## EE450 Discussion #4





- Shannon's Theorem
- Modulations
- Multiplexing



## Shannon's Theorem

- $C = B \log_2(1 + SNR)$
- Theoretical Maximum Capacity that can be obtained on a line
- Sets an Upper Bound on the capacity given the conditions
  - Used for Calculating the
    - Signal to Noise Ratio Given the Bandwidth and capacity of the channel
    - Bandwidth Given the SNR and Channel Capacity
    - Capacity Given the SNR and the Bandwidth

## Problem #1

- What SNR is needed to put a T-1 carrier on a 50 khz line?
  - What do we know?
    - T-1 Capacity = 1.544 Mbps
    - Bandwidth = 50 KHz
  - Move them around and Solve:
    - $\bullet$  1,544,000 = 50,000 log 2 (1+SNR)
    - $2^30.88 1 = SNR$

# Continued

- So SNR = 1976087931
  - SNR is typically measured in DB
    - Use SNR dB =  $10 \log_{10}$  (SNR)
  - In this case
    - SNR dB =  $10 \log_{10} (1976087931)$
    - SNR aprox. 92.9 dB
  - However you must NOT plug SNR into Shannon's theorem in dB format

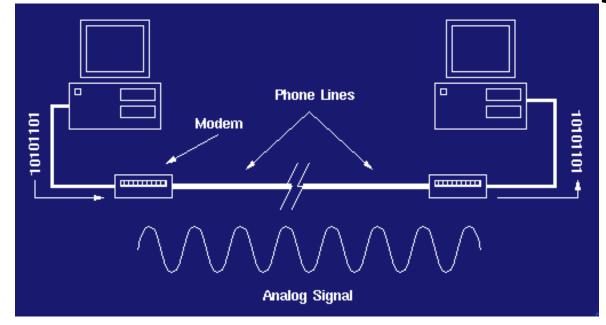
## Problem #2

- Calculate the maximum rate supported by a telephone line with BW of 4 KHz. When the signal is 10 volts, the noise is 5 milivolts.
- SNR=Signal power/Noise Power
- Power is proportional to square of the voltage
- $S/N = (10^2)/(0.005^2) = 4000000$
- B = 4000 Hz
- $C = B \log_2 (1 + S/N)$ 
  - Reminder:  $\log_2 x = \ln x / \ln 2$
- $C = 4000 \log_2 (1+4000000) = 87726 \text{ bps}$

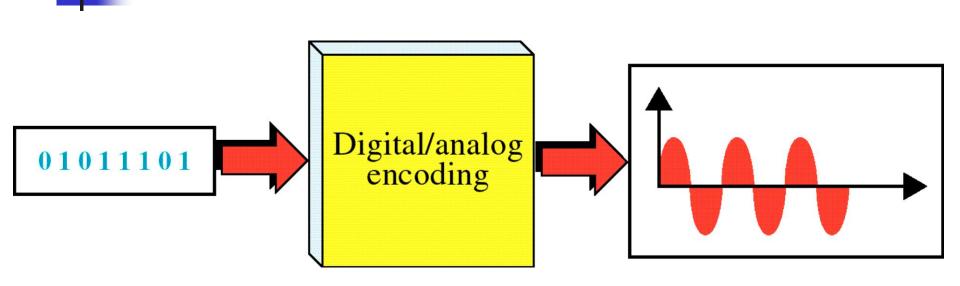


## Review on Modems

- Modem Stands for
  - MOdulator / DEModulator
- Uses Sine wave As the carrier Signal



#### **Digital to Analog Encoding**



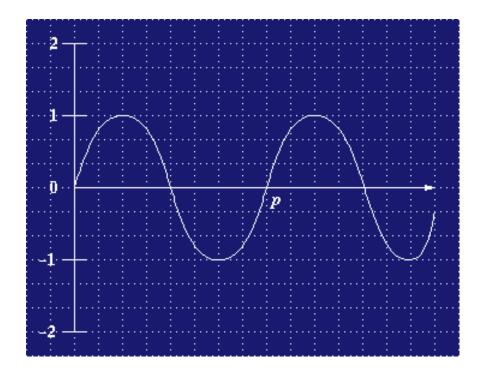


## Modulation

- Need to Encode Digital Data in an Analog Signal
- In modem transmission we use different techniques for modulation
  - Amplitude Modulation
  - Frequency Modulation
  - Phase Shift

