MultiFEBE

Tutorial 6: static analysis of a floating pile with boundary elements and finite elements

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1 Problem description

In this sixth tutorial, the horizontal pressure distribution along different floating piles due to a static load is obtained using the BEM-FEM coupling. The results can be directly compared against the literature [1], which serves as a validation case for this coupled model.

A floating pile is a foundation with a slender cylindrical shape which is buried into the soil. The structure is mainly one-dimensional, thus it is modelled as a finite element region consisting on beam finite elements. The soil is a half-space (unbounded domain) and it is modelled as a boundary element region. For this boundary element region, the half-space Green's function (Mindlin solution) is used, so no discretization is needed for the free-surface. The soil-pile interaction is introduced by including in the boundary element region a body line load whose discretization must be conforming to the beam finite elements. Figure 1 shows the devised mesh for the problem.

2 Pre-processing

Pre-processing in MultiFEBE consists of defining the geometry and mesh of the problem. There are three ways to do such definition: directly from the input file (mode = 0), from another file in the native format (mode = 1) or from another file in the Gmsh MSH file format version 2.2 (mode = 2). However, it is preferable to use a *.msh file for relatively large geometries, therefore, this is the syntax explained in the following subsections.

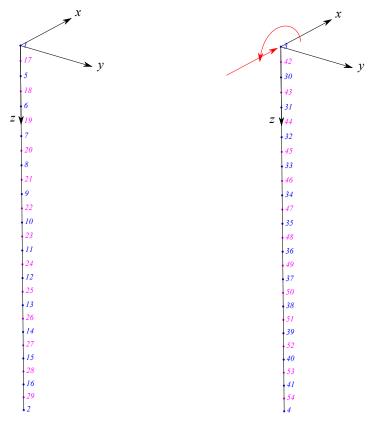
2.1 Mesh generation with Gmsh

Gmsh [2, 3] is a finite element mesh generator with its own language. The software allows to create the geometry in a "bottom-up" manner, going from the most basic elements (points) to the highest order elements (volumes) or in a "Constructive Solid Geometry" manner (boolean operations) or with a combination of methodologies. Gmsh also allows to define the so-called "physical groups" which are unmodifiable entities that gather elementary entities as sole entities, where every entity must have a unique tag. On the other hand, the file containing all this geometric definition is the file *.geo whereas the mesh definition is in the file *.msh.

2.1.1 File *.geo

The Gmsh language allows to define parameters to use later in the script and comments as every other programming language.

In this example two parameters are defined: the pile length (Lpile) and the mesh element size (ms_pile). Every point in the geometry can be specified by its coordinates (x y z) and the mesh element size to use there with the function "Point". Every straight line of the model is created with the function "Line" and its initial and final points. Then, with the function "Physical Line" every



Body line load elements

Beam finite elements

Figure 1: Mesh for the floating pile example. Boundary element mesh consists only on body line load elements, which geometrically coincides to beam finite element mesh.

line is converted into a single entity or physical entity with its own name. The function "Transfinite Line" explicitly defines the location of the nodes on the line by following the expression specified and the function "Ceil" rounds up values to the nearest integer. Furthermore, it is worth noting that "if an expression defines a new entity, it is enclosed between parentheses but if an expression refers to a previously defined entity, it is enclosed between braces." [3]

Finally, the mesh generation, the element order and the *.msh file saving can also be specified with the expressions Mesh + mesh dimension, SetOrder + element order and Save + "name.msh", respectively.

