

# Hierarchical Compositionality in Recurrent Neural Networks

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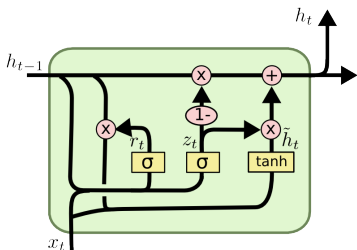
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# Recurrent Neural Networks

How can hierarchical compositionality be processed incrementally, in linear time, by a recurrent artificial neural network?

# Recurrent Neural Networks

How can hierarchical compositionality be processed incrementally, in linear time, by a recurrent artificial neural network?



$$z_t = \sigma(W_z \cdot [h_{t-1}, x_t])$$

$$r_t = \sigma(W_r \cdot [h_{t-1}, x_t])$$

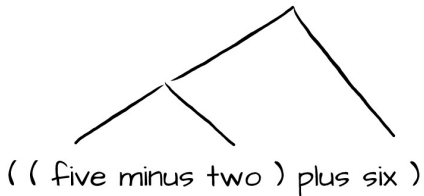
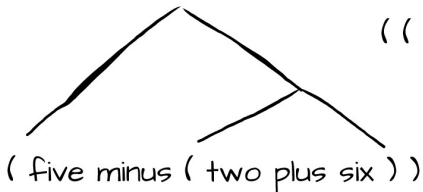
$$\tilde{h}_t = \tanh(W \cdot [r_t * h_{t-1}, x_t])$$

$$h_t = (1 - z_t) * h_{t-1} + z_t * \tilde{h}_t$$

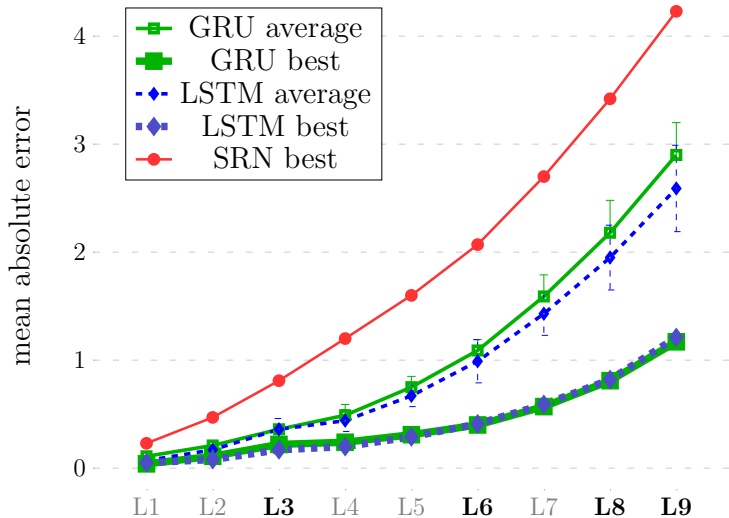
# Arithmetic Language

Name	#digits	Example
L1	1	minus three
L2	2	( five plus seven )
L3	3	( three - ( one + minus two ) )
...		
L5R	5	( ( ( ( nine + six ) + seven ) + five ) - seven )
L5L	5	( eight + ( six - ( two - ( ten + nine ) ) ) )

## Arithmetic Language



## Results



## Symbolic solutions

( five minus ( two plus six ) )

## Symbolic solutions

recursively

( five minus ( two plus six ) )



## Symbolic solutions

recursively

5

( five minus ( two plus six ) )

## Symbolic solutions

recursively      5      <sup>-</sup>  
5

( five minus ( two plus six ) )

## Symbolic solutions

recursively



5 - 5 - 5

( five minus ( two plus six ) )

## Symbolic solutions

recursively

5   -   5   2

5, -

( five minus ( two plus six ) )

## Symbolic solutions

recursively

$$5 - (5 - (2 + 2))$$

( five minus ( two plus six ) )

