Exercise 2

type closetozeroroundoff

```
function B=closetozeroroundoff(A,p) A(abs(A)<10^{-p})=0; B=A; end
```

type symmetric

```
%Creates the function symmetric
function [] = symmetric(A)
n = size(A,1);
                    %Creates nxn matrix
                    %p=7 for closetozeroroundoff function
p = 7;
x = isequal(A,A'); %Checks for symmetry statement
%If not, outputs msg that matrix is not symmetric and terminates program
if x == 0
    fprintf('A is not symmetric')
    return
end
%Constructs an orthogonal diagonalization
[P,D] = eig(A)
%Verifies for orthogonal diagonalization
if closetozeroroundoff(A*P-P*D,p) == zeros(n) & ...
        closetozeroroundoff(inv(P)-P',p) == zeros(n)
    disp('AP = PD and P is orthogonal')
else
    disp('What is wrong?!')
end
end %end of function
```

%(a) A=[2 -1 1;-1 2 -1;1 -1 2]

```
A = 3 \times 3
2 -1 1
-1 2 -1
1 -1 2
```

symmetric(A)

```
P = 3 \times 3
                        -0.5774
               0.7071
    0.4082
   -0.4082
               0.7071
                          0.5774
   -0.8165
                         -0.5774
D = 3 \times 3
    1.0000
                                0
         0
               1.0000
                                0
                          4.0000
AP = PD and P is orthogonal
```

```
A = 3 \times 3 
 2 -1 1 
 -1 2 -2
```

```
1 -1 2
```

symmetric(A)

A is not symmetric

%(c) B=A*A'

```
B = 3 \times 3
6 -6 5
-6 9 -7
5 -7 6
```

symmetric(B)

```
P = 3×3
    -0.0820     0.8577     0.5075
    0.5912     0.4518     -0.6681
    0.8024     -0.2453     0.5441

D = 3×3
    0.3315     0     0
    0     1.4096     0
    0     0     19.2588

AP = PD and P is orthogonal
```

%(d) A=[3 1 1;1 3 1;1 1 3]

$$A = 3 \times 3$$

$$3 \qquad 1 \qquad 1$$

$$1 \qquad 3 \qquad 1$$

$$1 \qquad 1 \qquad 3 \qquad 3$$

symmetric(A)

```
P = 3×3

0.4082  0.7071  0.5774

0.4082  -0.7071  0.5774

-0.8165  0  0.5774

D = 3×3

2.0000  0  0

0  2.0000  0

0  5.0000

AP = PD and P is orthogonal
```

%(e) A=[5 8 -4;8 5 -4;-4 -4 -1]

$$A = 3 \times 3$$

$$5 \quad 8 \quad -4$$

$$8 \quad 5 \quad -4$$

$$-4 \quad -4 \quad -1$$

symmetric(A)

```
0 -3.0000 0 15.0000 AP = PD and P is orthogonal
```

%(f)

A=[4 3 1 1; 3 4 1 1 ; 1 1 4 3; 1 1 3 4]

 $A = 4 \times 4$

symmetric(A)