# Analysis

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# Methodology

In this section we will talk about the methodology that has been used and the different models analysis that has been conducted.

#### Traning set and Test set

First of all we started by splitting our dataset into 2 sets: **training set** (German\_credit.tr) and **test set** (German\_credit.te). We do not forget to take the first variable **OBS**. out as it represents the index number for each observation. These two sets will allow us to train some models on the **training set** and then test the accuracy of the model fit on the **test set**.

#### Balancing the dataset

Then, we applied the balancing data technique in order to improve the predictions of **Good Credit** and **Bad Credit**, since we have more observations on the **Good Credit**.

The table below reveals the unbalanced problem.

Indeed, we observe that the "Good Credit" (1) response appears **527** times in the training set and "Bad Credit" (0) **223**, two times less. Since there are many more "Good Credit" than "Bad Credit", any model favors the prediction of the "Good Credit". It results a good accuracy but the specificity is low, as well as the balanced accuracy.

**Sub-sampling** Balancing using sub-sampling consists of taking all the cases in the smallest class (here "Bad Credit") and extract at random the same amount of cases in the largest category (here "Good").

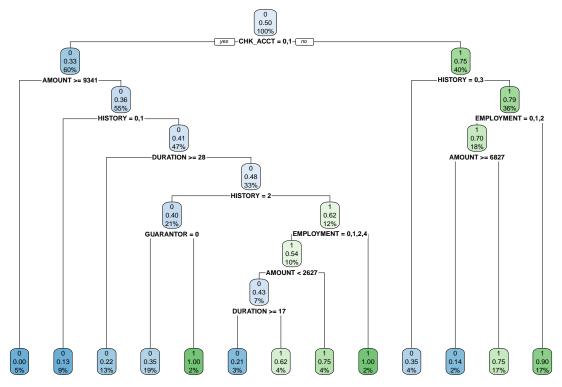
The **training set** is now balanced, we have 223 observations for both "Good Credit" (1) and "Bad Credit" (0). The new balanced training set is called German\_Credit.tr.subs.

#### **Models Fitting**

Once we had our training set and test set, we could fit some models and compare them with together to choose the best model.

1. Classification Tree (Decision Tree) We first started with a decision tree and more specifically we chose the classification tree as we want to classify the applicants. The model was build on our previously balanced training set German\_Credit.tr.subs. We used the R function rpart.

We obtained the following large tree.



We could see that among the 31 explanatory variables, this model uses 6 of them: CHK\_ACCT, AMOUNT, HISTORY, DURATION, GUARANTOR and EMPLOYMENT.

```
##
             Reference
##
  Prediction
##
               58
                    70
##
               19 103
##
            Sensitivity
                                   Specificity
                                                      Pos Pred Value
##
              0.7532468
                                     0.5953757
                                                            0.4531250
##
         Neg Pred Value
                                     Precision
                                                               Recall
               0.8442623
                                     0.4531250
                                                            0.7532468
##
##
                      F1
                                    Prevalence
                                                      Detection Rate
               0.5658537
                                                            0.2320000
##
                                     0.3080000
  Detection Prevalence
                             Balanced Accuracy
##
               0.5120000
                                     0.6743112
##
```

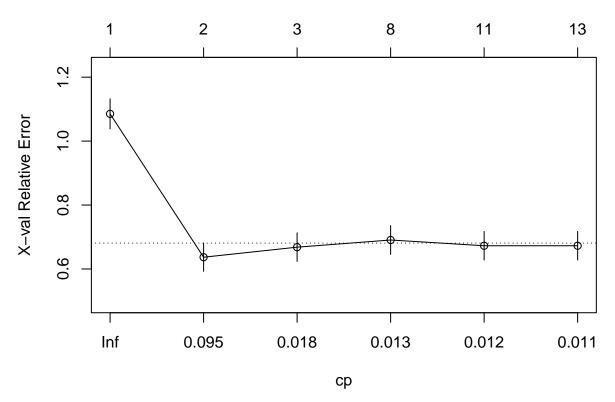
We first have an insight on how well it predict the test set (German\_credit.te). We recall that 0 means a "Bad Credit" risk and 1 means a "Good Credit" risk. It seems that it has difficulty to predict the "Bad Credit" risk applicants.

As the tree is quite big and we want to know if we can prune it. To do so, we decided to use the printcp and plotcp commands and choose the best **cp** (complexity parameter) value to prune our tree.

# Pruning the tree

```
## Root node error: 223/446 = 0.5
##
##
  n = 446
##
##
           CP nsplit rel error
                                xerror
                                            xstd
## 1 0.399103
                   0
                        1.00000 1.08520 0.047179
## 2 0.022422
                   1
                        0.60090 0.63677 0.044117
## 3 0.014574
                        0.57848 0.66816 0.044668
                   2
## 4 0.011958
                   7
                        0.48430 0.69058 0.045028
## 5 0.011211
                   10
                        0.44843 0.67265 0.044742
## 6 0.010000
                  12
                        0.42601 0.67265 0.044742
```

## size of tree

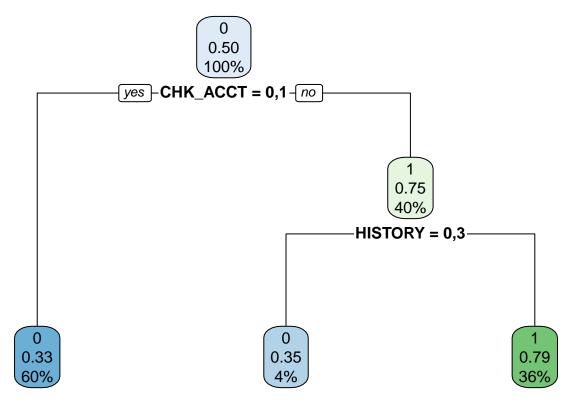


From the list of  $\mathbf{cp}$  (complexity parameter), we would choose the line that has the lowest cross validation error. This can be seen on the column **xerror**. So the best cp would be 0.022422 with one split.

