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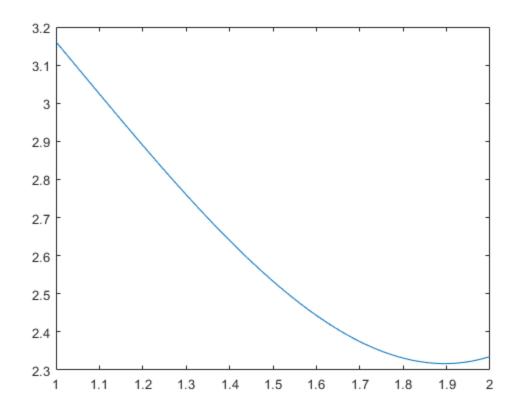
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clc;

# Define the function we are optimizing 1.1

## Plot the function

```
x = a:0.01:b;
plot(x, f(x));
```



## **Run Golden Section 1.1**

```
o = golden_sec(f, 1, 2, 0.02);
fprintf("Golden Section\n")
for row=1:size(o,1)
    fprintf("k = %i,\t ak = %0.12f,\t bk = %0.12f,\t f(ak) = %0.12f,\t
f(bk) = %0.12f\t [%0.6f, %0.6f]\n",o(row, :))
end
% This outputs at the very bottom for some strange reason
```

## **Run Newton 1.1**

```
o = newtons(f, f1, f2, 1, 10);
fprintf("Newtons:\n")
for row=1:size(o,1)
    fprintf("k = %i,\t xk = %0.12f,\t f(xk) = %0.12f,\t f'(xk) =
%0.12f,\t f''(xk) = %0.12f\n",o(row, :))
end

Newtons:
k = 0, xk = 1.000000000000, f(xk) = 3.161209223473, f'(xk) =
-1.365883939232, f''(xk) = -0.161209223473
k = 1, xk = -7.472740639831, f(xk) = 57.330143273665, f'(xk) =
-11.232666837815, f''(xk) = 0.511709396520
```

```
k = 2, xk = 14.478520982874, f(xk) = 208.288516590770, f'(xk) = 208.288516590770
 25.187832981772, f''(xk) = 3.339053260748
k = 3, xk = 6.935115408046, f(xk) = 51.275482705508, f'(xk) = 51.275482705508
 11.443343617834, f''(xk) = -1.179656982590
k = 4, xk = 16.635684121431, f(xk) = 274.347348438923, f'(xk) = 274.347348438923
 36.472389478119, f''(xk) = 4.398637749105
k = 5, xk = 8.343937549316, f(xk) = 67.738945865403, f'(xk) = 67.738945865403
 13.158460678096, f''(xk) = 3.882347961485
k = 6, xk = 4.954632724341, f(xk) = 25.507911272968, f'(xk) =
 13.792474194376, f''(xk) = 1.040474160139
k = 7, xk = -8.301317997722, f(xk) = 67.181618377811, f'(xk) = 67.181618377811
 -12.996226008912, f''(xk) = 3.730262121486
k = 8, xk = -4.817319933871, f(xk) = 23.625525354616, f'(xk) = 23.625525354616
 -13.612639055533, f''(xk) = 1.581045990659
k = 9, xk = 3.792574487895, f(xk) = 11.201664357595, f'(xk) = 11.201664357595
 10.009019920966, f''(xk) = 5.181956888635
k = 10, xk = 1.861060942709, f(xk) = 2.318724705799, f'(xk) = 2.318724705799
 -0.110550812403, f''(xk) = 3.144823126679
```

### **Run Custom 1.1**

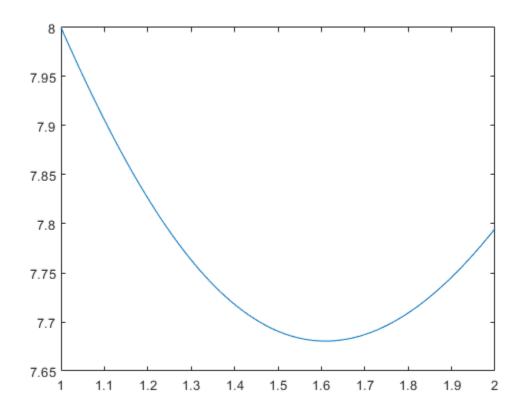
```
o = custom(f, 1, 1.5, 2, 10);
fprintf("Custom:\n")
for row=1:size(o,1)
    fprintf("k = %i, \t xk = %0.12f, \t f(xk) = % 0.12f \n", o(row, :))
end
Custom:
k = 1, xk = 2.000000000000, f(xk) = 2.335412653811
k = 2, xk = 1.979306971299, f(xk) = 2.328684216801
k = 3, xk = 1.881459171969, f(xk) = 2.317129339417
k = 4, xk = 1.896580738126, f(xk) = 2.316810354179
k = 5, xk = 1.895288900889, f(xk) = 2.316808488868
k = 6, xk = 1.895491823988, f(xk) = 2.316808419798
k = 7, xk = 1.895494223557, f(xk) = 2.316808419788
k = 8, xk = 1.895493592208, f(xk) = 2.316808419789
k = 9, xk = 1.895590080093, f(xk) = 2.316808434826
k = 10, xk = 1.895501987455, f(xk) = 2.316808419886
k = 11, xk = 1.895494500296, f(xk) = 2.316808419788
```