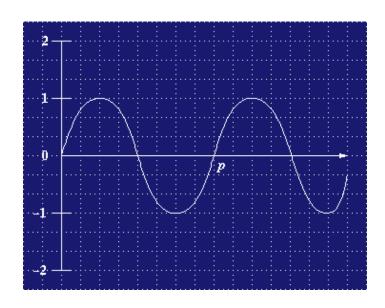
# **Amplitude Modulation**

Varies the Amplitude of the Signal

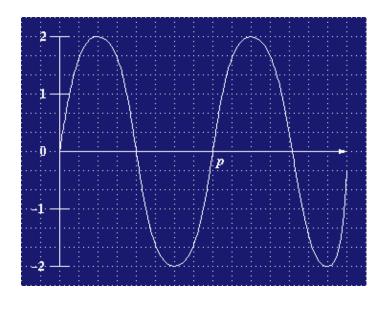


# **Amplitude Modulation**

Same Signal Greater Amplitude

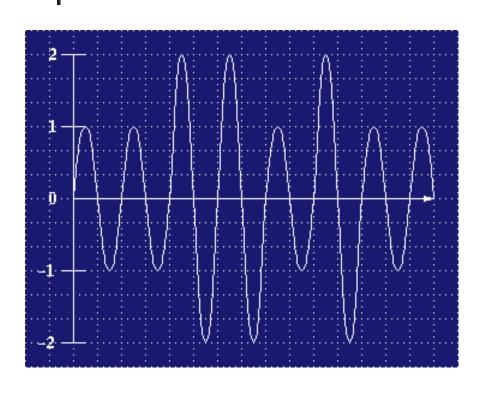


Amplitude = 1



Amplitude = 2

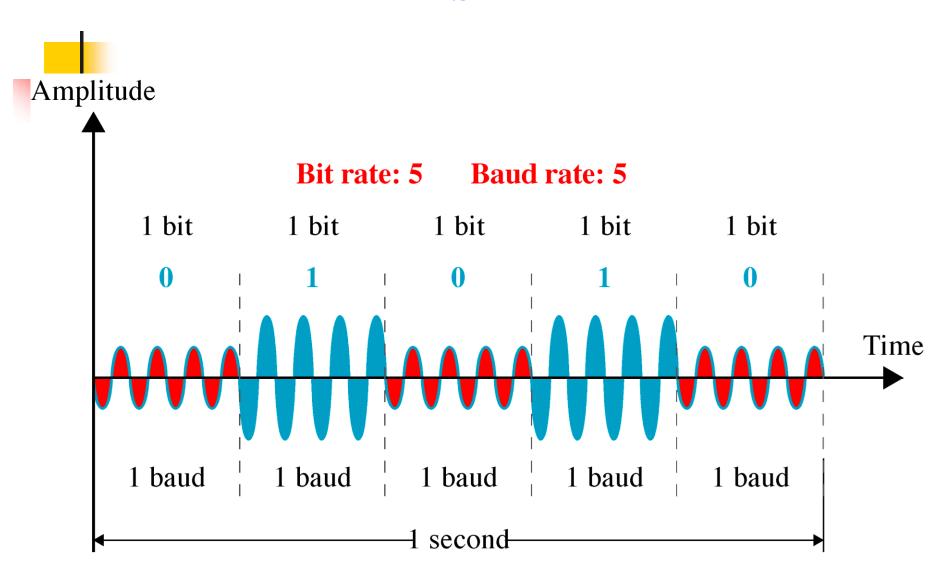
# **Amplitude Modulation**



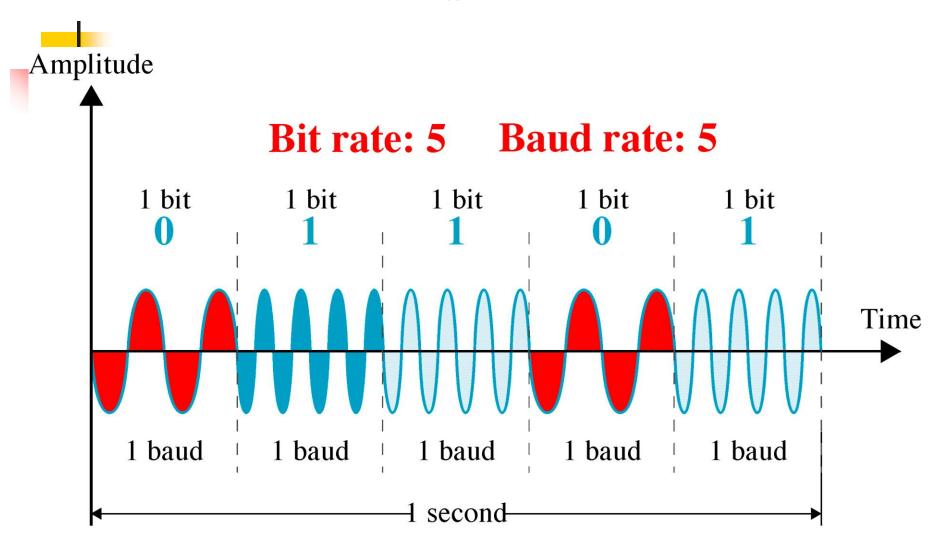
- Amplitude 2 = 1
- $\blacksquare$  Amplitude 1 = 0

- This signal Represents:
  - **0011010**

#### **ASK**

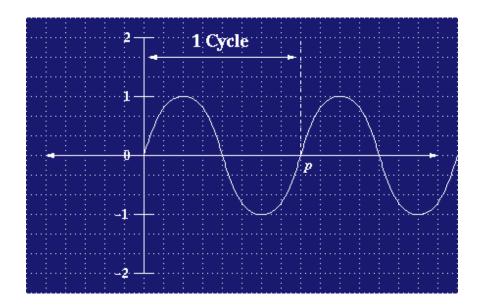


#### **FSK**



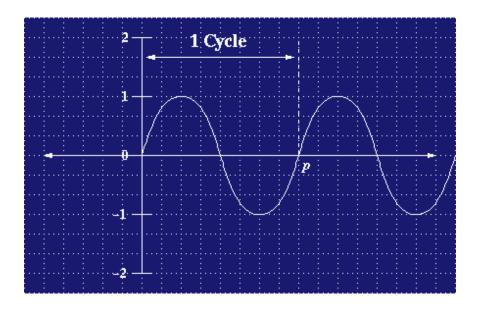
## Phase-Shift Modulation

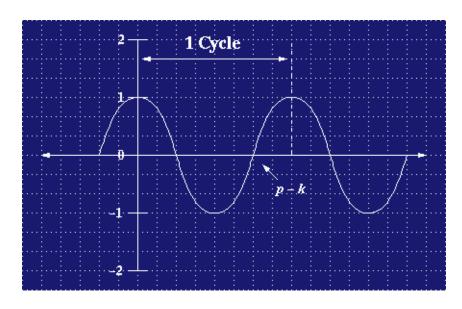
- Start with our normal sine wave
- The sine wave has a period of P
  - P may be denoted as T instead in the equations