From the graph, we can identify that, according to the 1-SE rule, the tree with 2 and 3 are equivalent. The tree with 3 nodes should be preferred. It appears below the dotted-line.

The value of cp can be chosen arbitrarily between 0.018 and 0.095. So we decided to go with the suggested cp of 0.022 from the summary.

With these value, we obtain a very small tree.

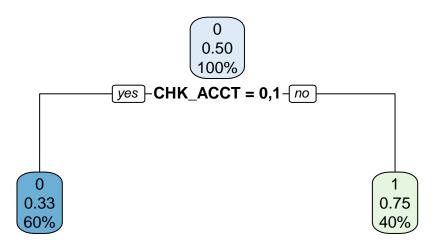


This pruned decision tree with a cp of 0.022 uses the variables  $\mathbf{CHK\_ACCT}$  and  $\mathbf{HISTORY}$ .

Using this pruned tree, we can computed the prediction and build a confusion matrix to see the performance of the model.

##	Reference		
##	Prediction 0 1		
##	0 63 95		
##	1 14 78		
##	Sensitivity	Specificity	Pos Pred Value
##	0.8181818	0.4508671	0.3987342
##	Neg Pred Value	Precision	Recall
##	0.8478261	0.3987342	0.8181818
##	F1	Prevalence	Detection Rate
##	0.5361702	0.3080000	0.2520000
##	Detection Prevalence	Balanced Accuracy	
##	0.6320000	0.6345244	

We also decided to look at what would an automatically pruned using 1-SE rule would give us and whether or not it is better than the pruned tree we made by looking at the cp.



Here, only the variable CHK\_ACCT is used. As we prune the tree more information are lost.

```
Reference
## Prediction 0 1
            0 61 88
##
            1 16 85
##
##
            Sensitivity
                                  Specificity
                                                    Pos Pred Value
                                    0.4913295
##
              0.7922078
                                                          0.4093960
##
         Neg Pred Value
                                    Precision
                                                             Recall
##
              0.8415842
                                    0.4093960
                                                          0.7922078
                                   Prevalence
##
                     F1
                                                    Detection Rate
              0.5398230
                                    0.3080000
                                                          0.2440000
##
## Detection Prevalence
                           Balanced Accuracy
                                    0.6417686
##
              0.5960000
```

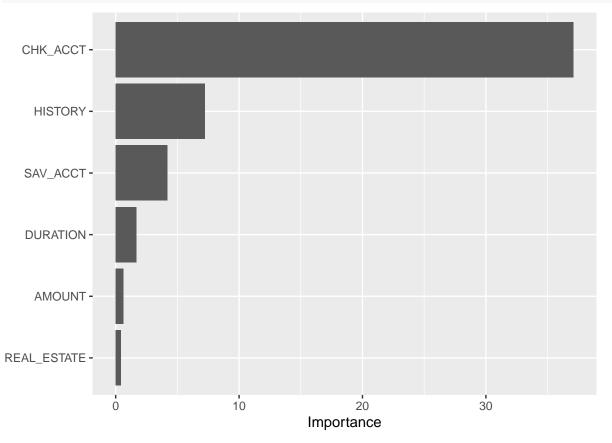
varImp(german.ct.prune)

## Variable importance of the classification tree

##		Overall
##	AMOUNT	17.947179
##	CHK_ACCT	37.098755
##	DURATION	11.073258
##	EMPLOYMENT	4.645266
##	HISTORY	18.840050
##	OTHER_INSTALL	3.216630
##	RETRAINING	3.509915
##	SAV_ACCT	9.538067
##	NEW_CAR	0.00000
##	USED_CAR	0.00000
##	FURNITURE	0.000000
##	RADIO.TV	0.000000
##	EDUCATION	0.000000
##	INSTALL_RATE	0.000000
##	MALE_DIV	0.000000
##	MALE_SINGLE	0.000000
##	MALE_MAR_or_WID	0.000000
##	CO.APPLICANT	0.00000
##	GUARANTOR	0.000000

```
## PRESENT_RESIDENT 0.000000
## REAL_ESTATE
                     0.000000
## PROP_UNKN_NONE
                     0.000000
## AGE
                     0.00000
## RENT
                     0.000000
## OWN RES
                     0.000000
## NUM_CREDITS
                     0.000000
## JOB
                     0.000000
## NUM_DEPENDENTS
                     0.000000
## TELEPHONE
                     0.000000
## FOREIGN
                     0.000000
```

vip(german.ct.prune)



From this plot, we see that the variables that influences the most are CHK\_ACCT, HISTORY, SAV\_ACCT, DURATION, AMOUNT and REAL\_ESTATE. They are not exactly the same as the one we saw above.

The variable CHK\_ACCT and HISTORY were noticed though.

