## Fitting joint model for longitudinal ordinal and multistate process in INLA

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You will need packages mstate, haven, INLAjoint, and INLA.

```
#read packages necessary to run this analysis
library(mstate)

## Loading required package: survival
library(haven)

## Warning: package 'haven' was built under R version 4.2.2
library(INLA)
library(INLAjoint)
```

The first step is to obtain data for multistate model in the right format. For that we use the *mstate* package in R and its functions.

```
#converting imported dataset into a data frame in R to avoid errors later
ms cvd mortality=as.data.frame(ms cvd mortality)
#defining matrix for state transitions
tmat <- matrix(NA, 3, 3)</pre>
tmat[1, 2:3] <- 1:2
tmat[2, 3] <- 3
tmat
##
        [,1] [,2] [,3]
## [1,]
          NA 1
## [2,]
          NA
               NA
                     3
## [3,]
          NA
               NA
                    NA
#the dimension names of our matrix will be healthy, nonfatal CVD and death
 dimnames(tmat) <- list(from = c("healthy", "nonfatal CVD", "CVD death"), to</pre>
= c("healthy",
                  "nonfatal CVD", "CVD death"))
tmat
```

```
##
                  to
## from
                   healthy nonfatal CVD CVD death
##
     healthy
                        NA
                                       1
                                                  2
                                                  3
##
     nonfatal CVD
                        NA
                                      NA
     CVD death
                                                 NA
##
                        NA
                                      NΑ
#defining transition matrix
tmat \leftarrow transMat(x = list(c(2, 3), c(3), c()), names = c("healthy", "nonfatal")
CVD", "CVD death"))
tmat
##
## from
                   healthy nonfatal CVD CVD death
     healthy
                        NA
                                       1
                                                  3
##
     nonfatal CVD
                        NA
                                      NA
##
     CVD death
                        NA
                                      NA
                                                 NA
#specifying that transitions are for illness to death model
tmat <- trans.illdeath(names = c("healthy", "nonfatal CVD", "CVD death"))</pre>
tmat
##
## from
                   healthy nonfatal CVD CVD death
                                                  2
##
     healthy
                        NA
                                       1
     nonfatal CVD
                                                  3
##
                        NA
                                      NA
##
     CVD death
                        NA
                                      NA
                                                 NA
paths(tmat)
##
        [,1] [,2] [,3]
## [1,]
           1
               NA
                     NA
## [2,]
           1
                 2
                     NA
## [3,]
                 2
                      3
           1
           1
                     NΑ
## [4,]
#getting data for multistate model
covs <- c("female", "ili", "takes_ins", "Diab_Dur", "cvd_his", "bmi_bas", "bl</pre>
ack", "hispan", "other_race", "native",
          "b_age10")
ms_cvdmortality <- msprep(time = c(NA, "fu_nonfatal_cvd_years", "fu_cvd_death</pre>
_years"), status = c(NA, "nonfatal_cvd_event",
"CVD death"),
                        data = ms_cvd_mortality, trans = tmat, keep = covs, id
="sid")
#checking how many subjects transitioned into each of the states
events(ms_cvdmortality) #do not take out other race and native from any trans
ition
```

```
## $Frequencies
##
                 to
                  healthy nonfatal CVD CVD death no event total entering
## from
##
     healthy
                        0
                                   708
                                               65
                                                      4081
                                                                     4854
     nonfatal CVD
                        0
                                               34
                                                       674
                                                                       708
##
                                     0
     CVD death
                        0
                                      0
                                                0
                                                        99
                                                                       99
##
##
## $Proportions
##
                 to
## from
                     healthy nonfatal CVD CVD death
                                                        no event
##
     healthy
                  0.00000000
                               0.14585909 0.01339102 0.84074990
     nonfatal CVD 0.00000000
                               0.00000000 0.04802260 0.95197740
##
##
     CVD death
                  0.00000000
                               0.00000000 0.00000000 1.00000000
       ID variable must be converted to an integer
ms cvdmortality$id=as.integer(ms cvdmortality$sid)
```

More information about the multistate package and its functions and uses can be found in de Wreede LC., Fiocco M, Putter H. mstate: An R package for the analysis of competing risks and Multi-State Models. Journal of Statistical Software; 2011, 38(7).

```
###### separate data for each transition, this will be necessary later, when
specifying model in INLA
transition1=ms_cvdmortality[ms_cvdmortality$trans==1, ]
transition2=ms_cvdmortality[ms_cvdmortality$trans==2, ]
transition3=ms_cvdmortality[ms_cvdmortality$trans==3, ]
```