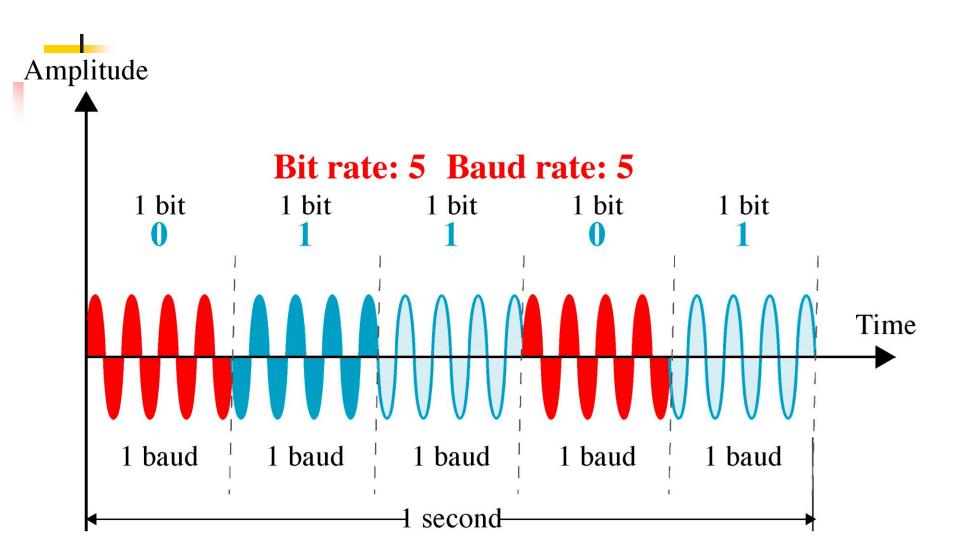


- Shift the Phase of the Sine Wave
- Shifted diagram shows that the cycle starting at 1 vs. starting at 0





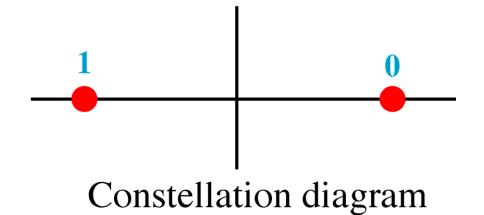
#### **PSK**



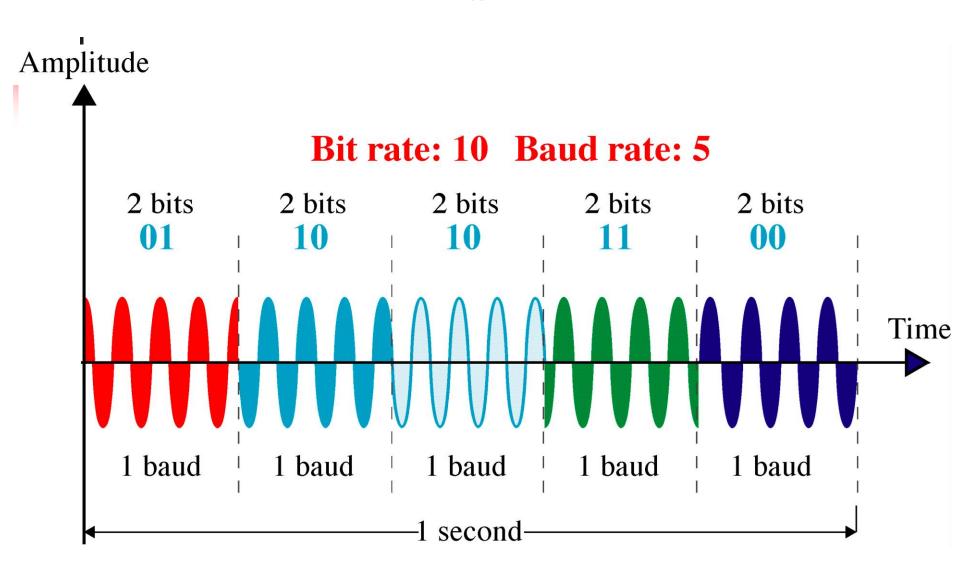


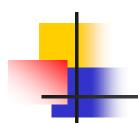


Bit	Phase
0	0
1	180
Bits	



#### 4-PSK

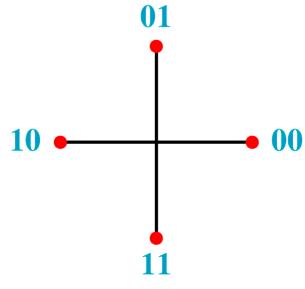




#### 4-PSK Constellation

Dibit	Phase
00	0
01	90
10	180
11	270

Dibit (2 bits)