The resulting *.geo file applied to the problem is the following:

```
// Geometry & mesh parameters
Lpile = 25;
ms_pile = 2;

Point (1) = {0, 0, 0, ms_pile};
Point (2) = {0, 0, Lpile, ms_pile};
Line (1) = {1, 2};
Transfinite Line {1} = Ceil(Lpile/ms_pile + 1.);
Physical Line ("line-load") = {1};

Point (3) = {0, 0, 0, ms_pile};
Point (4) = {0, 0, Lpile, ms_pile};
Line (2) = {3, 4};
```

```
Transfinite Line {2} = Ceil(Lpile/ms_pile + 1.);
Physical Line ("pile") = {2};

// Mesh generation
Mesh 1;
SetOrder 2;
Save "mesh.msh";
```

2.1.2 File *.msh

The *.msh file begins with a mandatory section about information of the file (MeshFormat) and following by the other sections. Here, three sections are used: the physical group names (PhysicalName), the nodes (Nodes) and the elements (Elements).

In the section "PhysicalName", all the physical entities of the model are defined. The first line indicates the number of physical entities. Then, one line per physical entity indicating the physical dimension, the tag and the name.

In the section "Nodes", all the nodes of the model are defined. The first line indicates the number of nodes. Then, one line per node indicating the node identifier and its coordinates (x y z).

In the section "Elements", all the elements of the model are defined. The first line indicates the number of elements. Then, one line per element indicating:

- Element identifier.
- Type of element.
- Number of auxiliary tags.
- List of tags, where the two first auxiliary tag are mandatory, and corresponds to the identifier of the physical entity to which the element belongs and the second one is the identifier of the elementary model entity to which the element belongs. The rest of the tags are optional.
- A list of identifiers corresponding to the nodes of the element.

For example, in this case, an element with the identifiers 1 8 2 1 1 1 5 7 corresponds to:

- 1: element 1.
- 8: type 8 (3-node second order line).
- 2: it has 2 auxiliary tags.
- 1: it belongs to the physical entity 1.
- 1: it belongs to the line 1.
- 1, 5, 7: it connects the nodes 1, 5 and 7.

Finally, the *.msh file can be obtain in $File \to Export$. The resultant *.msh file applied to the problem is the following:

```
$MeshFormat
2.2 0 8
$EndMeshFormat

$PhysicalNames
2
1 1 "line-load"
1 2 "pile"
$EndPhysicalNames
```

\$Nodes

54

- 1 0 0 0
- 2 0 0 25
- 3 0 0 0
- 4 0 0 25
- 5 0 0 1.923076923069284
- 6 0 0 3.846153846138358
- 7 0 0 5.769230769205297
- 8 0 0 7.692307692272241
- 9 0 0 9.615384615345244
- 10 0 0 11.53846153841902
- 11 0 0 13.4615384614928
- 12 0 0 15.38461538456658
- 13 0 0 17.30769230765023
- 14 0 0 19.23076923073767
- 15 0 0 21.15384615382511
- 16 0 0 23.07692307691256
- 17 0 0 0.9615384615346747
- 18 0 0 2.884615384604353
- 19 0 0 4.807692307671953
- 20 0 0 6.730769230738639
- 21 0 0 8.653846153808447
- 22 0 0 10.57692307688226
- 22 0 0 10.07032307000220
- 23 0 0 12.499999999539 24 0 0 14.42307692302983
- 25 0 0 16.34615384610878
- 26 0 0 18.26923076919312
- 20 0 0 10.20323070313312
- 27 0 0 20.19230769228153 28 0 0 22.11538461536667
- 29 0 0 24.03846153845748
- 30 0 0 1.923076923069284
- 31 0 0 3.846153846138358
- 31 0 0 3.040133040130330
- 32 0 0 5.769230769205297
- 33 0 0 7.692307692272241 34 0 0 9.615384615345244
- 35 0 0 11.53846153841902
- 36 0 0 13.4615384614928
- 37 0 0 15.38461538456658
- 38 0 0 17.30769230765023
- 39 0 0 19.23076923073767
- 40 0 0 21.15384615382511
- 41 0 0 23.07692307691256
- 42 0 0 0.9615384615346747
- 43 0 0 2.884615384604353
- 44 0 0 4.807692307671953
- 45 0 0 6.730769230738639
- 46 0 0 8.653846153808447
- 47 0 0 10.57692307688226
- 48 0 0 12.499999999539
- 49 0 0 14.42307692302983 50 0 0 16.34615384610878
- 51 0 0 18.26923076919312

```
52 0 0 20.19230769228153
53 0 0 22.11538461536667
54 0 0 24.03846153845748
$EndNodes
$Elements
26
1 8 2 1 1 1 5 17
2 8 2 1 1 5 6 18
3 8 2 1 1 6 7 19
4 8 2 1 1 7 8 20
5 8 2 1 1 8 9 21
6 8 2 1 1 9 10 22
7 8 2 1 1 10 11 23
8 8 2 1 1 11 12 24
9 8 2 1 1 12 13 25
10 8 2 1 1 13 14 26
11 8 2 1 1 14 15 27
12 8 2 1 1 15 16 28
13 8 2 1 1 16 2 29
14 8 2 2 2 3 30 42
15 8 2 2 2 30 31 43
16 8 2 2 2 31 32 44
17 8 2 2 2 32 33 45
18 8 2 2 2 33 34 46
19 8 2 2 2 34 35 47
20 8 2 2 2 35 36 48
21 8 2 2 2 36 37 49
22 8 2 2 2 37 38 50
23 8 2 2 2 38 39 51
24 8 2 2 2 39 40 52
25 8 2 2 2 40 41 53
26 8 2 2 2 41 4 54
$EndElements
```

