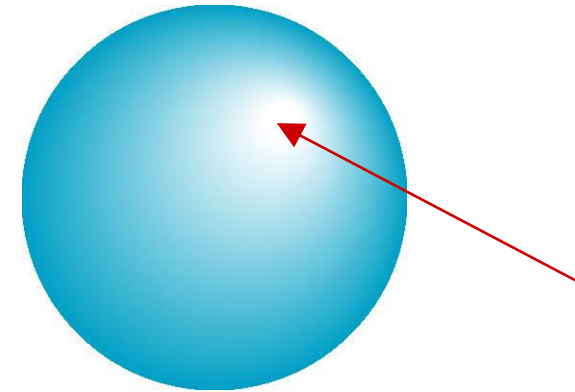
- Smooth surfaces show specular highlights



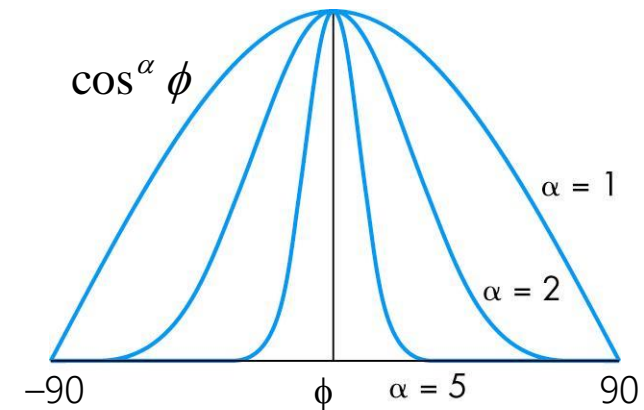
- Specular reflection term

$$\mathbf{I}_s = \mathbf{k}_s (\mathbf{r} \cdot \mathbf{v})^\alpha \mathbf{L}_s$$

- $\alpha$ : shininess coefficient
  - $\alpha \rightarrow \infty$  : mirror
  - $100 < \alpha < 200$  : metal
  - $5 < \alpha < 10$  : plastic



Specular Highlight



# Computation of Reflection

- Light sources
  - Each light source has separate ambient, diffuse, and specular terms + separate red, green, blue components = nine coefficients

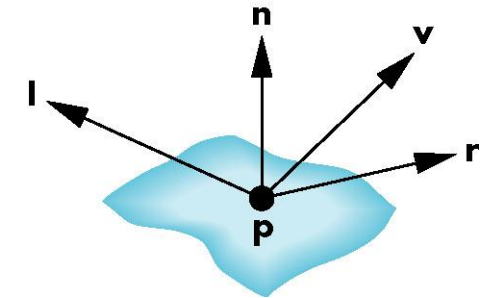
$$(L_{ar}, L_{ag}, L_{ab}, L_{dr}, L_{dg}, L_{db}, L_{sr}, L_{sg}, L_{sb})$$

- Material properties
  - Matching light source properties
  - Nine coefficients:  $(k_{ar}, k_{ag}, k_{ab}, k_{dr}, k_{dg}, k_{db}, k_{sr}, k_{sg}, k_{sb})$
  - Shininess coefficient:  $\alpha$

# Adding up the Components

- For each light source and each color component, the Phong model can be written
  - Most surfaces are neither ideal diffusers nor perfectly specular

$$\begin{aligned}\mathbf{I} &= \mathbf{I}_a + \mathbf{I}_d + \mathbf{I}_s \\ &= \mathbf{k}_a \mathbf{L}_a + \mathbf{k}_d (\mathbf{l} \cdot \mathbf{n}) \mathbf{L}_d + \mathbf{k}_s (\mathbf{r} \cdot \mathbf{v})^\alpha \mathbf{L}_s\end{aligned}$$



- Including the distance term

$$\mathbf{I} = \mathbf{k}_a \mathbf{L}_a + \frac{1}{k_c + k_l d + k_q d^2} \left( \mathbf{k}_d (\mathbf{l} \cdot \mathbf{n}) \mathbf{L}_d + \mathbf{k}_s (\mathbf{r} \cdot \mathbf{v})^\alpha \mathbf{L}_s \right)$$