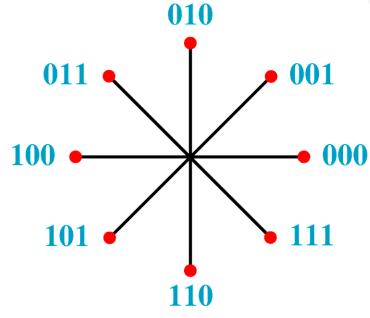
Constellation diagram

### 8-PSK Constellation



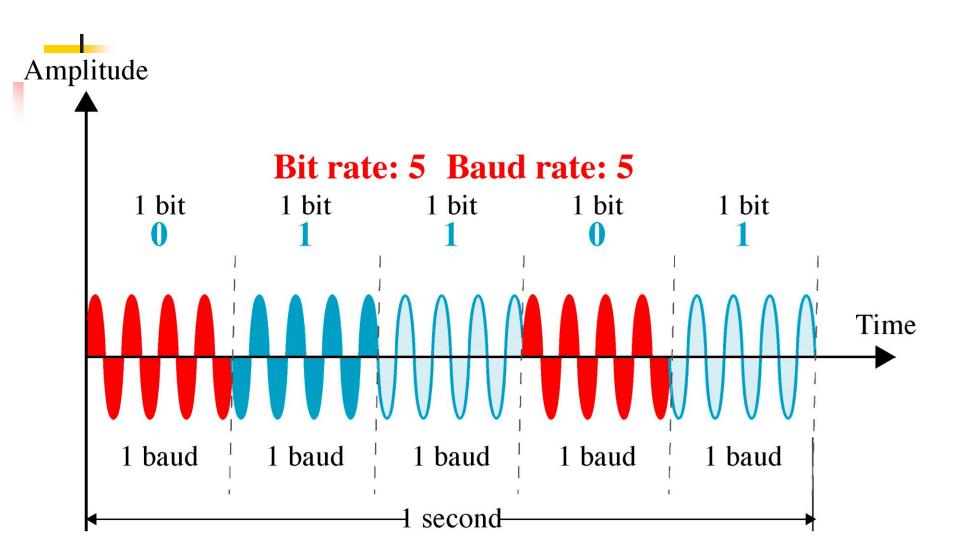
Tribit	Phase
000	0
001	45
010	90
011	135
100	180
1101	225 270
110	315
	313

Tribits (3 bits)



Constellation diagram

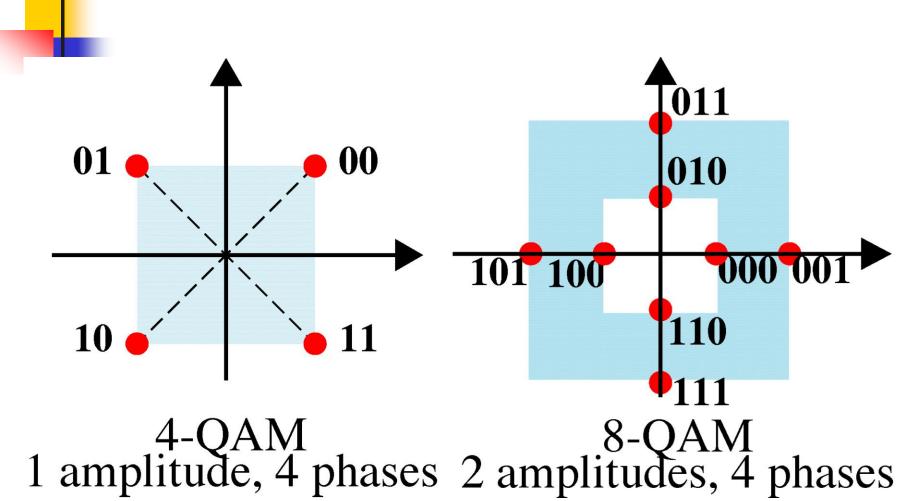
#### **PSK**



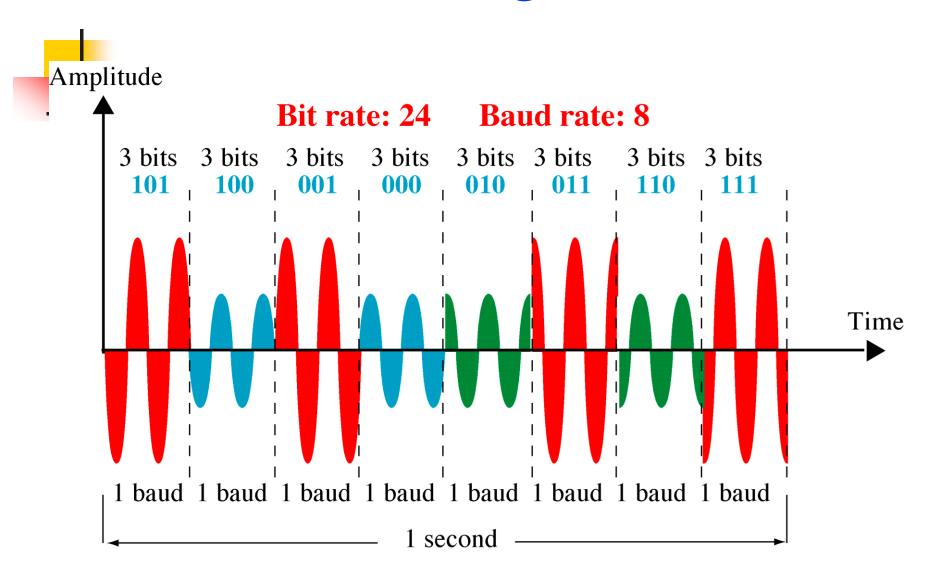
# Combining Both

- Modulation used in Modern Modems
  - Uses:
    - Amplitude Modulation
    - Phase Shift Keying
- QAM
  - Quadrature Amplitude Modulation
    - Big Name Simple Concept