The following steps should be followed to get data into a format accepted by *INLA and INLAjoint* packages. These steps are closely following instructions for the *INLAjoint* package that can be found at

https://github.com/DenisRustand/INLAjoint/blob/main/vignettes/INLAjoint.pdf

```
## [1] "double"
#If ID variable is not of "integer" type, transform it to integer
longitudinal mortalitys$id=as.integer(longitudinal mortalitys$sid)
typeof(longitudinal mortalitys$id)
## [1] "integer"
#keep only observations without missing data and only variables that will be
used to fit the model for the time-dependent covariate
Longi <- na.omit(longitudinal_mortalitys[, c("female", "ili",</pre>
"cvd_his", "time_years2", "ckd_risk_num","id", "bmi_bas", "b_age10")])
typeof(Longi$id)
## [1] "integer"
## joint model for ordinal risk catefory of CKD and CVD mortality process ##
library(INLA)
library(INLAjoint)
#setting up multistate outcomes in INLA for each transition
t1=inla.surv(time=transition1$Tstop, event=transition1$status)
t2=inla.surv(time=transition2$Tstop, event=transition2$status)
t3=inla.surv(time=transition3$Tstop, truncation = transition3$Tstart, event =
transition3$status)
```

To fit the backward continuation ratio logistic regression model, we have to transform the data into the format explained at *Bender R, Benner A. Calculating ordinal regression models in SAS and S-plus. Biometrical Journal; 2000, 6:677-699.* 

The JMbayes2 package in R contains the function cr\_setup, which transforms the data into the right format to fit the backward continuation ratio logistic regression model. More information on how to use this function can be found at

