Part One: Backward Elimination

a. The best model for the IQ data set uses Test1, Test2 and Test4 as shown below

```
Step: AIC=71.69
IQ ~ Test1 + Test2 + Test4
       Df Sum of Sq
                     RSS
                             AIC
                    1047.0 71.685
<none>
- Test2 1
             406.25 1453.3 74.603
- Test1 1
            415.39 1462.4 74.697
- Test4 1
             484.13 1531.2 75.386
call:
lm(formula = IQ ~ Test1 + Test2 + Test4, data = IQ)
Coefficients:
(Intercept)
                 Test1
                              Test2
                                           Test4
    90.733
                 -1.965
                             -1.649
                                           3.789
```

b. The adjusted R² value is 0.2158. This represents a modification that is supposed to take into account the number of terms in the model.

```
> fitbest = lm(IQ ~ Test1 + Test2 + Test4, data = IQ)
> summary(fitbest)
call:
lm(formula = IQ ~ Test1 + Test2 + Test4, data = IQ)
Residuals:
    Min
                 Median
                               3Q
              1Q
                                       Max
-10.9184 -6.8179 -0.9142 4.3920 21.1950
Coefficients:
           Estimate Std. Error t value Pr(>|t|)
(Intercept) 90.7327 12.8272 7.073 2.06e-05 ***
            -1.9650
                       0.9406 -2.089 0.0607 .
Test1
            -1.6485
                       0.7980 -2.066 0.0632 .
Test2
                                2.255 0.0455 *
Test4
            3.7890
                        1.6801
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 9.756 on 11 degrees of freedom
Multiple R-squared: 0.3839,
                              Adjusted R-squared:
F-statistic: 2.284 on 3 and 11 DF, p-value: 0.1356
```

c.

- All other things being equal, a higher score on the Test1 reduces IQ rating
- All other things being equal, an increase in Test2 scores reduces IQ rating
- All other things being equal, a higher score on the Test4 increases IQ rating

•

Part Two: ALL THREE

Backward Elimination

```
Step: AIC=213.38
Y \sim X2 + X4 + X6 + X10 + X11 + X12
       Df Sum of Sq
                         RSS
<none>
                         608 213.38
                         618 213.63
- X11
                 11
- X2
        1
                 14
                         622 214.33
                      24360 683.83
- X10
        1
              23753
             247389 247996 980.85
- X12
        1
           444955 445563 1055.85
3278411 3279019 1311.33
- X4
        1
- X6
        1
call:
lm(formula = Y \sim X2 + X4 + X6 + X10 + X11 + X12, data = stepwiseRegression)
Coefficients:
                                                              X10
                                                                                         X12
(Intercept)
                      X2
                                    X4
                                                  х6
                                                                            x11
 1410.27177
                -0.06975
                                             5.98660
                                                        -11.97829
                                                                                   -25.98121
                               2.80806
                                                                       -0.13102
```

Forward Selection

```
Step: AIC=213.38
Y \sim X6 + X4 + X12 + X10 + X2 + X11
      Df Sum of Sq
                     RSS
                    607.73 213.38
<none>
            6.0187 601.71 214.11
+ X7
            4.7325 602.99 214.38
+ X5
        1
+ X3
       1
            3.2840 604.44 214.69
+ X9
       1
            2.6094 605.12 214.83
            2.1408 605.58 214.93
+ X8
       1
            0.6137 607.11 215.25
+ X1
       1
call:
lm(formula = Y \sim X6 + X4 + X12 + X10 + X2 + X11, data = stepwiseRegression)
Coefficients:
(Intercept)
                     Хб
                                  X4
                                               X12
                                                            X10
                                                                          X2
                                                                                      X11
1410.27177
                5.98660
                             2.80806
                                         -25.98121
                                                      -11.97829
                                                                    -0.06975
                                                                                 -0.13102
```

Both

```
Step: AIC=213.38
Y \sim X6 + X4 + X12 + X10 + X2 + X11
       Df Sum of Sq
                        RSS
<none>
                        608 213.38
- X11
                        618
                            213.63
       1
                 11
+ X7
                        602 214.11
       1
                 6
                            214.33
- X2
                        622
       1
                 14
                        603
                            214.38
+ X5
       1
                 5
+ X3
       1
                 3
                        604 214.69
+ X9
       1
                  3
                        605 214.83
+ X8
                        606 214.93
       1
                        607
+ X1
                 1
                            215.26
       1
             23753
                     24360
- X10
                            683.83
       1
- X12
       1
            247389 247996 980.85
             444955 445563 1055.85
- X4
       1
- X6
       1 3278411 3279019 1311.33
lm(formula = Y \sim X6 + X4 + X12 + X10 + X2 + X11, data = stepwiseRegression)
Coefficients:
(Intercept)
                      х6
                                              X12
                                                            X10
                                                                          X2
                                                                                      X11
1410.27177
                 5.98660
                              2.80806
                                         -25.98121
                                                      -11.97829
                                                                    -0.06975
                                                                                 -0.13102
```

- a. All the final models from the 3 stepwise regression types are exactly the same.
- b. An increase in predictor variables x4 and x6 cause an increase in Y, while a an increase in predictor variables x2, x10, x11 and x12 causes a decrease in response variable Y
- c. These variables account for 99% of the variation in Y

```
> fitsome <- lm(formula = Y \sim X2 + X4 + X6 + X10 + X11 + X12, data = stepwiseRegression)
> summary(fitsome)
call:
lm(formula = Y \sim X2 + X4 + X6 + X10 + X11 + X12, data = stepwiseRegression)
Residuals:
   Min
             1Q Median
                             3Q
-5.3190 -1.7438 -0.0897 1.7094 5.3882
Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept) 1.410e+03 1.320e+01 106.815 <2e-16 ***
            -6.975e-02 4.158e-02 -1.677 0.0961 .
X2
            2.808e+00 9.434e-03 297.644
5.987e+00 7.410e-03 807.924
-1.198e+01 1.742e-01 -68.769
                                             <2e-16 ***
X4
                                              <2e-16 ***
Х6
                                             <2e-16 ***
X10
X11
            -1.310e-01 8.950e-02 -1.464 0.1458
            -2.598e+01 1.171e-01 -221.937 <2e-16 ***
X12
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
Residual standard error: 2.241 on 121 degrees of freedom
Multiple R-squared: 0.9999, Adjusted R-squared: 0.9998
F-statistic: 1.385e+05 on 6 and 121 DF, p-value: < 2.2e-16
```