2.2 Input data file

Solving in MultiFEBE consists of running the software by specifying several options in the following sections¹: [problem], [settings], [materials], [regions], [conditions over nodes], etc.

The first part to configurate is the problem definition in the section [problem]. This example is a 3D static mechanical problem.

```
[problem]
n = 3D
type = mechanics
analysis = static
```

In the section [export], several export settings are defined. In this example, the nodal solutions and the **element** solutions will be exported by writing the option T with the corresponding expression, *export_nso* and *export_tot*, respectively.

```
[export]
export_nso = T
export_tot = T
```

¹See reference manual.

Next step is to configurate the mesh. In this case, a mesh from *Gmsh* will be used so that it is necessary to write the option number 2 and the document name obtained from it in the section [settings]. However, if the mesh were going to be read from the input file, it would require to write the sections [nodes], [elements] and [parts] instead.

```
[settings]
mesh_file_mode = 2 "mesh.msh"
```

As the problem has two materials, the section [materials] will need three lines: a first line for the number of materials in the model and a line per material with their properties such as tag, type, E and ν .

```
[materials]
2
1 elastic_solid E 200.d6 nu 0.49d0
2 elastic_solid E 182.4214d9 nu 0.3d0
```

In the section [be body loads], all body loads in BE regions are defined. The format consists of a first line with the number of BE body loads to be defined, next as many lines as BE body loads. Each line contains first the BE body load identifier and last the mesh part which contains the elements associated with it.

```
[be body loads]
1
1 1
```

The section [fe subregions] indicates the number of fe subregions in the first line (1) and a line per subregions indicating the subregion identifier (1) and the part identifier (2). The last two zeros at the end are mandatory and they are going to be used in the future for additional features.

```
[fe subregions]
1
1 2 0 0
```

In the section [cross sections], it is necessary to specify the number of cross sections in the first line and a line per cross section by indicating the type of fe (strbeam_t = straight beam, Timoshenko model), number of fe subregions related to the cross section (1), fe subregion identifier (1), type of cross section (circle), radius (1.) and reference vector for the section orientation (1. 0. 0.).

```
[cross sections]
1
strbeam_t 1 1 circle 1. 1. 0. 0.
```

The format of the [regions] section consists of a first line indicating the number of regions (2). Furthermore, for each region there must be a block of data consisting of several lines.

The first region is a BE half-space, so the region identifier and the region class (discretization method) are 1 be. Then, as a half-space the following data specify:

- -3: The normal vector to the surface is in -z direction.
- 0.: Coordinate of the free surface.
- 1: Boundary condition of the free surface. Free traction in this case.