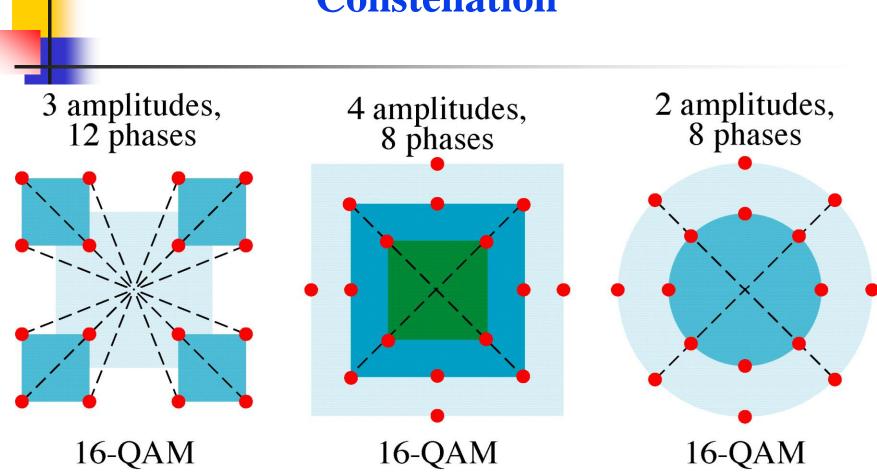
# 4-QAM and 8-QAM Constellation



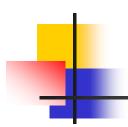
## 8-QAM Signal

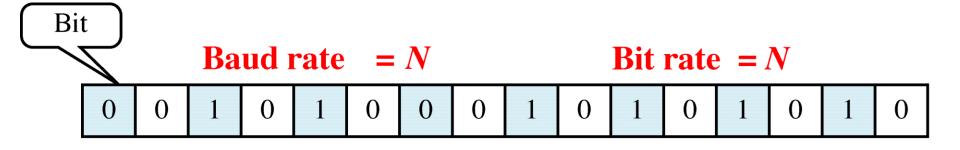


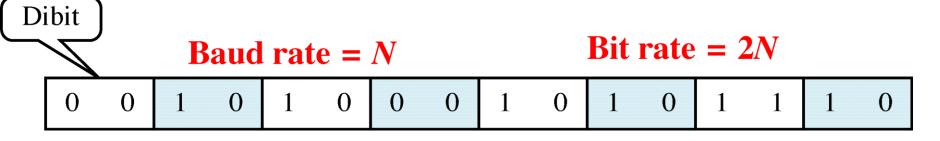
### 16-QAM Constellation









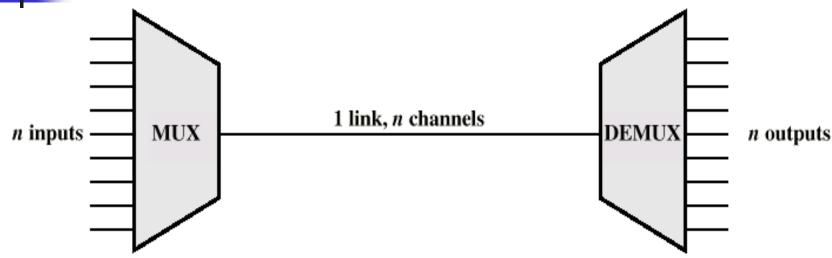


## Problem #3

- A modem uses an 8-PSK modulation scheme supporting data rate of 4800 bps. What is the signaling rate (aka baud rate)?
- 8 PSK (Phase Shift Keying)
  - 8 different encoding levels
  - Each encoding has log<sub>2</sub> 8 = 3 bits
  - 4800 / 3 = 1600 Baud Rate



## Ways of Multiplexing/Demultiplexing



- Time Division Multiplexing (TDM)
- You have n input lines coming in
- The same # of lines going out..
- Only one line interconnecting. How?



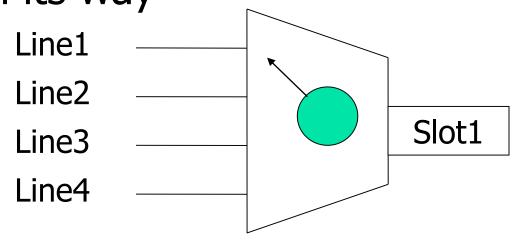
## Packing the Data In

- Multiplexing A way of aggregating data onto a single line without compromising the rate at which original data is sent.
- We are not limiting anyone's channel capacity
- We are simply sending there signal through a shared line

# Sharing – by time slots

 Sample the Line 1 – Place its value in slot 1

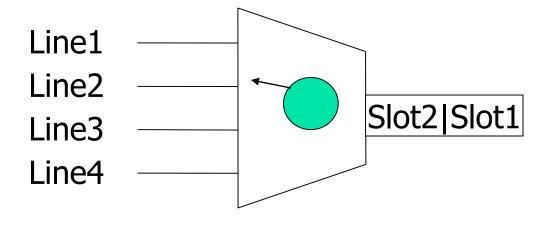
 Sampling the Line – and Send its value on its way





## More Time Slots

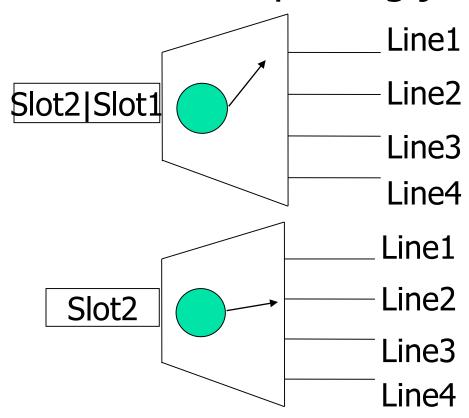
- Line 2 Places its Sample on the Line
- And it goes on...