2. Logistic Regression The next model we performed is a logistic regression.

```
## Coefficients:
##
                       Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                      1.1911402
                                1.7958756
                                              0.663 0.507161
## CHK ACCT1
                      0.5692882
                                 0.3363406
                                              1.693 0.090533
## CHK ACCT2
                      0.8404451
                                 0.5339512
                                             1.574 0.115485
## CHK ACCT3
                      2.4337691
                                 0.3770606
                                             6.455 1.09e-10 ***
## DURATION
                     -0.0123731
                                 0.0142153
                                            -0.870 0.384078
## HISTORY1
                     -1.0734853
                                 0.8514386
                                            -1.261 0.207384
## HISTORY2
                      0.0865599
                                 0.6747882
                                             0.128 0.897930
## HISTORY3
                     -0.0598560
                                 0.7410028
                                            -0.081 0.935619
## HISTORY4
                      1.1072483
                                 0.6576414
                                             1.684 0.092246
## NEW_CAR1
                                            -0.775 0.438096
                     -0.4538649
                                 0.5853211
## USED_CAR1
                      1.6322817
                                 0.7540134
                                             2.165 0.030404 *
                                              0.082 0.934305
## FURNITURE1
                      0.0509645
                                 0.6182782
## RADIO.TV1
                      0.5261147
                                 0.5896893
                                              0.892 0.372291
## EDUCATION1
                                 0.7499724
                      0.5441469
                                              0.726 0.468111
                                 0.6787931
                                             -0.632 0.527080
## RETRAINING1
                     -0.4293160
## AMOUNT
                     -0.0002155
                                             -2.916 0.003550 **
                                 0.0000739
## SAV ACCT1
                      0.6181742
                                 0.4475399
                                             1.381 0.167195
## SAV_ACCT2
                     -0.2531524
                                 0.5541205
                                            -0.457 0.647776
## SAV ACCT3
                      0.7292579
                                 0.6813687
                                             1.070 0.284492
## SAV_ACCT4
                                             3.351 0.000804 ***
                      1.4221687
                                 0.4243610
## EMPLOYMENT1
                      0.7574673
                                 0.7956778
                                              0.952 0.341108
## EMPLOYMENT2
                      1.4785839
                                 0.7640267
                                              1.935 0.052959
## EMPLOYMENT3
                      1.9691166
                                 0.7947873
                                              2.478 0.013229 *
## EMPLOYMENT4
                      1.8560330
                                 0.7511387
                                              2.471 0.013475 *
                                            -2.386 0.017035 *
## INSTALL_RATE
                     -0.3367533
                                 0.1411404
## MALE_DIV1
                     -0.5653453
                                 0.5705857
                                            -0.991 0.321775
                                 0.3327207
## MALE_SINGLE1
                      0.1618525
                                             0.486 0.626647
## MALE_MAR_or_WID1
                    -0.5551862
                                 0.5312986
                                            -1.045 0.296041
## CO.APPLICANT1
                     -0.6994379
                                 0.6920599
                                             -1.011 0.312179
## GUARANTOR1
                      1.7126786
                                 0.6556150
                                             2.612 0.008993 **
## PRESENT_RESIDENT2 -1.1195205
                                             -2.345 0.019008
                                 0.4773294
## PRESENT RESIDENT3 -0.2590309
                                 0.5313455
                                             -0.487 0.625904
## PRESENT_RESIDENT4 -0.9082582
                                 0.4793144
                                            -1.895 0.058104
## REAL ESTATE1
                     -0.0137202
                                 0.3384983
                                             -0.041 0.967669
## PROP_UNKN_NONE1
                     -1.4578770
                                 0.6505748
                                            -2.241 0.025032 *
## AGE
                      0.0167050
                                 0.0141041
                                             1.184 0.236255
## OTHER_INSTALL1
                     -0.6758552
                                            -1.985 0.047113 *
                                 0.3404321
## RENT1
                     -1.2066453
                                 0.8244600
                                            -1.464 0.143315
## OWN RES1
                     -0.4707135
                                 0.7665544
                                            -0.614 0.539173
## NUM CREDITS
                     -0.3634820
                                 0.3011721
                                            -1.207 0.227474
                                            -0.637 0.524069
## JOB1
                     -0.7402802
                                 1.1619781
## JOB2
                     -1.2142377
                                 1.1317833
                                            -1.073 0.283337
## JOB3
                     -1.4358446
                                 1.1604352
                                             -1.237 0.215964
                      0.1270172
## NUM_DEPENDENTS
                                 0.3832474
                                              0.331 0.740325
## TELEPHONE1
                      0.6259633
                                 0.3143236
                                              1.991 0.046430 *
## FOREIGN1
                      1.2496315
                                 0.8543880
                                             1.463 0.143576
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
```

```
## Null deviance: 618.29 on 445 degrees of freedom
## Residual deviance: 390.97 on 400 degrees of freedom
## AIC: 482.97
##
## Number of Fisher Scoring iterations: 5
```

We see that a lot of variables are not statistically significant for the model so we can think of a model reduction.

Before doing a reduction of the model, we fitted the model and predicted on the test set.

```
##
             Reference
## Prediction
                 0
                     1
##
                49
                    46
                28 127
##
             1
##
                                                       Pos Pred Value
             Sensitivity
                                   Specificity
##
               0.6363636
                                     0.7341040
                                                            0.5157895
##
         Neg Pred Value
                                     Precision
                                                               Recall
##
               0.8193548
                                     0.5157895
                                                            0.6363636
##
                                    Prevalence
                                                       Detection Rate
                      F1
##
               0.5697674
                                      0.3080000
                                                            0.1960000
## Detection Prevalence
                             Balanced Accuracy
               0.3800000
                                     0.6852338
##
```

Variable selection and interpretation with step method (AIC criteria) In order to reduce the logistic regression we used a stepwise variable selection. This has been done with the command step.