The second line indicates the number of boundaries and a list of boundaries (0), the third line defines the material (material 1) and the fourth line defines the number and a list of BE body loads (1 1).

The second region is a FE region, so the first line shows the region identifier and the region class (discretization method) (2 fe). Then, the second line indicates the number of subregions (1) and its identifier (1) and the third line the material (material 2).

```
[regions]
2

1 be half-space -3 0. 1
0
material 1
1 1
2 fe
1 1
material 2
```

In the section [conditions over nodes] all boundary conditions over nodes will be specified. As a 3D model, there are 6 lines for every boundary condition. Every line has two digits, where the first one indicates the type of condition (0 for displacement and 1 for force) and the second one the value. In case of displacement, firstly the displacements u_x, u_y, u_z are configured and then the rotations $\theta_x, \theta_y, \theta_z$. In case of force, firstly the forces F_x, F_y, F_z and then the moments M_x, M_y, M_z .

The whole data file applied to the problem is the following:

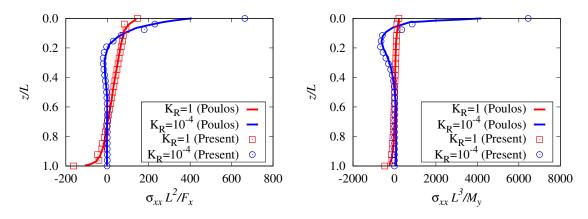
```
[problem]
n = 3D
type = mechanics
analysis = static
[export]
export_nso = T
export_tot = T
[settings]
mesh_file_mode = 2 "mesh.msh"
[materials]
1 elastic_solid E 200.d6 nu 0.49d0
2 elastic_solid E 182.4214d9 nu 0.3d0
[be body loads]
1 1
[fe subregions]
1 2 0 0
[cross sections]
```

3 Post-processing

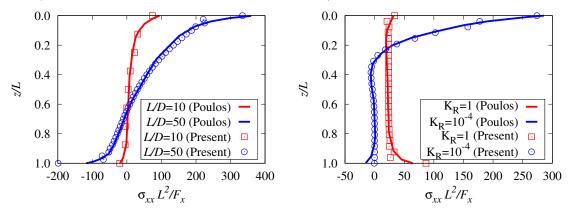
Figure 2 shows the dimensionless pressure along a floating pile for several cases. The results [1] are shown together with the obtained results from the present model. The cases differ in pile slenderness L = D (L is the pile length and D is the pile diameter), pile head constraints (free-head or fixed-head where rotation is constrained), loading type (horizontal force F_x or moment M_y), and pile flexibility factor $K_R = E_p I_p = (E_s L^4)$. It is observed a very good agreement except around the pile tip and head, where small discrepancies appear presumably due to the simplification introduced by a one-dimensional modelling of the pile-soil interaction.

References

- [1] H.G. Poulos and E.H. Davis. Elastic solutions for soil and rock mechanics. Centre for Geotechnical Research, (1991).
- [2] C. Geuzaine and J.-F. Remacle, "Gmsh: a three-dimensional finite element mesh generator with built-in pre- and post-processing facilities." *Int. J. Numer. Methods Eng.*, Volume 79, Issue 11, pages 1309–1331, (2009)
- [3] C. Geuzaine and J.-F. Remacle, "Gmsh." http://gmsh.info/



(a) Free-head and horizontal load F_x applied. Pile (b) Free-head and moment load M_y applied. Pile with L/D=25, and soil $\nu_s=0.5$.



(c) Free-head and horizontal load F_x applied. Pile (d) Fixed-head and horizontal load F_x applied. Pile flexibility $K_R=0.01$, and soil $\nu_s=0.5$. with L/D=25, and soil $\nu_s=0.5$.

Figure 2: Pressure distribution along floating piles for several cases. Reference results are taken from [1].