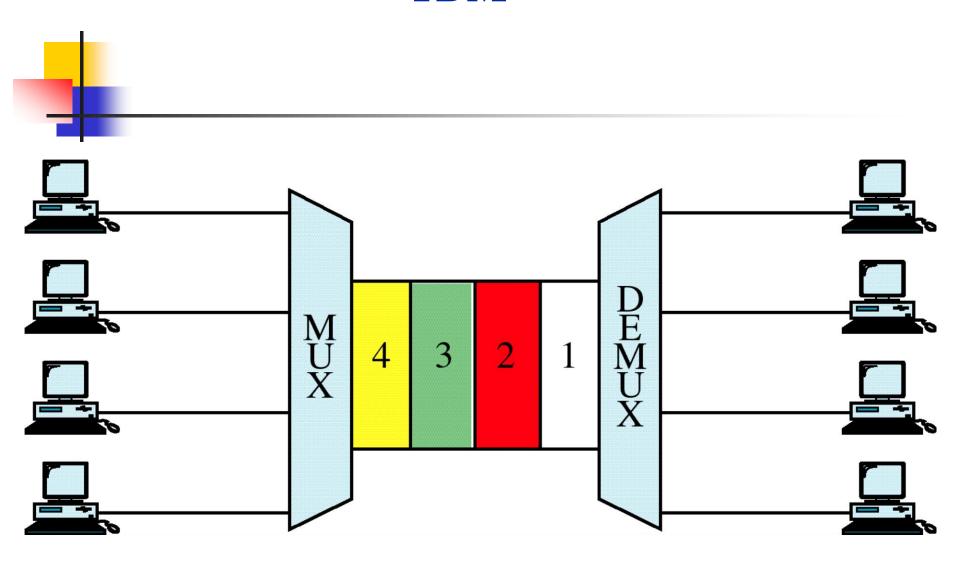


# Other Side - Demultiplexing

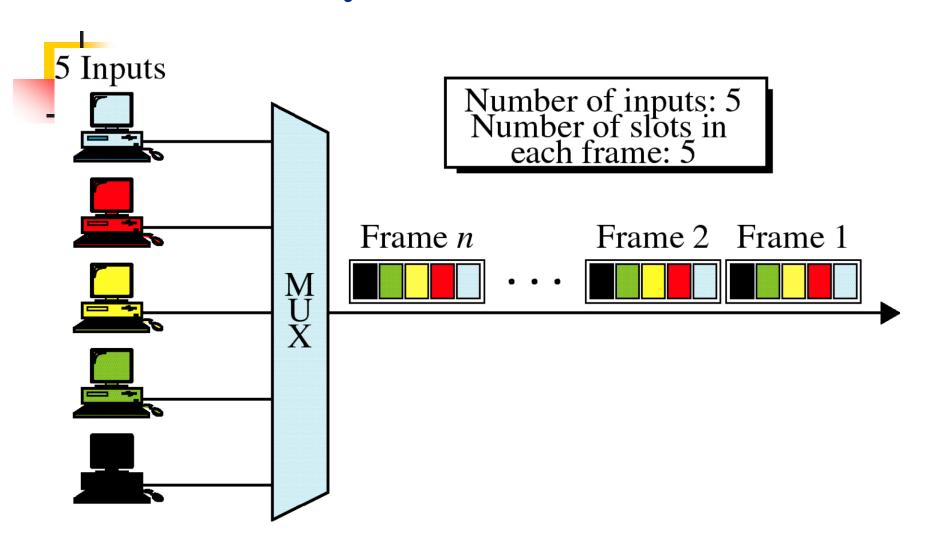
Similar to Multiplexing just the reverse



