

```
In[2]:= a = 0; b = 0.6; p[x_] = 3 + x; f[x_] =  $\frac{2}{7 + x^2}$ ; n = 4;
```

```
{Minimize[{p[x], a ≤ x ≤ b}, x][[1]] ≥ 0,  $\int_a^b p[x] \, dx > 0$ }
```

[минимизировать](#)

```
Out[3]= {True, True}
```

```
In[4]:=  $\omega_n[x_] = x^{n+1} + \sum_{k=0}^n c_k x^k$ ;
```

```
eqns = Table[ $\int_a^b p[x] \omega_n[x] x^i \, dx == 0$ , {i, 0, n}];
```

[таблица значений](#)

```
koef = Solve[eqns, {}] // Flatten;
```

[решить уравнения](#) [уплостить](#)

```
In[7]:=  $\omega_n[x_] = \omega_n[x] /. koef$ 
```

```
Out[7]=  $-0.000321888 + 0.015865 x - 0.183238 x^2 + 0.80833 x^3 - 1.5069 x^4 + x^5$ 
```

```
In[8]:= kor = Solve[ $\omega_n[x] == 0$ , x] // Flatten;
```

[решить уравнения](#) [уплостить](#)

```
In[9]:= Do[Print[{xk = kor[[k+1, 2]], a < xk < b}], {k, 0, n}]
```

[... печатать](#)

```
{0.0286149, True}
```

```
{0.140279, True}
```

```
{0.302482, True}
```

```
{0.46325, True}
```

```
{0.572276, True}
```

```
In[10]:= Do[Print[xk != xk+1], {k, 0, n-1}]
```

[... печатать](#)

```
True
```

```
True
```

```
True
```

```
True
```

```
In[11]:= Do[Print[{Ak =  $\int_a^b p[x] \left( \prod_{i=0}^{k-1} \frac{(x - x_i)}{x_k - x_i} \right) \left( \prod_{i=k+1}^n \frac{(x - x_i)}{x_k - x_i} \right) \, dx$ , Ak > 0}], {k, 0, n}]
```

[... печатать](#)

```
{0.218656, True}
```

```
{0.454889, True}
```

```
{0.563354, True}
```

```
{0.49283, True}
```

```
{0.250271, True}
```

```
In[12]:= Table[Chop[ $\int_a^b p[x] x^i dx - \sum_{k=0}^n A_k x_k^i$ ,  $10^{-8}$ ] == 0, {i, 0, 2 n + 1}]
```

$$\int_a^b p[x] x^{2n+2} dx = \sum_{k=0}^n A_k x_k^{2n+2}$$

```
Out[12]:= {True, True, True, True, True, True, True, True, True, True}
```

```
Out[13]:= True
```

```
In[14]:= IT =  $\int_a^b p[x] f[x] dx$ 
```

```
Out[14]:= 0.555882
```

```
In[15]:= IP =  $\sum_{k=0}^n A_k f[x_k]$ 
```

```
Out[15]:= 0.555882
```

```
In[16]:= M = Maximize[{Abs[D[f[x], {x, 2 n + 2}]], a ≤ x ≤ b}, x][[1]];
```

$$ER = \frac{M}{(2n+2)!} \int_a^b p[x] (\omega_n[x])^2 dx$$

```
Out[17]:=  $2.90748 \times 10^{-13}$ 
```

```
In[18]:= Abs[Chop[IT - IP,  $10^{-8}$ ]] < ER
```

```
Out[18]:= True
```

```
In[19]:=
```

```
In[20]:= Задание 2
```

```
Out[20]:= 2 Задание
```

```
In[21]:= eps =  $10^{-4}$ ;
```

```
M := Maximize[{Abs[D[f[x], {x, 2 n + 2}]], a ≤ x ≤ b}, x][[1]];
```

$$\omega[x_] := \left( x^{n+1} + \sum_{k=0}^n c_k x^k \right) //.$$

$$\left( \text{Solve}\left[\text{Table}\left[\int_a^b p[x] \left(x^{n+1} + \sum_{k=0}^n c_k x^k\right) x^i dx == 0, \{i, 0, n\}\right], \{c\}\right] // \text{Flatten}\right)$$

$$\text{While}\left[\left(ER = \frac{M}{(2n+2)!} \int_a^b p[x] (\omega[x])^2 dx\right) > \text{eps}, n++\right]$$

```
n
```

```
Out[25]:= 4
```

```

In[26]:= kor = Solve[ω[x] == 0, x] // Flatten;
           [решить уравнения] [уплостить]
Do[xk = kor[[k + 1, 2]], {k, 0, n}]
[оператор цикла]

Do[Ak = ∫ab p[x] (∏i=0k-1  $\frac{x - x_i}{x_k - x_i}$ ) (∏i=k+1n  $\frac{x - x_i}{x_k - x_i}$ ) dx, {k, 0, n}]
[оператор цикла]

IP = ∑k=0n Ak f[xk] // Simplify // N
           [упростить] [численное приближение]

Abs[Chop[IT - IP, 10-8]] < N[ER]
[аб... [отсечь малые числа] [численное приближение]

```

Out[29]= 0.555882

Out[30]= True