## Symbolic solutions

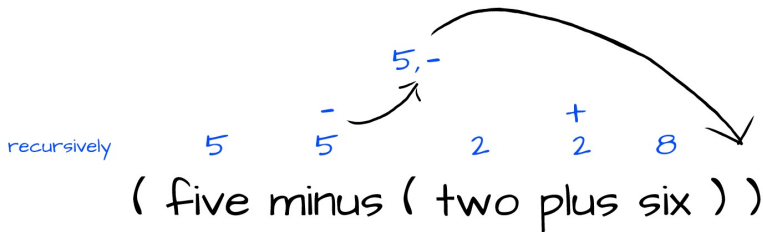
recursively

$$5 \quad - \quad 5 \quad 2 \quad + \quad 2 \quad 8$$

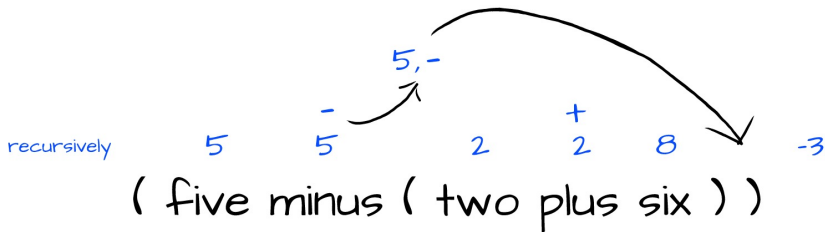
5, -

( five minus ( two plus six ) )

## Symbolic solutions

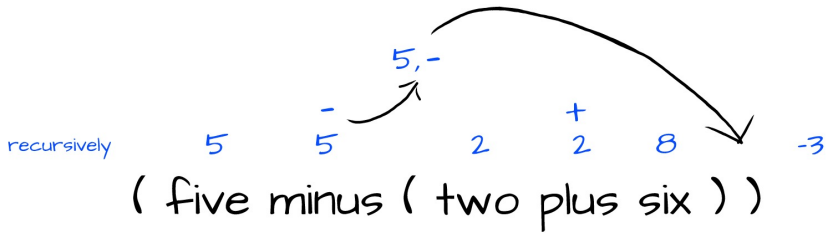


## Symbolic solutions



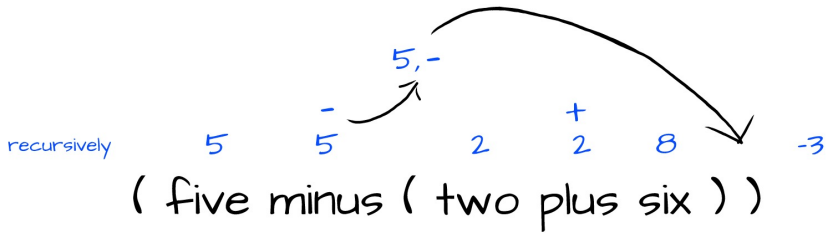


## Symbolic solutions



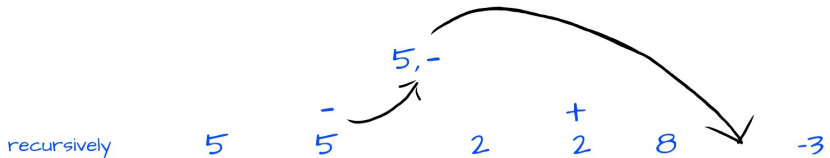
cummulatively

## Symbolic solutions



cummulatively   5

## Symbolic solutions

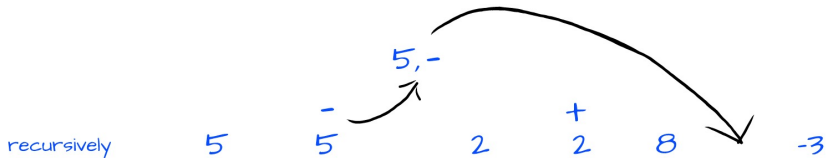


( five minus ( two plus six ) )

cummulatively

5   5  
-

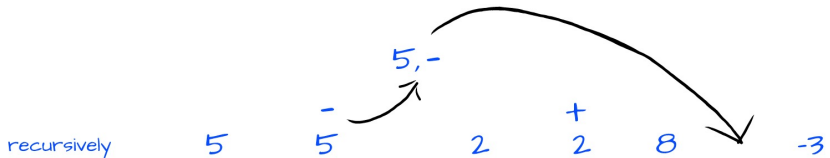
## Symbolic solutions



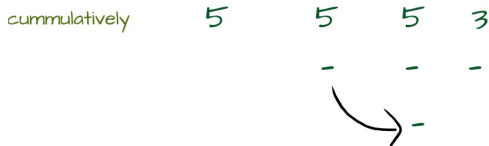
( five minus ( two plus six ) )