# Define the function we are optimizing 1.2

### Plot the function

```
x = a:0.01:b;
```

plot(x, f(x));



## **Run Golden Section 1.2**

```
o = golden sec(f, 1, 2, 0.02);
fprintf("Golden Section\n")
for row=1:size(o,1)
    fprintf("k = %i,\t ak = %0.12f,\t bk = %0.12f,\t f(ak) = %0.12f,\t
 f(bk) = %0.12f\t [%0.6f, %0.6f]\n",o(row, :))
end
Golden Section
k = 0, ak = 1.000000000000, bk = 2.00000000000, f(ak) =
 8.000000000000, f(bk) = 7.795065793291 [1.000000, 2.000000]
k = 1, ak = 1.381966011250, bk = 1.618033988750, f(ak) = 1.618033988750
 7.724695924128, f(bk) = 7.795065793291 [1.381966, 2.000000]
k = 2, ak = 1.618033988750, bk = 1.763932022500, f(ak) = 1.8180888888
 7.724695924128, f(bk) = 7.699467246802 [1.381966, 1.763932]
k = 3, ak = 1.527864045000, bk = 1.618033988750, f(ak) = 1.618033988750
 7.686003353484, f(bk) = 7.699467246802 [1.527864, 1.763932]
k = 4, ak = 1.618033988750, bk = 1.673762078751, f(ak) = 1.673762078751
 7.686003353484, f(bk) = 7.683813693632 [1.527864, 1.673762]
k = 5, ak = 1.583592135001, bk = 1.618033988750, f(ak) = 1.618033988750
 7.680996340185, f(bk) = 7.683813693632 [1.583592, 1.673762]
k = 6, ak = 1.618033988750, bk = 1.639320225002, f(ak) = 1.639320225002
 7.680996340185, f(bk) = 7.681179501562 [1.583592, 1.639320]
```

```
k = 7, ak = 1.604878371253, bk = 1.618033988750, f(ak) = 7.680996340185, f(bk) = 7.680507437210 [1.583592, 1.618034] k = 8, ak = 1.596747752498, bk = 1.604878371253, f(ak) = 7.680577644873, f(bk) = 7.680507437210 [1.596748, 1.618034] k = 9, ak = 1.604878371253, bk = 1.609903369994, f(ak) = 7.680462600136, f(bk) = 7.680507437210 [1.604878, 1.618034]
```

#### Run Newton 1.2

```
o = newtons(f, f1, f2, 1, 10);
fprintf("Newtons:\n")
for row=1:size(o,1)
    fprintf("k = %i, \t xk = %0.12f, \t f(xk) = %0.12f, \t f'(xk) =
0.12f, \t f''(xk) = 0.12fn", o(row, :))
end
Newtons:
k = 0, xk = 1.000000000000, f(xk) = 8.00000000000, f'(xk) =
-1.000000000000, f''(xk) = 1.00000000000
k = 1, xk = 2.000000000000, f(xk) = 7.795065793291, f'(xk) =
 0.556964470628, f''(xk) = 1.193035529372
k = 2, xk = 1.533153492150, f(xk) = 7.685300898722, f'(xk) =
 -0.128260959094, f''(xk) = 1.715999639124
k = 3, xk = 1.607897656524, f(xk) = 7.680447702719, f'(xk) =
 -0.002444130364, f''(xk) = 1.648375432610
k = 4, xk = 1.609380407550, f(xk) = 7.680445890164, f'(xk) =
 -0.000001087244, f''(xk) = 1.646908206850
k = 5, xk = 1.609381067723, f(xk) = 7.680445890163, f'(xk) = 1.680445890163
 -0.000000000000, f''(xk) = 1.646907552651
k = 6, xk = 1.609381067723, f(xk) = 7.680445890163, f'(xk) =
 0.000000000000, f''(xk) = 1.646907552651
k = 7, xk = 1.609381067723, f(xk) = 7.680445890163, f'(xk) =
 0.0000000000000, f''(xk) = 1.646907552651
k = 8, xk = 1.609381067723, f(xk) = 7.680445890163, f'(xk) =
 0.0000000000000, f''(xk) = 1.646907552651
k = 9, xk = 1.609381067723, f(xk) = 7.680445890163, f'(xk) =
 0.000000000000, f''(xk) = 1.646907552651
k = 10, xk = 1.609381067723, f(xk) = 7.680445890163, f'(xk) = 10.680445890163
 0.0000000000000, f''(xk) = 1.646907552651
```