The final reduced model is as follow.

```
summary(mod.logreg.sel)
```

```
##
## Call:
   glm(formula = RESPONSE ~ CHK_ACCT + HISTORY + NEW_CAR + USED_CAR +
##
       RETRAINING + AMOUNT + SAV_ACCT + EMPLOYMENT + INSTALL_RATE +
##
       GUARANTOR + PRESENT_RESIDENT + PROP_UNKN_NONE + AGE + OTHER_INSTALL +
       RENT + TELEPHONE + FOREIGN, family = binomial, data = German_Credit.tr.subs)
##
##
## Deviance Residuals:
##
        Min
                   10
                         Median
                                        30
                                                 Max
## -2.39343 -0.68768 -0.02628
                                   0.71315
                                             2.60726
##
## Coefficients:
##
                       Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                     -0.6339113
                                 1.1570626
                                            -0.548 0.583786
## CHK_ACCT1
                      0.5970566
                                 0.3291383
                                              1.814 0.069678
## CHK_ACCT2
                      1.1123874
                                 0.5042812
                                              2.206 0.027392 *
## CHK_ACCT3
                      2.4109175
                                 0.3597629
                                              6.701 2.06e-11 ***
## HISTORY1
                     -0.6393459
                                 0.8007632
                                             -0.798 0.424626
## HISTORY2
                      0.3153810
                                 0.6295178
                                              0.501 0.616379
## HISTORY3
                                 0.7411154
                                              0.033 0.973541
                      0.0245812
                                              1.643 0.100475
## HISTORY4
                      1.0638624
                                 0.6476870
## NEW CAR1
                     -0.7159178
                                 0.3141611
                                             -2.279 0.022678 *
## USED_CAR1
                      1.3489217
                                 0.5579072
                                              2.418 0.015614 *
## RETRAINING1
                                            -1.838 0.066072 .
                     -0.8489518
                                 0.4619050
## AMOUNT
                     -0.0002631 0.0000595 -4.421 9.81e-06 ***
```

```
## SAV_ACCT1
                     0.5675624 0.4173990
                                            1.360 0.173906
## SAV_ACCT2
                    -0.0693577
                                0.5399345 -0.128 0.897788
## SAV ACCT3
                     0.5603771
                                0.6437202
                                            0.871 0.384011
## SAV_ACCT4
                     1.3592948
                                0.4069584
                                            3.340 0.000837 ***
## EMPLOYMENT1
                     0.5542570
                                0.6967423
                                            0.795 0.426324
## EMPLOYMENT2
                     1.2338686 0.6524020
                                            1.891 0.058588
## EMPLOYMENT3
                     1.7999683 0.6887566
                                            2.613 0.008966 **
## EMPLOYMENT4
                     1.5521376 0.6518729
                                            2.381 0.017264 *
## INSTALL RATE
                     -0.3278020
                                0.1249721
                                           -2.623 0.008716 **
## GUARANTOR1
                     1.6927223
                                0.6068573
                                            2.789 0.005282 **
## PRESENT_RESIDENT2 -1.1117822
                                0.4641005 -2.396 0.016595 *
## PRESENT_RESIDENT3 -0.3408387
                                0.5041109
                                           -0.676 0.498966
## PRESENT_RESIDENT4 -0.7613632
                                0.4531619 -1.680 0.092935
## PROP_UNKN_NONE1
                    -1.0532655
                                           -2.737 0.006203 **
                                0.3848454
## AGE
                     0.0181856
                                0.0128738
                                           1.413 0.157769
## OTHER_INSTALL1
                     -0.6281982
                                0.3256821
                                           -1.929 0.053747 .
## RENT1
                    -0.8736712
                                0.3412119 -2.560 0.010452 *
## TELEPHONE1
                     0.5251823
                                0.2863172
                                            1.834 0.066614
## FOREIGN1
                     1.2896516 0.8049248
                                            1.602 0.109111
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 618.29
                             on 445
                                     degrees of freedom
## Residual deviance: 403.37 on 415 degrees of freedom
  AIC: 465.37
## Number of Fisher Scoring iterations: 5
```

The variables that have been removed are: FURNITURE, RADIO.TV, EDUCATION, RETRAINING, MALE\_DIV, MALE\_SINGLE, MALE\_MAR\_or\_WID, CO.APPLICANT, REAL\_ESTATE, OWN\_RES, NUM\_CREDITS, JOB and NUM\_DEPENDENTS

In the end, we get the most significant model:

 $RESPONSE = -0.6339113 + 0.5970566 * CHK_{ACCT1} + 1.1123874 * CHK_{ACCT2} + 2.4109175 * CHK_{ACCT3} - 0.6393459 * HISTOCOMBOUNDED FOR A CHRONIC AND A CHRO$ 

$$p = (e^{RESPONSE})/(1 + e^{RESPONSE})$$

It means that:

- The predicted probability of being a good applicant for CHCK\_ACCT3 is higher than for CHK\_ACCT0 (and also higher than for CHK\_ACCT1 and CHK\_ACCT2).
- The predicted probability of being a good applicant for **HISTORY1** is lower than for **HISTORY0**.
- The predicted probability of being a good applicant for **HISTORY4** is higher than for **HISTORY0** (and also higher than for **HISTORY2** and **HISTORY3**).
- The predicted probability of being a good applicant for NEW\_CAR1 is lower than for NEW\_CAR0.
- The predicted probability of being a good applicant for USED\_CAR1 is higher than for USED CAR0.
- The predicted probability of being a good applicant for RETRAINING1 is lower than for RETRAINING0.
- AMOUNT is negatively associated with RESPONSE.