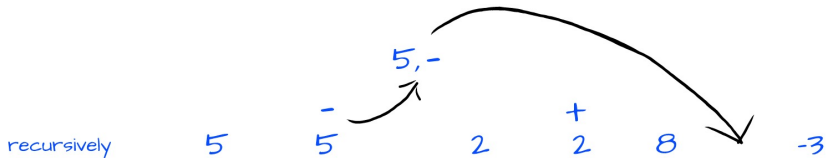
## Symbolic solutions



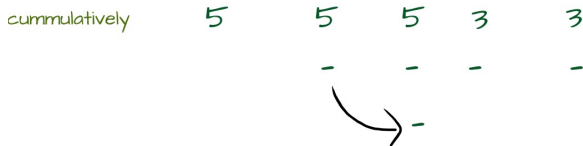
( five minus ( two plus six ) )



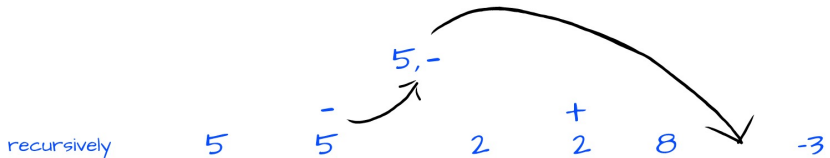
## Symbolic solutions



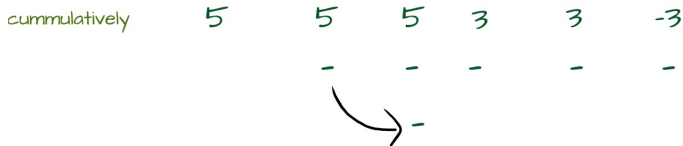
( five minus ( two plus six ) )



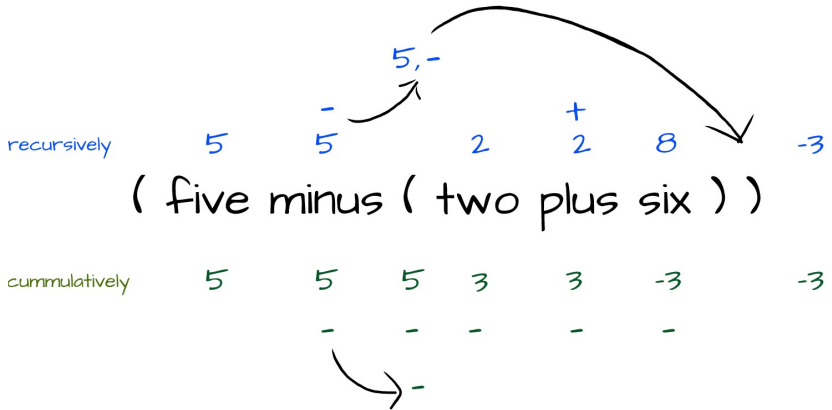
## Symbolic solutions



( five minus ( two plus six ) )



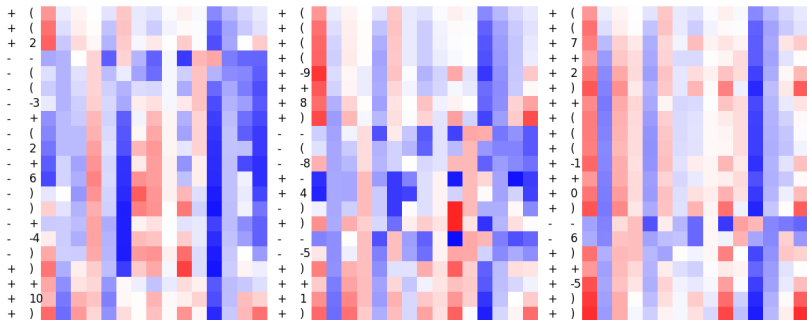
## Symbolic solutions





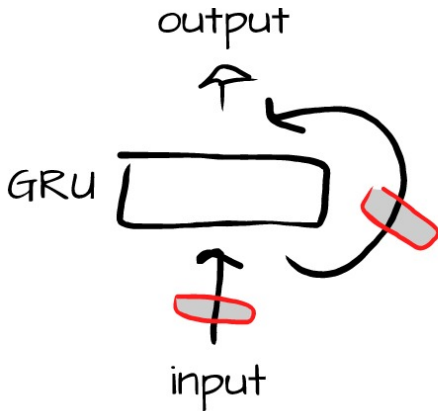
# How do we study the network?