# Computation of Vectors

- Normal vectors
- Ideal reflector

- Angle of incidence == angle of reflection

$$\mathbf{n} = (\mathbf{p}_1 - \mathbf{p}_0) \times (\mathbf{p}_2 - \mathbf{p}_0)$$

$$\begin{aligned}\mathbf{r} &= \mathbf{l} + 2((\mathbf{l} \cdot \mathbf{n})\mathbf{n} - \mathbf{l}) \\ &= 2(\mathbf{l} \cdot \mathbf{n})\mathbf{n} - \mathbf{l}\end{aligned}$$

- Halfway vector  $\mathbf{h} = \frac{\mathbf{l} + \mathbf{v}}{|\mathbf{l} + \mathbf{v}|}$
- Half-angle:

$$\begin{aligned}\theta + \psi &= (\theta - \psi) + \phi \\ \therefore 2\psi &= \phi\end{aligned}$$

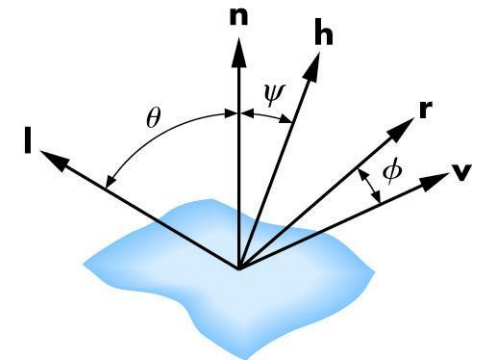
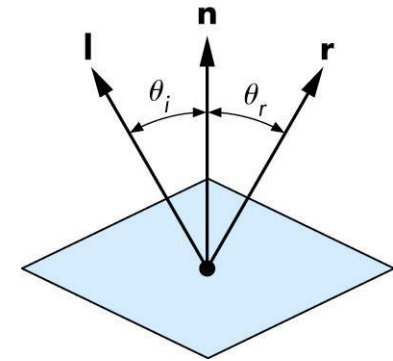
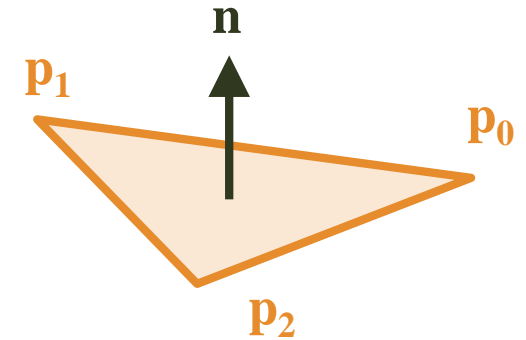
$$\mathbf{I}_s = k_s (\mathbf{r} \cdot \mathbf{v})^\alpha \mathbf{L}_s$$