- The predicted probability of being a good applicant for SAV\_ACCT4 is higher than for SAV\_ACCT0 (and also higher than for SAV\_ACCT1 and SAV\_ACCT3).
- The predicted probability of being a good applicant for SAV\_ACCT2 lower than for SAV\_ACCT0.
- The predicted probability of being a good applicant for **EMPLOYMENT3** is higher than for **Employment0** (and also higher than for **EMPLOYMENT1**, **EMPLOYMENT2** and **EMPLOYMENT4**).
- INSTALL\_RATE is negatively associated with RESPONSE.
- The predicted probability of being a good applicant for GUARANTOR1 is higher than for GUARANTOR0.
- The predicted probability of being a good applicant for PRESENT\_RESIDENT2 is lower than for PRESENT\_RESIDENT0 (and also lower than PRESENT\_RESIDENT3 and PRESENT\_RESIDENT4).
- The predicted probability of being a good applicant for PROP\_UNKN\_NONE1 is lower than for PROP\_UNKN\_NONE0.
- AGE is positively associated with RESPONSE.
- The predicted probability of being a good applicant for **OTHER\_INSTALL1** is lower than for **OTHER\_INSTALL0**.
- The predicted probability of being a good applicant for **RENT1** is lower than for **RENT0**.
- The predicted probability of being a good applicant for TELEPHONE1 is higher than for TELE-PHONE0.
- The predicted probability of being a good applicant for FOREIGN1 is higher than for FOREIGN0.

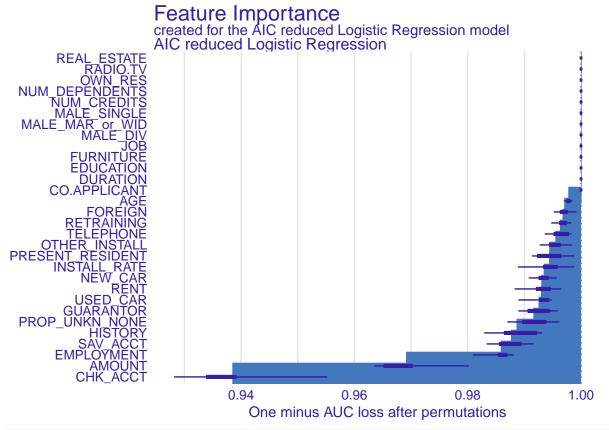
```
##
             Reference
## Prediction
                0
                    1
##
            0 50 52
            1 27 121
##
##
            Sensitivity
                                  Specificity
                                                     Pos Pred Value
##
              0.6493506
                                    0.6994220
                                                           0.4901961
##
         Neg Pred Value
                                    Precision
                                                              Recall
##
              0.8175676
                                    0.4901961
                                                           0.6493506
##
                                   Prevalence
                                                     Detection Rate
                      F1
##
              0.5586592
                                    0.3080000
                                                           0.2000000
## Detection Prevalence
                            Balanced Accuracy
##
              0.4080000
                                    0.6743863
```

#### Variable importance for logistic regression

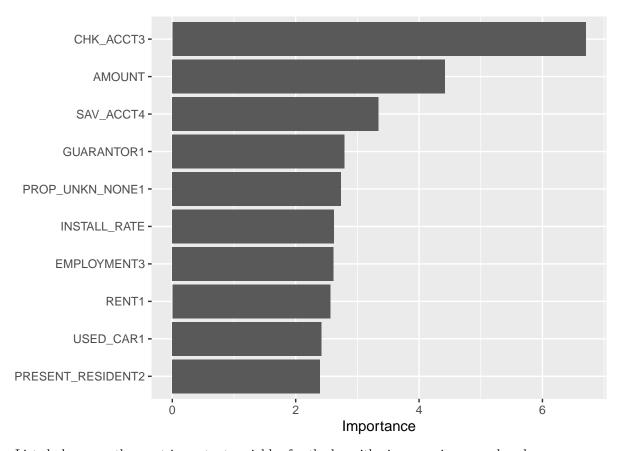
```
## Preparation of a new explainer is initiated
##
    -> model label
                         : AIC reduced Logistic Regression
##
    -> data
                            446 rows 30 cols
##
    -> target variable
                            446 values
##
    -> predict function :
                            yhat.glm will be used ( default )
                        : No value for predict function target column. ( default )
##
    -> predicted values
##
    -> model info
                            package stats , ver. 4.1.3 , task classification ( default )
    \rightarrow predicted values : numerical, min = 0.007541882 , mean = 0.5 , max = 0.9975191
##
##
    -> residual function : difference between y and yhat ( default )
                         : numerical, min = 0.05702613, mean = 1, max = 1.96659
##
    -> residuals
```

# ## A new explainer has been created!

importance\_logreg <- calculate\_importance(explainer\_logreg)
plot(importance\_logreg)</pre>



vip(mod.logreg.sel)



Listed above are the most important variables for the logarithmic regression we reduced.

**3. K-Nearest Neighbor** To perform a k-nearest neighbor method, we do not need to balance the data so we will use the unbalanced training set.

We first try to model it using a 2-NN (with Euclidean distance). Note that the model is fitting on the training set and the predictions are computed on the test set.

##	Reference		
##	Prediction 0 1		
##	0 21 45		
##	1 56 128		
##	Sensitivity	Specificity	Pos Pred Value
##	0.2727273	0.7398844	0.3181818
##	Neg Pred Value	Precision	Recall
##	0.6956522	0.3181818	0.2727273
##	F1	Prevalence	Detection Rate
##	0.2937063	0.3080000	0.0840000
## ##	Detection Prevalence 0.2640000	Balanced Accuracy 0.5063058	

The table is read as follow:

- We predicted 21 Bad credits and there were indeed 21 observed Bad credits. But the prediction misjudges 45 good credits by predicting bad credits.
- We predicted 128 Good credits as it was in fact a Good credits but 56 where predicted as Good while it
  was in fact Bad.