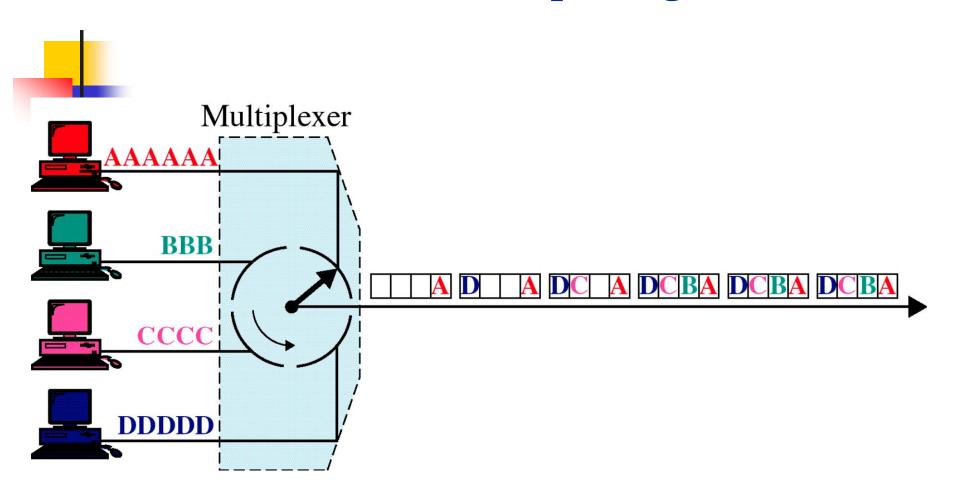
#### **TDM**



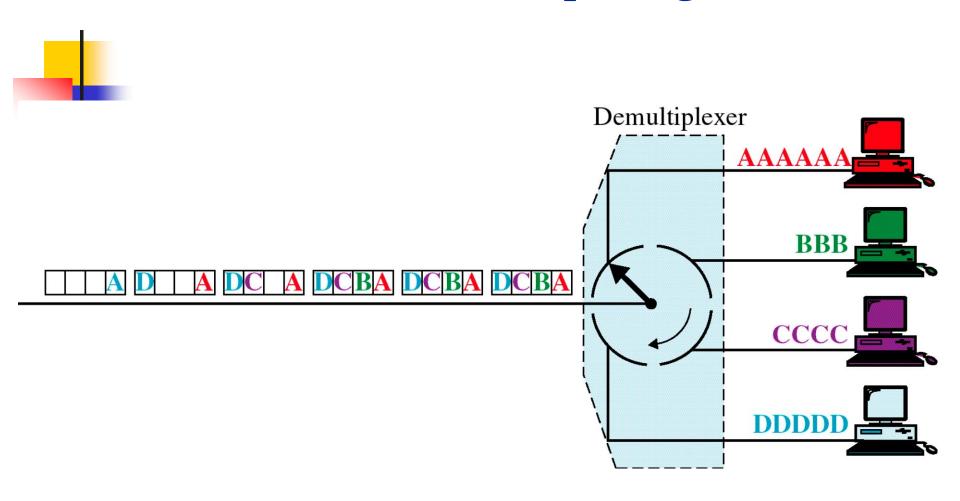
#### **Synchronous TDM**



#### TDM, Multiplexing

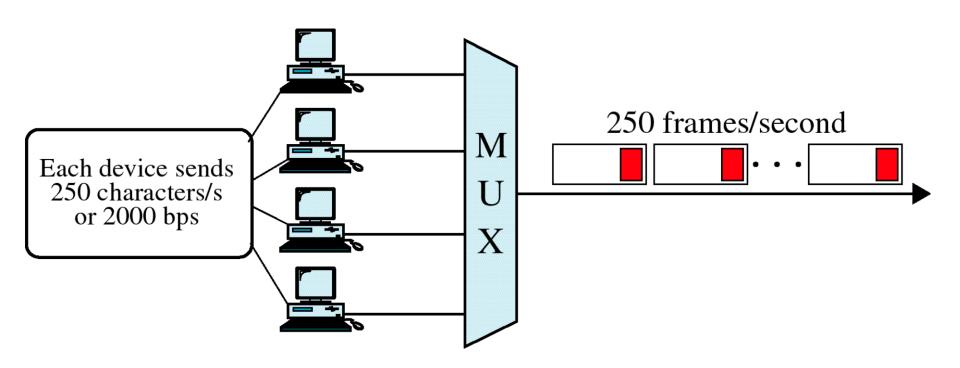


#### TDM, Demultiplexing



#### **Data Rate**

8250 bps = 250 frames/second x 33 bits/frameor  $8250 \text{ bps} = 4 \times 2000 \text{ bps} + 250 \text{ synchronization bps}$ 



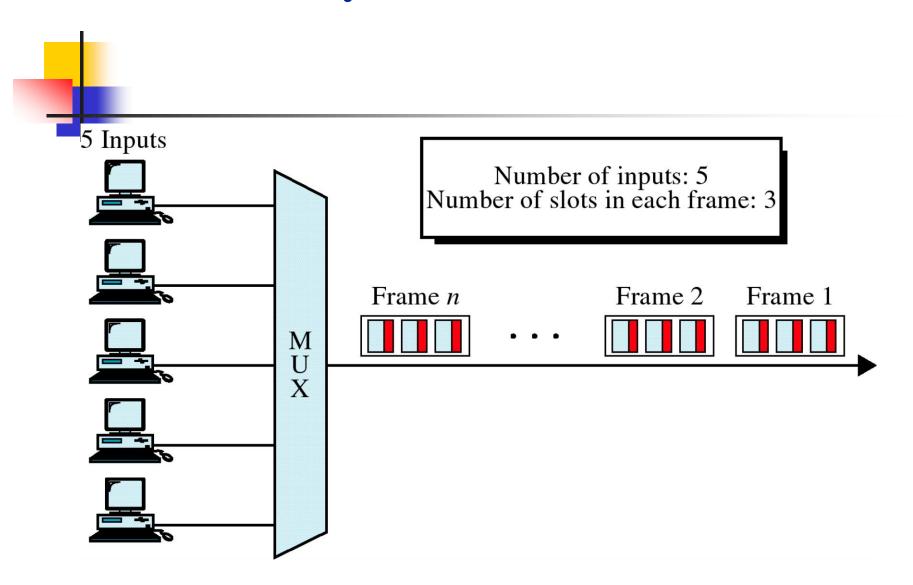
## TDM - Example

- T-1 Lines
  - Carries the equivalent of 24 voice lines
  - Each analog voice line is sampled at 8000 times a second
  - Digital Sample is thrown on the Digital Carrier Line
  - On the other side Digital samples are used to reconstruct Analog Signal.

