Welcome and Introduction

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https:
//github.com/philschulz/VITutorial

About us ...

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- Sampling, VI, Machine Translation

Philip Schulz

- PhD candidate at UvA
- Applied Scientist at Amazon
- ▶ VI, Machine Translation, Bayesian Models

Problems

Supervised problems: "learn a distribution over observed data"

sentences in natural language, images, videos, . . .

Unsupervised problems: "learn a distribution over observed and unobserved data"

sentences in natural language + parse trees, images + bounding boxes . . .

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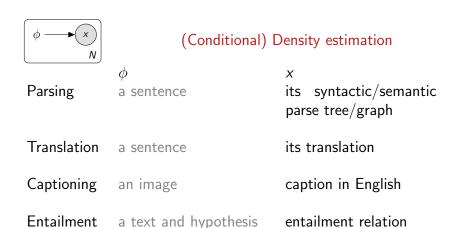
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and proceed to estimate parameters that assign maximum likelihood to observations

Multiple problems, same language



Where does deep learning kick in?

Let ϕ be all side information available e.g. deterministic *inputs/features*

Have neural networks predict parameters of our probabilistic model

$$X|\phi \sim \mathsf{Cat}(\pi_{\mathsf{w}}(\phi))$$
 or $X|\phi \sim \mathcal{N}(\mu_{\mathsf{w}}(\phi), \sigma_{\mathsf{w}}(\phi)^2)$

and proceed to estimate parameters w of the NNs

Task-driven feature extraction

Often our side information ϕ is itself some high dimensional data

- $ightharpoonup \phi$ is a sentence and x a tree
- lacktriangledown ϕ is the source sentence and x is the target
- $ightharpoonup \phi$ is an image and x is a caption

and part of the job of the NNs that parametrise our models is to also deterministically encode that input in a low-dimensional space

NN as efficient parametrisation

From the statistical point of view NNs do not generate data

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Prediction is done by a decision rule outside the statistical model

e.g. beam search

MLE via gradient-based optimisation

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Given a dataset of i.i.d. observations, SGD gives us a local optimum of the log-likelihood

DL in NLP recipe

Maximum likelihood estimation

tells you which loss to optimise (i.e. negative log-likelihood)

Automatic differentiation (backprop)

"give me a tractable forward pass and I will give you gradients"

Stochastic optimisation powered by backprop

general purpose gradient-based optimisers

Tractability is central

Likelihood gives us a differentiable objective to optimise for

but we need to stick with tractable likelihood functions

When do we have intractable likelihood?

Latent variables: assessing the likelihood requires marginalisation

too many forward passes

$$P_X(x) = \sum_{c=1}^K \mathsf{Cat}(c|\pi_1, \dots, \pi_K) \underbrace{\mathcal{N}(x|\mu_w(c), \sigma_w(c)^2)}_{\mathsf{forward\ pass}}$$

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even infinitely many

$$P_X(x) = \int \mathcal{N}(z|0, I) \underbrace{\operatorname{Cat}(x|\pi_w(z))}_{\text{forward pass}} dz$$

Can we approximate the marginal?

Beam-search

biased gradient estimates bye bye stochastic optimisation!

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Monte Carlo sampling

breaks differentiability bye bye backprop!

What do we do then?



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But what if

- we want to learn clusters?
- or segmentation?
- or sparse models?

- or latent factors?
- or learn from incomplete supervision?
- or Bayesian NNs?

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- but requires efficient inference which is the reason why we are here today