The prediction is not perfect. We need to try to improve the prediction by changing K at that point. Therefore, we use K=3.

```
##
             Reference
## Prediction
                0
                     1
##
            0
               14 28
            1 63 145
##
##
            Sensitivity
                                   Specificity
                                                      Pos Pred Value
##
               0.1818182
                                     0.8381503
                                                           0.3333333
         Neg Pred Value
##
                                     Precision
                                                              Recall
##
               0.6971154
                                     0.3333333
                                                           0.1818182
                      F1
##
                                    Prevalence
                                                      Detection Rate
##
               0.2352941
                                     0.3080000
                                                           0.0560000
## Detection Prevalence
                            Balanced Accuracy
##
               0.1680000
                                     0.5099842
```

The table is read as follow:

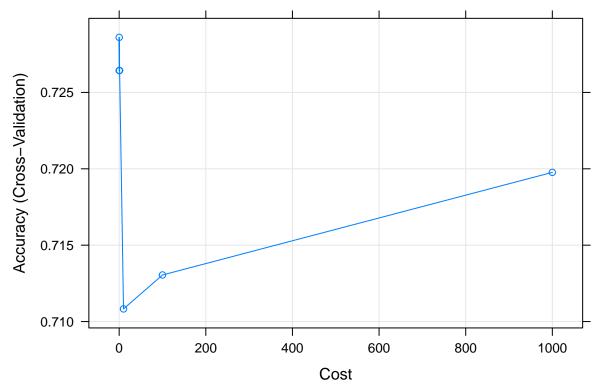
- We predicted 14 Bad credits and they were indeed observed Bad credits. But the prediction misjudges 28 good credits by predicting bad credits.
- We predicted 145 Good credits as it was in fact a Good credits but 6 where predicted as Good while it
  was in fact Bad.
- 4. Linear Support Vector Machine The next model is the linear Support Vector Machine.

```
##
## Call:
## svm(formula = RESPONSE ~ ., data = German_Credit.tr.subs, kernel = "linear")
##
##
## Parameters:
##
      SVM-Type: C-classification
##
    SVM-Kernel:
                 linear
##
          cost:
                 1
##
## Number of Support Vectors:
                                246
##
             Reference
## Prediction
                0
                    1
               50 50
##
            1 27 123
##
                                                     Pos Pred Value
##
            Sensitivity
                                  Specificity
##
              0.6493506
                                     0.7109827
                                                           0.5000000
##
         Neg Pred Value
                                     Precision
                                                              Recall
              0.8200000
                                     0.5000000
##
                                                           0.6493506
##
                      F1
                                   Prevalence
                                                      Detection Rate
##
              0.5649718
                                     0.3080000
                                                           0.2000000
## Detection Prevalence
                            Balanced Accuracy
##
              0.4000000
                                     0.6801667
```

Tunning the hyperparameters of Linear SVM We want to select the good hyperparameters for our linear SVM.

```
## Support Vector Machines with Linear Kernel
##
## 446 samples
```

```
30 predictor
##
    2 classes: '0', '1'
##
## No pre-processing
## Resampling: Cross-Validated (10 fold)
## Summary of sample sizes: 402, 400, 402, 401, 402, 402, ...
## Resampling results:
##
##
     Accuracy
                Kappa
##
     0.7264361 0.4530209
##
## Tuning parameter 'C' was held constant at a value of 1
We see that we have a good accuracy (0.72).
## Support Vector Machines with Linear Kernel
##
## 446 samples
  30 predictor
    2 classes: '0', '1'
##
##
## No pre-processing
## Resampling: Cross-Validated (10 fold)
## Summary of sample sizes: 402, 400, 402, 401, 402, 402, ...
## Resampling results across tuning parameters:
##
##
            Accuracy
                       Kappa
##
     1e-02 0.7264339 0.4532044
##
     1e-01 0.7286056 0.4575791
     1e+00 0.7264361 0.4530209
##
##
     1e+01 0.7108278 0.4216992
##
     1e+02 0.7130501 0.4261940
##
     1e+03 0.7197672 0.4397558
##
## Accuracy was used to select the optimal model using the largest value.
## The final value used for the model was C = 0.1.
```



```
Reference
##
## Prediction
                 0
                49
                   49
##
##
             1
                28 124
##
             Sensitivity
                                   Specificity
                                                      Pos Pred Value
##
               0.6363636
                                     0.7167630
                                                            0.5000000
##
         Neg Pred Value
                                     Precision
                                                               Recall
##
               0.8157895
                                     0.5000000
                                                            0.6363636
##
                      F1
                                    Prevalence
                                                      Detection Rate
##
               0.5600000
                                     0.3080000
                                                            0.1960000
## Detection Prevalence
                             Balanced Accuracy
               0.3920000
                                     0.6765633
##
```