https://rdrr.io/github/drizopoulos/JMbayes2/man/cr\_setup.html

```
library(JMbayes2)
cr_vals <- cr_setup(Longi$ckd_risk_num, "backward")</pre>
cr_data <- Longi[cr_vals$subs, ]</pre>
cr data$y new <- cr vals$y</pre>
cr data$cohort <- cr vals$cohort</pre>
#create dummy variables for each category to fit model
cr_data$cat2=ifelse(cr_data$cohort=="y<=2", 1, 0)</pre>
cr_data$cat3=ifelse(cr_data$cohort=="y<=3", 1, 0)</pre>
cr data$cat4=ifelse(cr data$cohort=="all", 1,0)
cr_data$treatment=ifelse(cr_data$ili=="1", 1, 0)
##### fitting joint model
mjoint2=joint(formSurv = list(t1~ili+female+b age10+bmi bas+cvd his,
                         t2~ili+female+b age10+bmi bas+cvd his,
                         t3~ili+female+b_age10+bmi_bas+cvd_his),
            formLong = list(y new ~ -1+cat2+cat3+cat4+treatment+female+b ag
e10+bmi bas+time years2+
                           treatment*time_years2+(1+time_years2|id)),
            basRisk = c("rw2", "rw2", "rw2"),
            dataSurv = list(transition1, transition2, transition3),
            dataLong = cr_data, id="id", timeVar = "time_years2", corLong =
FALSE,
            family=c("binomial"),
            assoc=list(c("CV", "CV", "CV")),
            control=list(verbose=TRUE, strategy="adaptive", int.strategy="eb
", priorFixed=list(mean=0, prec=0.16,
mean.intercept=0, prec.intercept=0.16),
                       priorAssoc=list(mean=0, prec=0.16) ))
```

```
##### exploring results of joint model
summary(mjoint2, hazr=TRUE)
## Longitudinal outcome (binomial)
                                          sd 0.025quant 0.5quant 0.975quant
                                mean
                              -8.5386 0.4626 -9.4453 -8.5386
## cat2 L1
                                                                     -7.6318
## cat3 L1
                            -11.5942 0.4655 -12.5065 -11.5942
                                                                    -10.6819
## cat4 L1
                            -13.9468 0.4700 -14.8680 -13.9468
                                                                    -13.0256
                             -0.2606 0.0901
                                               -0.4372 -0.2606
## treatment L1
                                                                    -0.0840
## female L1
                             -0.3061 0.0827
                                               -0.4682 -0.3061
                                                                    -0.1440
## b_age10_L1
                             0.6932 0.0582
                                               0.5791 0.6932
                                                                      0.8073
                             0.0671 0.0068
                                                 0.0538 0.0671
## bmi bas L1
                                                                      0.0804
## time_years2_L1
                             0.2061 0.0091
                                                 0.1883 0.2061
                                                                      0.2239
                                                -0.0359 -0.0106
## treatment:time_years2_L1 -0.0106 0.0129
                                                                      0.0146
## Random effects variance-covariance (L1)
##
                                           sd 0.025quant 0.5quant 0.975quant
                                  mean
                                5.7331 0.3567
                                                           5.6888
## Intercept L1
                                                  5.1606
                                                                       6.5459
## time_years2_L1
                                0.0528 0.0099
                                                  0.0380
                                                           0.0512
                                                                       0.0768
                                                 -0.0602 -0.0023
## Intercept L1:time years2 L1 0.0053 0.0446
                                                                       0.1147
##
## Survival outcome (S1)
                             exp(mean)
                                          sd 0.025quant 0.5quant 0.975quant
## Baseline risk (variance)_S1
                               0.0260 0.0138
                                                0.0122
                                                         0.0218
                                                                   0.0642
## Baseline risk (mean)_S1
                               0.0047 0.0022
                                                0.0017
                                                         0.0042
                                                                   0.0103
## ili1 S1
                               0.9548 0.0708
                                                0.8230
                                                         0.9520
                                                                   1.1013
## female S1
                               0.6070 0.0471
                                                0.5196
                                                         0.6051
                                                                   0.7048
                               1.3307 0.0750
## b_age10_S1
                                                1.1892
                                                         1.3284
                                                                   1.4839
## bmi bas S1
                               0.9945 0.0066
                                                0.9816
                                                         0.9945
                                                                   1.0076
## cvd_his_S1
                               3.6282 0.2939
                                                3.0843
                                                         3.6159
                                                                   4.2390
##
## Survival outcome (S2)
                                          sd 0.025quant 0.5quant 0.975quant
                             exp(mean)
## Baseline risk (variance) S2
                               0.0148 0.0033
                                                0.0091
                                                         0.0146
                                                                   0.0221
## Baseline risk (mean)_S2
                               0.0017 0.0030
                                                0.0000
                                                         0.0008
                                                                   0.0098
## ili1 S2
                               1.2906 0.3161
                                                0.7783
                                                         1.2529
                                                                   2.0166
## female S2
                               0.5848 0.1508
                                                0.3429
                                                         0.5659
                                                                   0.9337
## b_age10_S2
                               1.3036 0.2162
                                                0.9295
                                                         1.2857
                                                                   1.7782
## bmi_bas_S2
                               0.9874 0.0205
                                                0.9478
                                                         0.9872
                                                                   1.0282
## cvd_his_S2
                               3.6449 0.9616
                                                2.1106
                                                         3.5221
                                                                   5.8762
##
## Survival outcome (S3)
                                          sd 0.025quant 0.5quant 0.975quant
                             exp(mean)
## Baseline risk (variance)_S3
                               0.0139 0.0029
                                                0.0085
                                                         0.0139
                                                                   0.0199
## Baseline risk (mean)_S3
                               0.0585 0.1571
                                               -0.0002
                                                         0.0131
                                                                   0.4228
## ili1 S3
                               0.5532 0.2057
                                                0.2537
                                                         0.5177
                                                                   1.0560
## female S3
                                                0.0782
                               0.2422 0.1293
                                                         0.2128
                                                                   0.5779
## b_age10_S3
                               1.3434 0.2993
                                                0.8493
                                                         1.3107
                                                                   2.0225
                                                0.8910
## bmi_bas_S3
                               0.9495 0.0304
                                                         0.9489
                                                                   1.0106
## cvd his S3
                               2.4837 0.9202
                                                1.1424
                                                         2.3256
                                                                   4.7318
##
```

```
## Association longitudinal - survival
##
             mean
                   sd 0.025quant 0.5quant 0.975quant
## CV_L1_S1 0.0993 0.0264 0.0494 0.0986
                                                0.1530
## CV_L1_S2 0.3621 0.1070
                           0.1796
                                     0.3519
                                                0.5950
## CV_L1_S3 0.4813 0.0839
                           0.3253 0.4778
                                                0.6545
## log marginal-likelihood (integration)
                                          log marginal-likelihood (Gaussian)
##
                              -273779.0
                                                                  -273770.4
##
## Deviance Information Criterion: -483386.2
## Widely applicable Bayesian information criterion: -504411.2
## Computation time: 2235.16 seconds
```

To estimate time-dependent association of logit for probability of being in a higher risk category relative to lower risk categories of CKD progression with transition 1, transition 2, and transition 3, exponentiate mean of CV\_L1\_S1, CV\_L1\_S2, and CV\_L1\_S3, respectively.