#### **Run Custom 1.2**

```
k = 5, xk = 1.609376284453, f(xk) = 7.680445890182

k = 6, xk = 1.609381486522, f(xk) = 7.680445890164

k = 7, xk = 1.609380785503, f(xk) = 7.680445890163

k = 8, xk = 1.609224213561, f(xk) = 7.680445910424

k = 9, xk = 1.609381792856, f(xk) = 7.680445890164

k = 10, xk = 1.609380628483, f(xk) = 7.680445890164

k = 11, xk = 1.609381906066, f(xk) = 7.680445890164
```

## **Helper Function**

```
function out = golden_sec(f, a, b, eps)
            k = 0;
            out = [k, a, b, f(a), f(b), a, b]; % array of output
            ro = (3 - sqrt(5))/2;
            while (b - a) >= eps
                          k = k + 1;
                          a1 = a + ro * (b - a);
                          b1 = b - ro * (b - a);
                          fal = f(al); % can store these to re-compute
                          fb1 = f(b1);
                          if fa1 > fb1
                                       a = a1;
                          else
                                       b = b1;
                          end
                          out = [out ; [k, a1, b1, f(a), f(b), a, b]];
                          f(k) = i, t = 0.12f, t = 0.12f,
  0.12f, f(bk) = 0.12f [0.6f, 0.6f] \n", k, al, bl, fal, fbl, a,
  b)
             end
end
function out = newtons(f, f1, f2, x, iter)
            k = 0;
            out = [k, x, f(x), f1(x), f2(x)];
             for i = 1:iter
                          k = k + 1;
                         x = x - f1(x)/f2(x);
                          out = [out ; [k, x, f(x), f1(x), f2(x)]];
             end
end
function out = custom(f, x0, x1, x2, iter)
            k = 3;
            x = [x0, x1, x2];
            out = [k - 2, x(k), f(x(k))];
             for i = 1:iter
                          s02 = x(k-0)^2 - x(k-2)^2;
                          s10 = x(k-1)^2 - x(k-0)^2;
                          s21 = x(k-2)^2 - x(k-1)^2;
                          d12 = x(k-1) - x(k-2);
```

```
d20 = x(k-2) - x(k-0);
d01 = x(k-0) - x(k-1);
num = -f(x(k-1))*s02 - f(x(k-2)) * s10 - f(x(k)) * s21;
den = f(x(k)) * d12 + f(x(k-1)) * d20 + f(x(k-2)) * d01;
x(k+1) = num / (2 * den);
k = k + 1;
out = [out ; [k - 2, x(k), f(x(k))]];
end
end
Golden Section
k = 0, ak = 1.000000000000, bk = 2.00000000000, f(ak) = 3.161209223473, f(bk) = 2.335412653811 [1.000000, 2.000000]
k = 1, ak = 1.381966011250, bk = 1.618033988750, f(ak) = 2.660670580070, f(bk) = 2.335412653811 [1.381966, 2.000000]
k = 2, ak = 1.618033988750, bk = 1.763932022500, f(ak) = 2.618033988750, f(ak) = 2.61803398750, f(ak) = 2.6180398750, f(ak) = 2.61803988750, f(ak) = 2.618039887
```

2.429153603732, f(bk) = 2.335412653811 [1.618034, 2.000000] k = 3, ak = 1.763932022500, bk = 1.854101966250, f(ak) = 2.343707268370, f(bk) = 2.335412653811 [1.763932, 2.000000] k = 4, ak = 1.854101966250, bk = 1.909830056251, f(ak) = 2.319569958647, f(bk) = 2.335412653811 [1.854102, 2.000000] k = 5, ak = 1.909830056251, bk = 1.944271909999, f(ak) = 2.319569958647, f(bk) = 2.320778769582 [1.854102, 1.944272] k = 6, ak = 1.888543819998, bk = 1.909830056251, f(ak) = 2.319569958647, f(bk) = 2.317146921623 [1.854102, 1.909830] k = 7, ak = 1.875388202502, bk = 1.888543819998, f(ak) = 2.317465461693, f(bk) = 2.317146921623 [1.875388, 1.909830] k = 8, ak = 1.888543819998, bk = 1.896674438754, f(ak) = 2.316887339366, f(bk) = 2.317146921623 [1.888544, 1.909830] k = 9, ak = 1.896674438754, bk = 1.901699437495, f(ak) = 2.316887339366, f(bk) = 2.316871642186 [1.888544, 1.901699]

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