# 5. Radial Basis Support Vector Machine We try now with a radial basis kernel (the default).

```
German_credit.rbsvm <- svm(RESPONSE ~ ., data=German_Credit.tr.subs, kernel="radial")
German_credit.rbsvm</pre>
```

```
##
## svm(formula = RESPONSE ~ ., data = German_Credit.tr.subs, kernel = "radial")
##
##
##
  Parameters:
##
      SVM-Type:
                 C-classification
##
    SVM-Kernel:
                 radial
##
          cost:
##
## Number of Support Vectors:
```

```
German_credit.rbsvm.pred <- predict(German_credit.rbsvm,</pre>
                                    newdata = German credit.te)
cm_rbsvm <- confusionMatrix(data=German_credit.rbsvm.pred,</pre>
                            reference = German_credit.te$RESPONSE )
cm_rbsvm$table
##
             Reference
## Prediction
               0
               54 52
            1 23 121
##
cm_rbsvm$byClass
##
            Sensitivity
                                 Specificity
                                                   Pos Pred Value
##
              0.7012987
                                   0.6994220
                                                         0.5094340
##
         Neg Pred Value
                                   Precision
                                                            Recall
##
              0.8402778
                                   0.5094340
                                                         0.7012987
##
                     F1
                                  Prevalence
                                                    Detection Rate
##
              0.5901639
                                   0.3080000
                                                         0.2160000
## Detection Prevalence
                           Balanced Accuracy
              0.4240000
                                   0.7003603
Tunning the hyperparameters of Radial basis SVM
## Support Vector Machines with Radial Basis Function Kernel
##
## 446 samples
##
   30 predictor
##
     2 classes: '0', '1'
##
## No pre-processing
## Resampling: Cross-Validated (10 fold)
## Summary of sample sizes: 402, 400, 402, 401, 402, 402, ...
## Resampling results across tuning parameters:
##
##
     sigma C
                  Accuracy
                             Kappa
##
     0.01
                  0.7309289
                             0.4618150
               1
##
     0.01
              10 0.6971476 0.3942416
##
     0.01
             100
                  0.6907708 0.3814209
##
     0.01
             500
                  0.6975889
                             0.3950572
##
     0.01
            1000
                  0.6975889 0.3950572
##
     0.02
               1 0.7309816 0.4620420
##
     0.02
             10
                  0.6972925 0.3946754
##
     0.02
             100
                  0.7064273
                             0.4127482
##
     0.02
             500
                  0.7064273 0.4127482
##
     0.02
            1000 0.7064273 0.4127482
##
                  0.7038647 0.4085756
     0.05
               1
##
     0.05
              10
                  0.6860299
                             0.3726705
##
     0.05
                  0.6860299 0.3726705
             100
##
     0.05
             500 0.6860299 0.3726705
##
     0.05
            1000
                  0.6860299
                             0.3726705
##
     0.10
              1
                  0.6588603
                             0.3190546
```

##

0.10

10 0.6611792 0.3234506

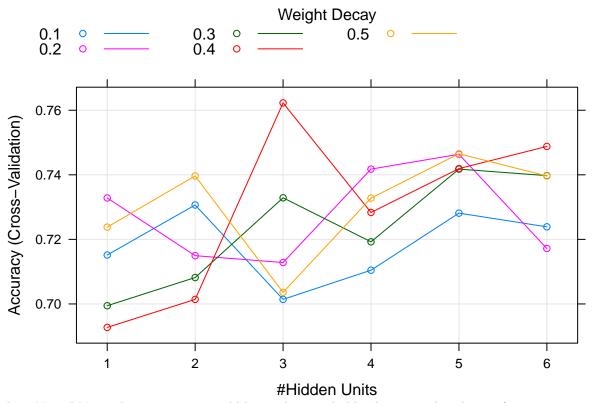
```
100 0.6611792 0.3234506
##
     0.10
##
     0.10
             500
                   0.6611792 0.3234506
     0.10
##
             1000 0.6611792 0.3234506
##
## Accuracy was used to select the optimal model using the largest value.
## The final values used for the model were sigma = 0.02 and C = 1.
                                              Sigma
   0.01
          0
                            0.02
                                                     0.05
                                                                              0.1
                                                                                   0
Accuracy (Cross-Validation)
    0.72
    0.70
    0.68
    0.66
                                        400
                                                                                 1000
              0
                           200
                                                      600
                                                                    800
                                              Cost
     sigma C
## 6 0.02 1
German_credit.rbsvm.tuned <- svm(RESPONSE ~ .,data = German_Credit.tr.subs,</pre>
                                   kernel = "radial",
                                   gamma = svm_Radial_Grid$bestTune$sigma,
                                   cost = svm_Radial_Grid$bestTune$C)
German_credit.rbsvm.tuned.pred <- predict(German_credit.rbsvm.tuned,</pre>
                                             newdata = German_credit.te)
cm_rbsvm_tuned <- confusionMatrix(data=German_credit.rbsvm.tuned.pred,</pre>
                                    reference = German_credit.te$RESPONSE)
cm_rbsvm_tuned$table
              Reference
##
## Prediction
                 0
                    1
##
                54 53
                23 120
```

## Sensitivity Specificity Pos Pred Value

cm\_rbsvm\_tuned\$byClass

##	0.7012987	0.6936416	0.5046729
##	Neg Pred Value	Precision	Recall
##	0.8391608	0.5046729	0.7012987
##	F1	Prevalence	Detection Rate
##	0.5869565	0.3080000	0.2160000
##	Detection Prevalence	Balanced Accuracy	
##	0.4280000	0.6974702	

**6. Neural Network - Simple hyperparameter tuning** To select the good parameters, we build a search grid and fit the model with each possible value in the grid. This is brute force and time consuming. The best model is selected among all the possible choices.



best Neural Networks parameters would be to choose 3 hidden layers, with a decay of 0.4.

The

##	Reference		
##	Prediction 0 1		
##	0 52 53		
##	1 25 120		
##	Sensitivity	Specificity	Pos Pred Value
##	0.6753247	0.6936416	0.4952381
##	Neg Pred Value	Precision	Recall
##	0.8275862	0.4952381	0.6753247
##	F1	Prevalence	Detection Rate
##	0.5714286	0.3080000	0.2080000
##	Detection Prevalence	Balanced Accuracy	
##	0.4200000	0.6844831	