Plotting activation values



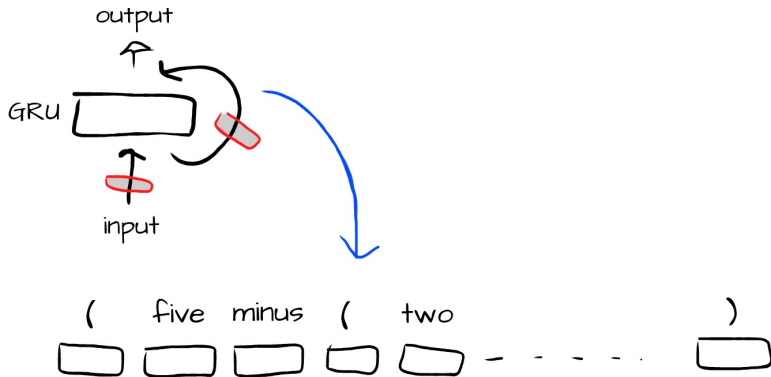
# How do we study the network?

Diagnostic Classification



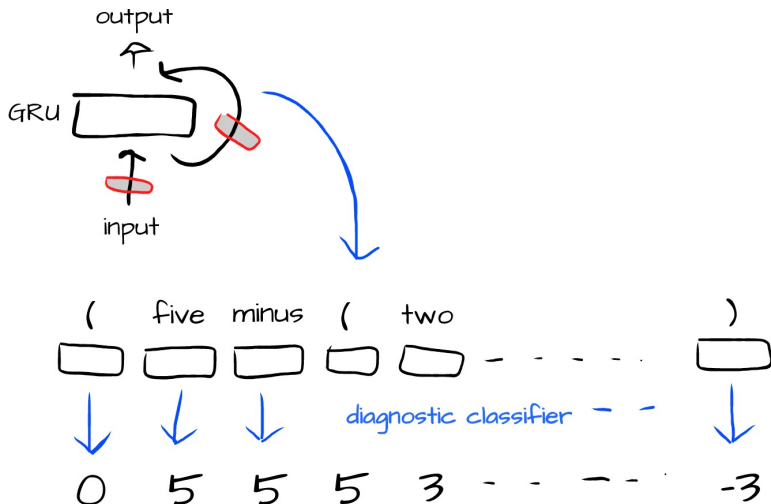
# How do we study the network?

## Diagnostic Classification



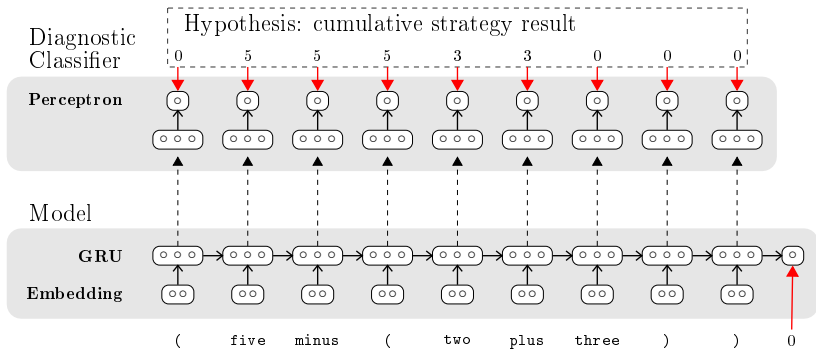
# How do we study the network?

## Diagnostic Classification



# How do we study the network?

## Diagnostic Classification



## Hypotheses

```

      minus_scope3+      1 1      1 1 1 1
      minus_scope2+      1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
      minus_scope1+      1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
close_minus_scope1+ 0 0 0 0 1 1 1 2 3 3 3 4 4 4 4 3 2 2 3 3 3 3 2 1 0 0 0 1 1 1 1 1 0 0
      . ( ( -2 - ( 6 - ( ( 8 + ( -3 - 10 ) ) - ( -2 - 10 ) ) ) ) - ( 1 - -8 ) )
      mode      + + + - - - + + + + + + - - + + - - - + + - + - + - - - + + - +
switch_mode      1      1      1 1 1 1 1 1 1 1 1 1 1 1 1 1

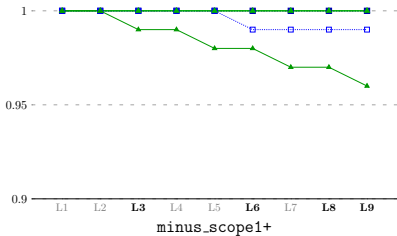
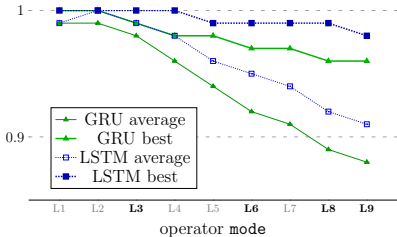
```