Phong Model

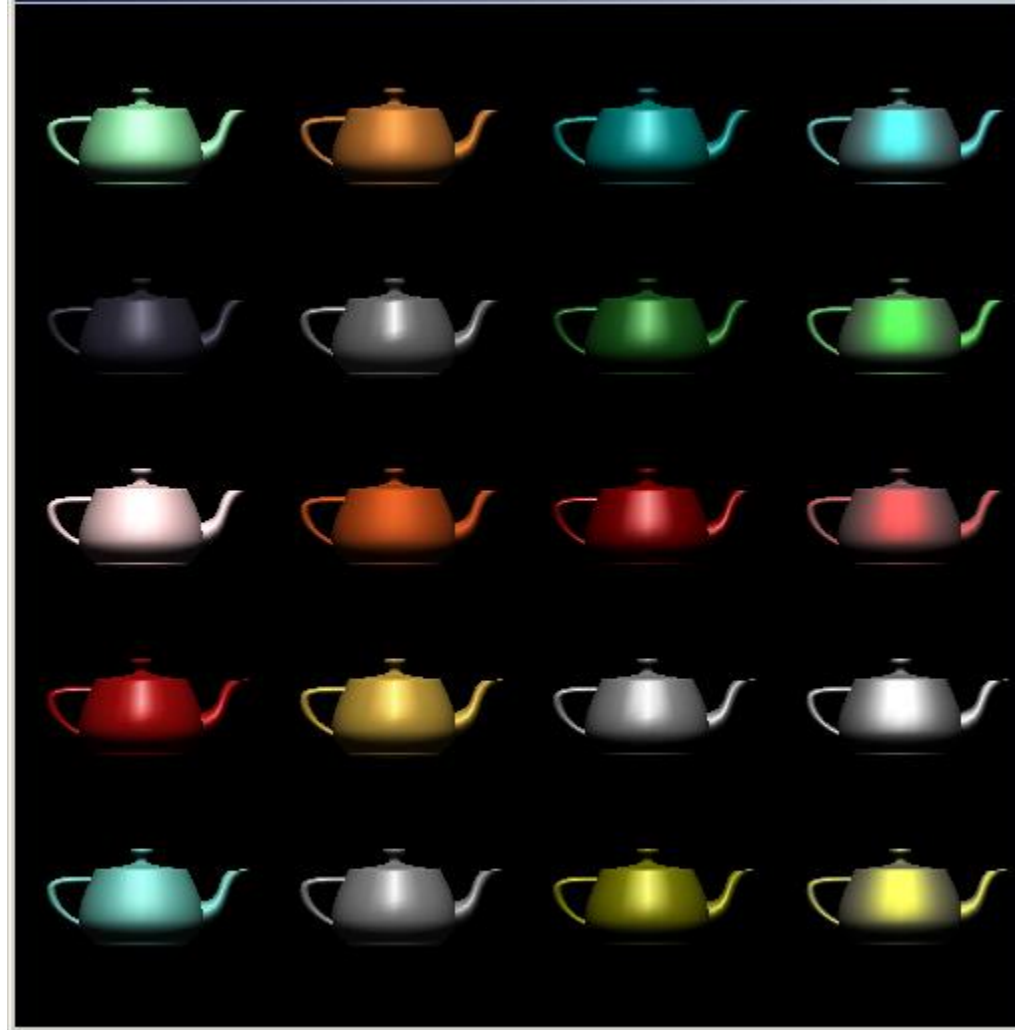


$$\mathbf{I}_s = k_s (\mathbf{n} \cdot \mathbf{h})^\beta \mathbf{L}_s$$

Blinn Model



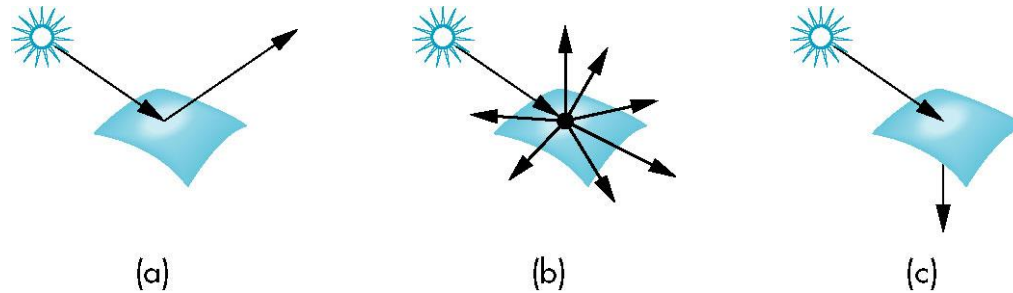
# Utah Teapots with Different Material Properties



# Summary

- Shading → light-material interaction

- Surface types



- Light sources → point light, directional light, and spotlight

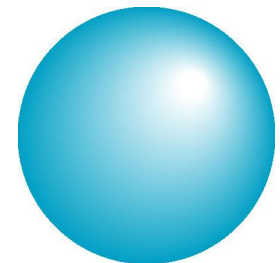
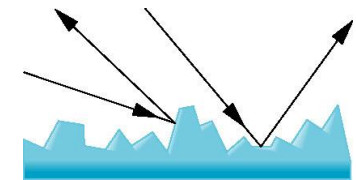
- Phong reflection model = ambient + diffuse + specular

$$\mathbf{I} = \mathbf{I}_a + \mathbf{I}_d + \mathbf{I}_s$$

$$= \mathbf{k}_a \mathbf{L}_a + \mathbf{k}_d (\mathbf{l} \cdot \mathbf{n}) \mathbf{L}_d + \mathbf{k}_s (\mathbf{r} \cdot \mathbf{v})^\alpha \mathbf{L}_s$$

- attenuation

$$\mathbf{I} = \mathbf{k}_a \mathbf{L}_a + \frac{1}{k_c + k_l d + k_q d^2} \left( \mathbf{k}_d (\mathbf{l} \cdot \mathbf{n}) \mathbf{L}_d + \mathbf{k}_s (\mathbf{r} \cdot \mathbf{v})^\alpha \mathbf{L}_s \right)$$



수고하셨습니다