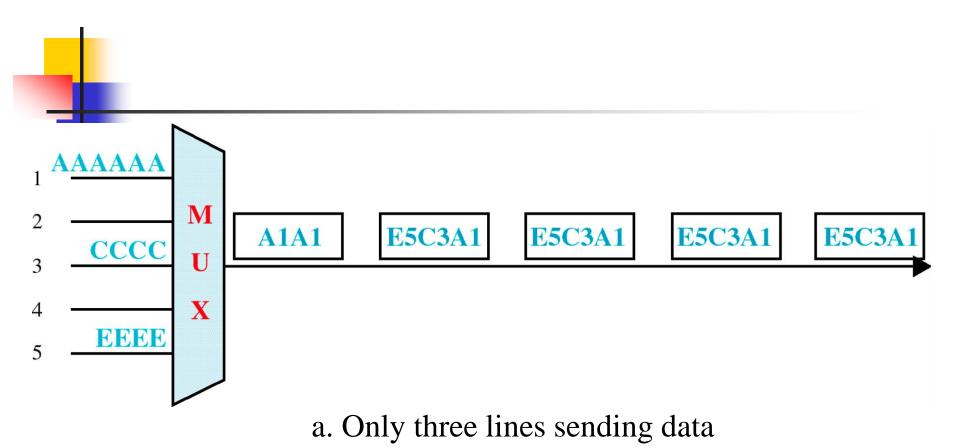
# STDM (Asynchronous TDM)

- How does it Work?
  - Checks to see if there is data to transmit on input line
    - If there is transmit data
    - If not move on to next input line

#### **Asynchronous TDM**



#### Frames and Addresses



## TDM vs. STDM

 Synchronous TDM – Gray Slots are actually carrying data

```
Slot 1 Slot 2 Slot 3 Slot 4 Slot 1 Slot 2 Slot 3
```

 Statistical TDM – Uses empty time slots but does add some overhead

```
Slot 1 Slot 2 Slot 1 Slot 2 Slot 3 Slot 1
```

# Notes on TDM

- Sampling Occurs very quickly
- Applicable to fixed number of flows

Requires Precise Timing

Resources are guaranteed

## STDM

- Statistical Time Division Multiplexing
- Similar to regular TDM but different in this:
  - Traffic is sent on demand Only if there is data on line 1, will slot 1 be occupied by line 1
  - Resources are not guaranteed
- If we are no longer guaranteed a time slot why use it?
  - We (the carrier) can take advantage of one of the input lines not being busy
- Important distinction STDM is used mainly for Digital Lines

#### TDM vs.

- Resources are guaranteed to the users
- Sampling Occurs very quickly
- Applicable to fixed number of flows
- 4. Requires Precise Timing
- Wastes valuable carrier space

#### **STDM**

- Traffic is sent on demand utilizing unused time slots so it benefits the Carrier
- Resources are not guaranteed so when time slots are busy the users suffer
- In real life there is some overhead
- 4. Speedup isn't as obvious

#### Statistical TDM Parameters

- I = Number of Input Sources
- R = Data rate of each source (bps)
- a (Alpha) = mean fraction of time each source is transmitting
- M = Effective capacity of multiplexed line
- K = M / (I x R) = Ratio of multiplexed line capacity to total input rate
- $\lambda$  (lambda) =  $\alpha \times I \times R$  = Average Arrival rate
- $T_s = 1 / M = Service time in seconds$

#### ρ: Line Utilization

- ρ = Fraction of total link capacity being used
- Many different forms to express line utilization
  - $\rho = \lambda T_s$
  - $\rho = (a \times I \times R) / M$
  - $\rho = a / K$
  - $\rho = \lambda / M$

- Ten 9600 bps lines are multiplexed using TDM. Ignoring overhead bits what is the total capacity required for Synchronous TDM?
  - Simple: 10 X 9600 = 96 kbps (96,000)

- Ten 9600 bps lines are multiplexed using TDM. Assuming that we limit line utilization to 0.8 and each line is busy 50 % of the time. What is the capacity required for <u>Statistical</u> TDM?
  - What do we know?
    - Line utilization  $\rho = .8$
    - Fraction of time transmitting a = .5
    - R Data Rate of each input source = 9600 bps
    - I number of Input Sources = 10

## Continued

- The Equation:
- $\rho = a \times I \times R \times /M$ 
  - Where M is the capacity of the multiplexed line
- Rearrange for M
  - $M = a \times I \times R / \rho$
- Plug in the given parameters
  - $M = 0.5 \times 10 \times 9600 / 0.8$
  - M = 60 kbps

- Calculate the capacity of a Multiplexed carrier?
  - 24 voice channels multiplexed
  - 8000 samples per second
    - Each frame lasts  $1/8000 = 125 \mu \text{ sec}$
  - Uses 8 bit encoding per sample
  - Capacity
    - 24 X 8000 samples/second X 8 bits/sample
    - 1,536,000 bits/second
  - T-1 Adds an extra bit per frame (for synchronization) which makes it 1.544 Mbps

- What is the percent overhead on a T-1 Carrier?
  - T-1 Carrier bandwidth of 1.544 Mbps
    - Every 192 bits one more bit is added for framing.
  - What is the overhead?



#### Continued



- Overhead in a T-1 Line
  - Every frame consists of 193 bits
  - 24 X 8 = 192 bits
  - 193-192 = 1 overhead bit
  - **1/193 = .5%**