## Hypotheses

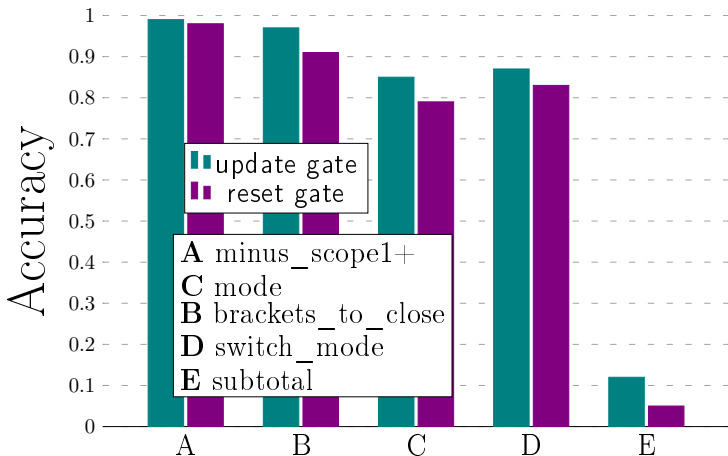
```

      minus_scope3+      1 1      1 1 1 1      1 1 1 1
      minus_scope2+      1 1 1 1 1 1 1 1 1 1 1 1 1 1      1 1
      minus_scope1+      1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1      1 1 1 1 1
close_minus_scope1+ 0 0 0 0 1 1 1 2 3 3 3 4 4 4 4 3 2 2 3 3 3 3 2 1 0 0 0 1 1 1 1 1 0 0
      . ( ( -2 - ( 6 - ( ( 8 + ( -3 - 10 ) ) - ( -2 - 10 ) ) ) ) - ( 1 - -8 ) )
      mode      + + + - - - + + + + + + - - + + - - + + - + - - - + + - +
switch_mode      1      1      1      1      1      1 1 1 1 1 1      1      1 1

```



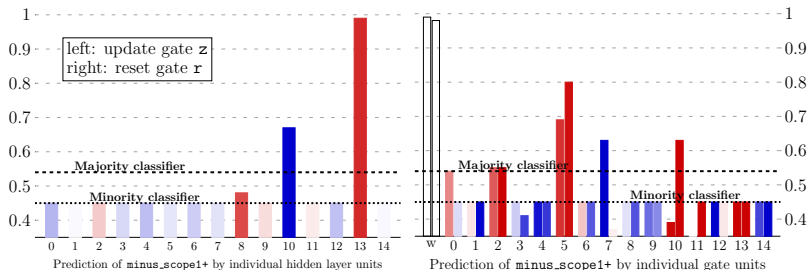
## How about the gates?



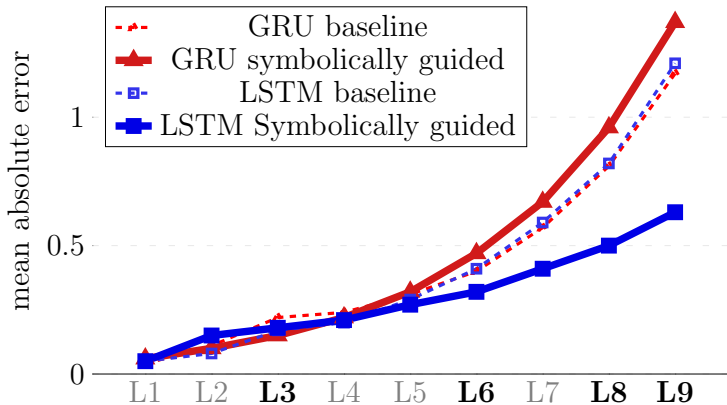


# Using diagnostic classifier weights

What happens where?



## Symbolic Guidance



## Future work

# Now what?

1. Understanding what learning biases we need?
2. Injecting symbolic knowledge in neural networks?
3. Understanding if neural networks have linguistic knowledge?
4. ...