7. Gradient Boosting The Gradient Boosting model accepts only numerical values so we have some transformation to do on our data in order to use it.

```
## ##### xgb.Booster
## raw: 31.2 Mb
## call:
     xgb.train(params = xgb_params, data = xgb_train, nrounds = 5000,
##
##
       verbose = 1)
## params (as set within xgb.train):
     booster = "gbtree", eta = "0.01", max_depth = "8", gamma = "4", subsample = "0.75", colsample_bytr
## xgb.attributes:
##
    niter
## callbacks:
     cb.print.evaluation(period = print_every_n)
## # of features: 46
## niter: 5000
## nfeatures : 46
Here we have an accuracy of 68.4%. It is good but there is room for improvement.
##
             Reference
## Prediction
                0
                    1
##
            0 57 59
            1 20 114
##
            Sensitivity
                                  Specificity
                                                     Pos Pred Value
##
##
              0.7402597
                                    0.6589595
                                                          0.4913793
##
         Neg Pred Value
                                    Precision
                                                             Recall
##
              0.8507463
                                    0.4913793
                                                          0.7402597
##
                                   Prevalence
                                                     Detection Rate
##
              0.5906736
                                    0.3080000
                                                          0.2280000
## Detection Prevalence
                            Balanced Accuracy
##
              0.4640000
                                    0.6996096
Cross-validation with caret The 10-CV can be easily obtained from caret.
First, set up the splitting data method using the trainControl function.
## Generalized Linear Model with Stepwise Feature Selection
##
## 750 samples
##
  30 predictor
     2 classes: '0', '1'
##
## No pre-processing
## Resampling: Cross-Validated (10 fold)
## Summary of sample sizes: 674, 676, 675, 675, 675, 675, ...
## Resampling results:
##
##
     Accuracy
                Kappa
     0.7479834 0.3632119
##
## Confusion Matrix and Statistics
##
##
             Reference
               0
## Prediction
                    1
            0 35 23
            1 42 150
##
```

Accuracy: 0.74

## ##

```
95% CI: (0.681, 0.7932)
##
##
       No Information Rate: 0.692
       P-Value [Acc > NIR] : 0.05592
##
##
##
                     Kappa: 0.3452
##
   Mcnemar's Test P-Value: 0.02557
##
##
##
               Sensitivity: 0.4545
               Specificity: 0.8671
##
##
            Pos Pred Value: 0.6034
            Neg Pred Value: 0.7812
##
##
                Prevalence: 0.3080
            Detection Rate: 0.1400
##
##
      Detection Prevalence: 0.2320
##
         Balanced Accuracy: 0.6608
##
##
          'Positive' Class: 0
##
```

Bootstrap with 10 replicates We now apply the bootstrap with 10 replicates. Like for CV, we use caret.

The approach is the same as before. We only need to change the method in the **trainControl** function. The corresponding method is "boot632".

100 replicates is veryyyy long to run... can do that on less sample?? I put 10, takes 3 minutes for me

```
## Generalized Linear Model with Stepwise Feature Selection
##
## 750 samples
##
   30 predictor
     2 classes: '0', '1'
##
##
## No pre-processing
## Resampling: Bootstrapped (10 reps)
## Summary of sample sizes: 750, 750, 750, 750, 750, 750, ...
## Resampling results:
##
##
     Accuracy
                Kappa
     0.7544188 0.3893564
##
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction
                0
               35
                   23
##
##
               42 150
##
##
                  Accuracy: 0.74
                    95% CI: (0.681, 0.7932)
##
##
       No Information Rate: 0.692
##
       P-Value [Acc > NIR] : 0.05592
##
##
                     Kappa: 0.3452
##
   Mcnemar's Test P-Value: 0.02557
##
```

## Sensitivity: 0.4545 ## Specificity: 0.8671 ## ## Pos Pred Value : 0.6034 Neg Pred Value : 0.7812 ## ## Prevalence: 0.3080 ## Detection Rate: 0.1400 Detection Prevalence : 0.2320 ## ## Balanced Accuracy: 0.6608 ## ## 'Positive' Class : 0 ##

# Review of statistics

Once all the models were modelized we have to compare them according to their scores and metrics. Below we summarized all their accuracy into one table.

Table 1: Scores of the models

Big				AIC re-	Linear	Tuned	Radial	Tuned		
clas-	Pruned	Autopru	ine	duced	sup-	linear	base	radial	Hyperparar	neter
sifi-	classi-	classi-	Logistic	c Logis-	$\operatorname{port}$	support	$\operatorname{support}$	base	tuned	
ca-	fica-	fica-	re-	$\operatorname{tic}$	vector	vector	vector	$\operatorname{support}$	neural	Gradient
tion	tion	tion	gres-	regres-	ma-	ma-	ma-	vector	network 3	Boost-
tree	tree	tree	sion	sion	chine	chine	chine	machine	nodes	ing
Accur <b>ac</b> §440	0.5640	0.5840	0.7040	0.6840	0.6920	0.6920	0.7000	0.6960	0.6880	0.6840
Kappa0.2945	0.2083	0.2251	0.3479	0.3200	0.3328	0.3283	0.3628	0.3564	0.3352	0.3500
Accur <b>ac58</b> 26v	e0.5001	0.5202	0.6432	0.6224	0.6307	0.6307	0.6391	0.6349	0.6266	0.6224
Accur <b>acy@3</b> p	e0.6264	0.6458	0.7599	0.7411	0.7486	0.7486	0.7561	0.7524	0.7449	0.7411
Accur <b>0c6920</b> 11	0.6920	0.6920	0.6920	0.6920	0.6920	0.6920	0.6920	0.6920	0.6920	0.6920
Accur <b>0c9F52</b> a	l <b>1e</b> 0000	0.9999	0.3690	0.6369	0.5308	0.5308	0.4219	0.4762	0.5847	0.6369
Mcner <b>0a0700</b> a	1 <b>0</b> e0000	0.0000	0.0481	0.0069	0.0122	0.0227	0.0012	0.0009	0.0022	0.0000

Another table is done to compare the KNN because they were not performed on the balanced dataset.

Table 2: Scores of the KNN models

	2-Nearest neighbor	3-Nearest neighbor
Accuracy	0.5960	0.6360
Kappa	0.0131	0.0229
AccuracyLower	0.5323	0.5730
AccuracyUpper	0.6574	0.6957
AccuracyNull	0.6920	0.6920
AccuracyPValue	0.9995	0.9752
McnemarPValue	0.3197	0.0004